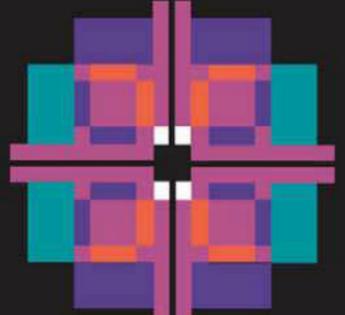
SYMMETRICAL PATTERNS



A Complete
Resource of Pattern
Designs Created
by Evolving
Symmetrical Shapes









Jay Friedenberg and Jacob Roesch

1001 SYMMETRICAL PATTERIS



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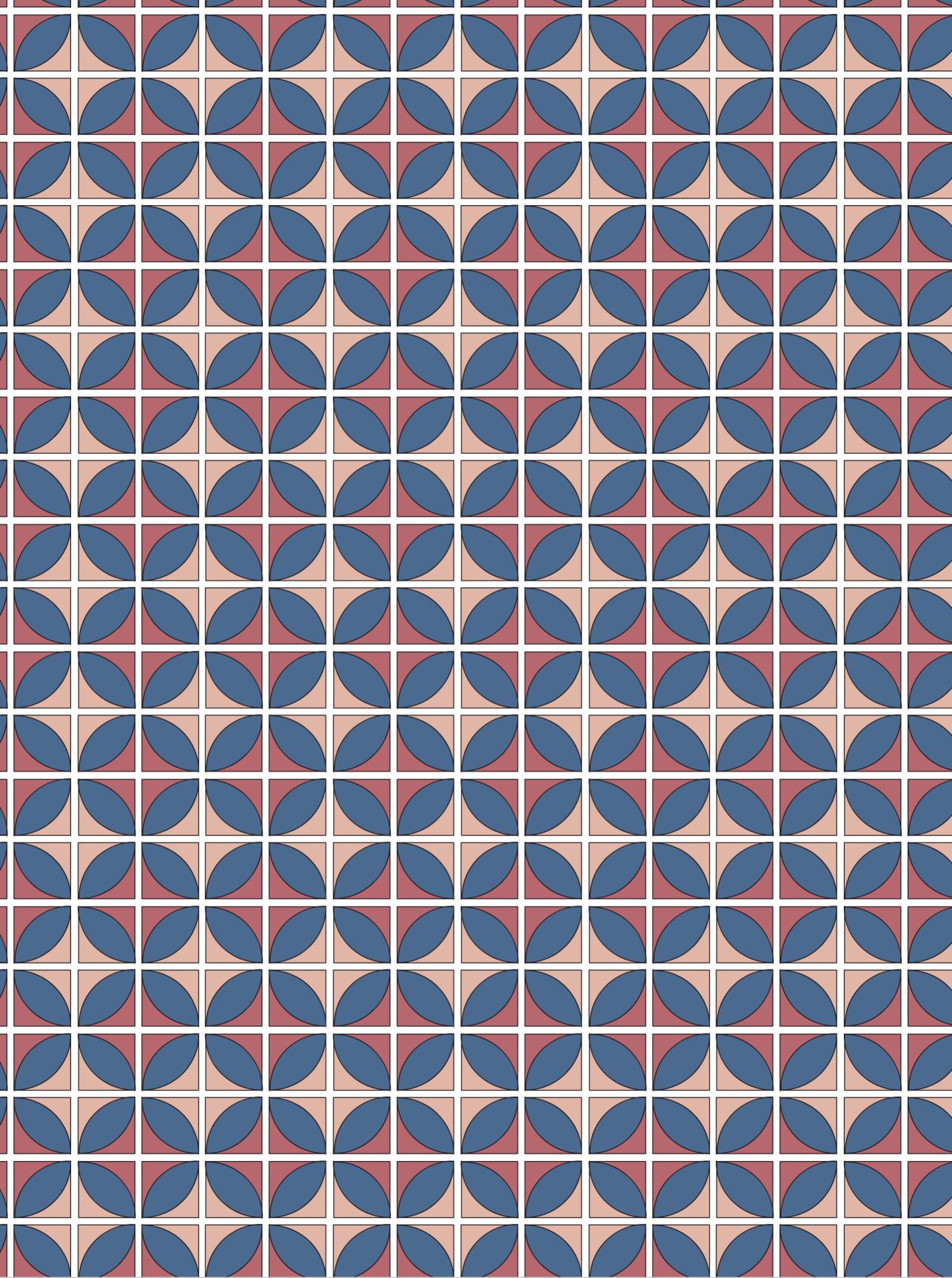
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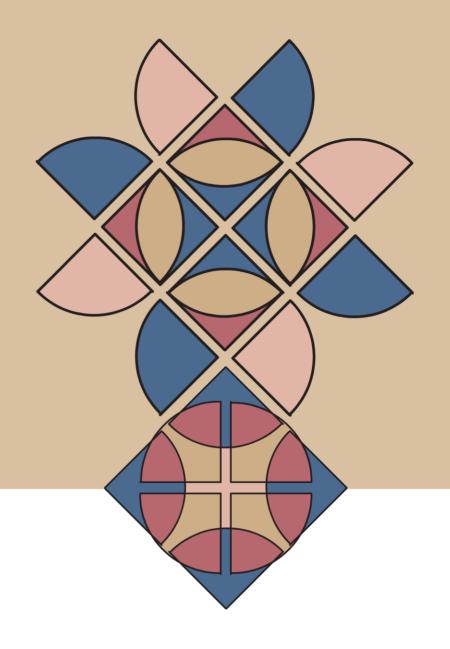
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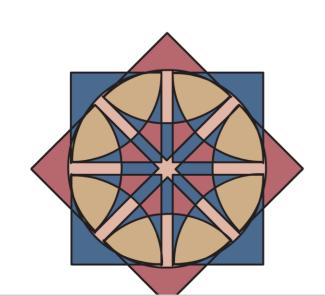
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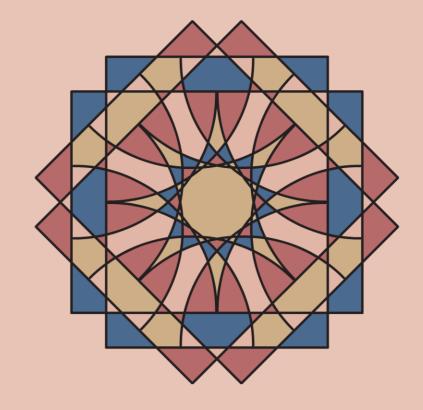
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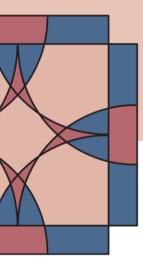


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Introduction





isual symmetry in a broad sense refers to self-similarity.

A pattern is symmetric if, after some operation, the pattern remains unchanged. There are three primary symmetry operations. A translation takes a pattern and simply moves it to a new location. We see the effect of translation in architecture, where columns repeat across the front of a building. In reflection a pattern is mirror-imaged or made bilateral with an axis defining the two opposite halves. Reflectional symmetry can be found in faces or bodies where one side corresponds to the other. Finally, there is rotation, where a pattern is spun about a point. Flower petals and wheel spokes are examples of rotational symmetry, since both are rotated about their centers.

Symmetry patterns are classified according to their dimensionality. A point or *finite symmetry* is a coherent single shape or object that is dimensionless because it is defined by its center. *One-dimensional symmetries* extend in a single direction only. Examples of these are decorative friezes or bands. There are a total of seven one-dimensional symmetry types. Each defined by the number and kind of symmetry operation applied. *Two-dimensional symmetries* extend outward in two directions and can



completely cover a planar surface. There are seventeen of these, again determined by the application of the number and kind of operation. Rugs and wallpaper are examples.

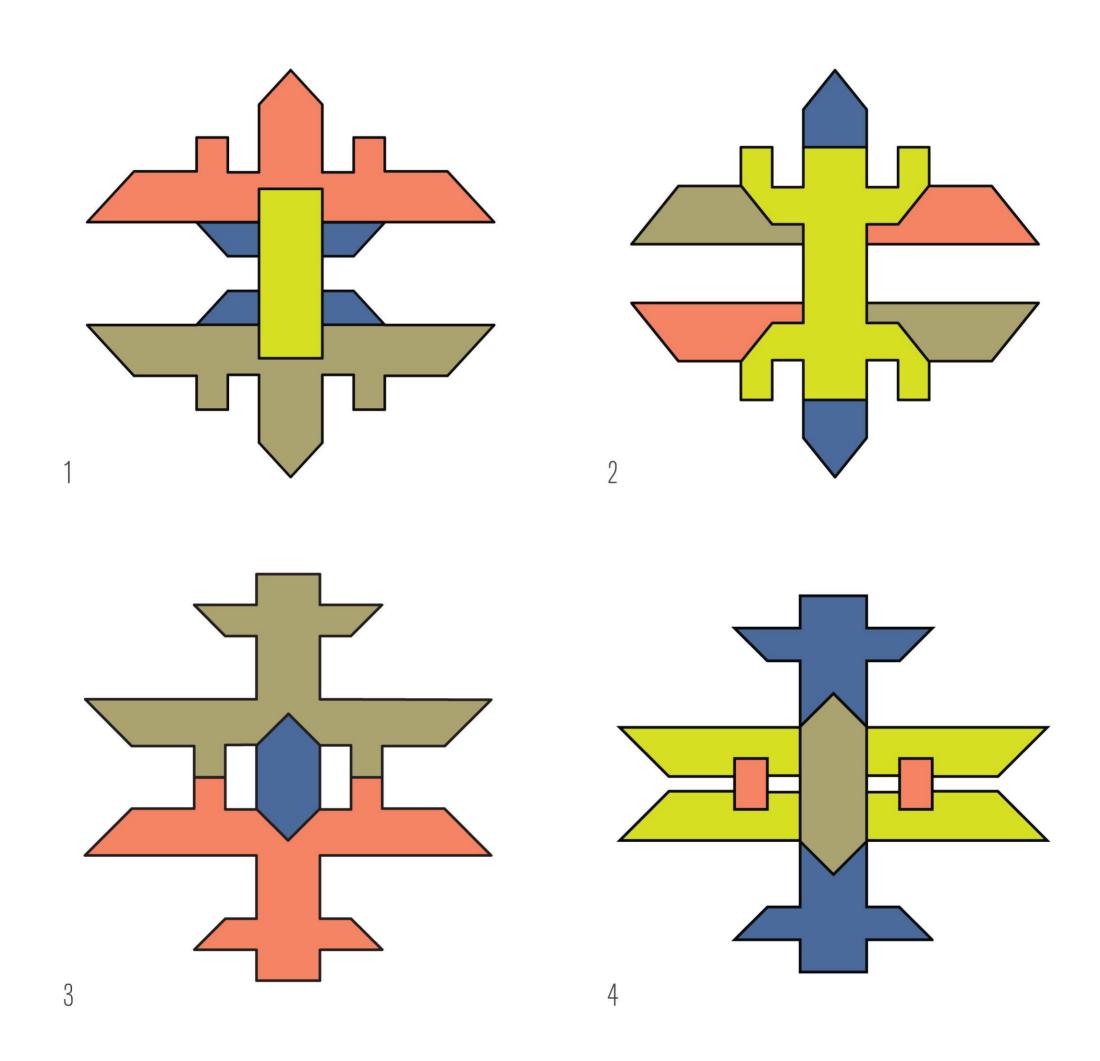
Symmetry is ubiquitous in the natural and artifactual world. Bilateral symmetry is found in biological organisms including most plants and animals, but we also see it in many human-constructed forms such as cars, airplanes, and furniture.³ It appears in the art of all human cultures, including weaving, baskets, pottery, tapestries, textiles, embroidery, tiles, and jewelry.⁴ Many of the plane symmetries can also be found as decorative art from around the world. All seventeen two-dimensional symmetry patterns have been found in the Alhambra.⁵

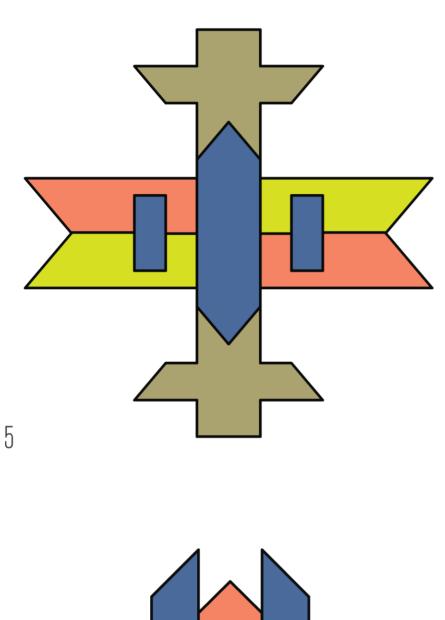
What is the enduring appeal of symmetry, and why does it seem to be regarded as universally aesthetic? There may be a biological basis. In psychology experiments, faces with greater reflectional symmetry are rated as more attractive. Some researchers argue that bilateral facial symmetry signals resistance to parasitic infection because infections during development disrupt the body's normal symmetrical growth processes, and because sexual selection of an immunocompetent partner would thus help to ensure fit offspring. However, this hypothesis cannot account for the allure of translational and rotational symmetries.

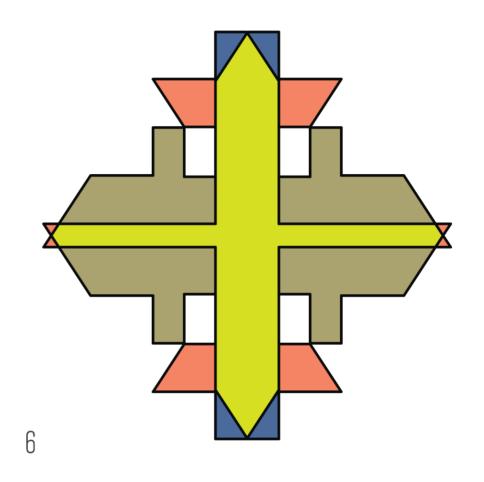
The patterns in this book are all finite-point symmetries forming single objects. The basis for each pattern is a motif that is translated, reflected, and rotated to create a new version of the motif that is then aligned with or superimposed upon itself. The motifs can be geometric, as in the case of squares, circles, and hexagons, or they can be representative of a shape such as a mushroom, ice cream cone, or kite. A number of the motifs we utilize here are inspired by existing designs from the history of decorative art and include Egyptian, Greek, Roman, Arabic, Indian, Japanese, Chinese, and Celtic as well as more modern computer-generated shapes.⁸

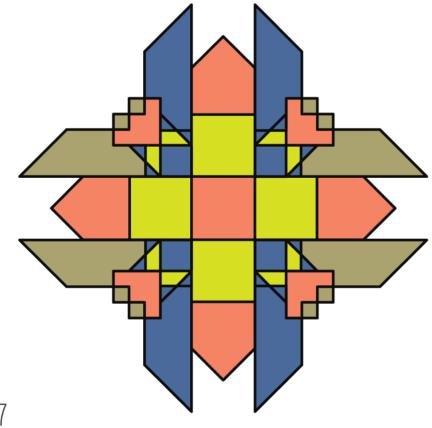
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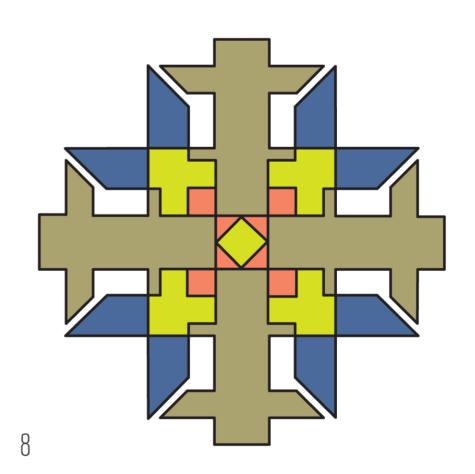
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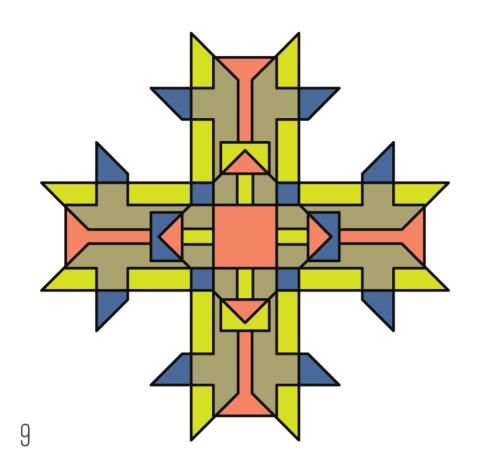


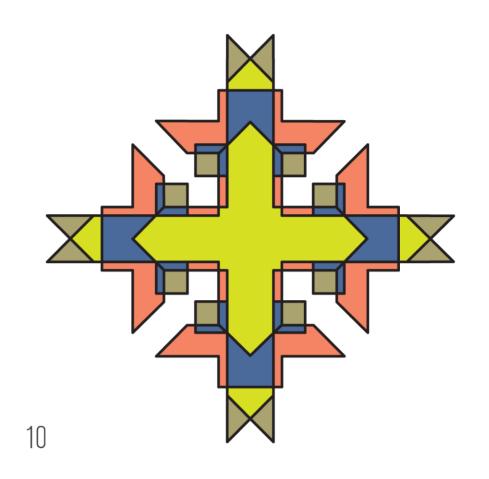


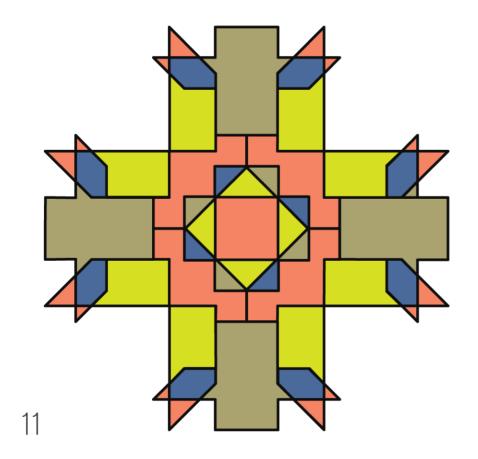


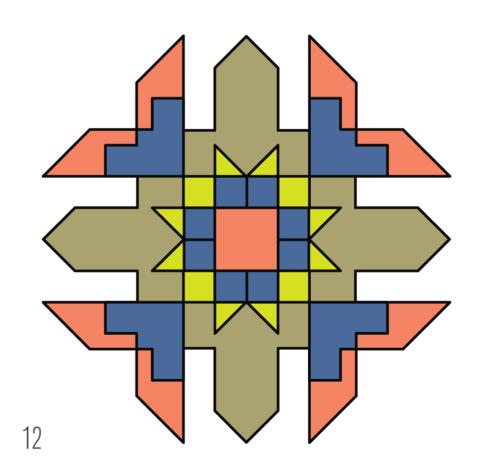


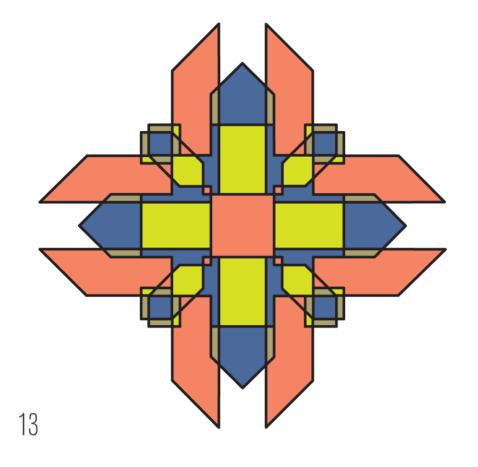
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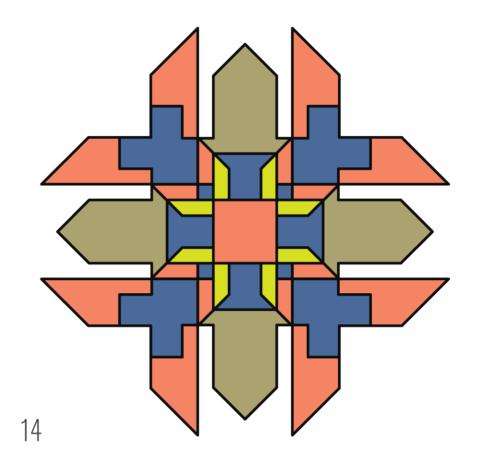


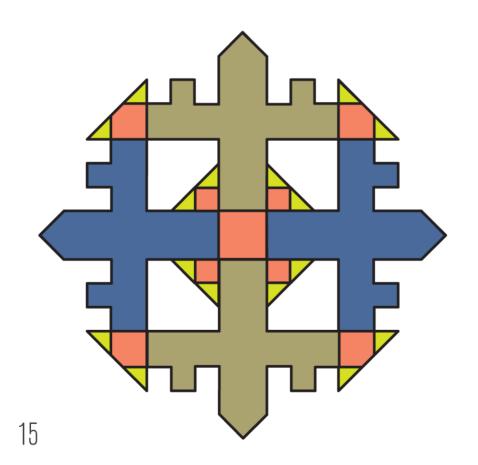


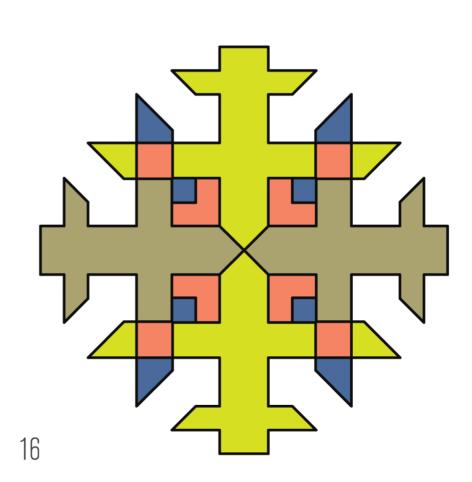




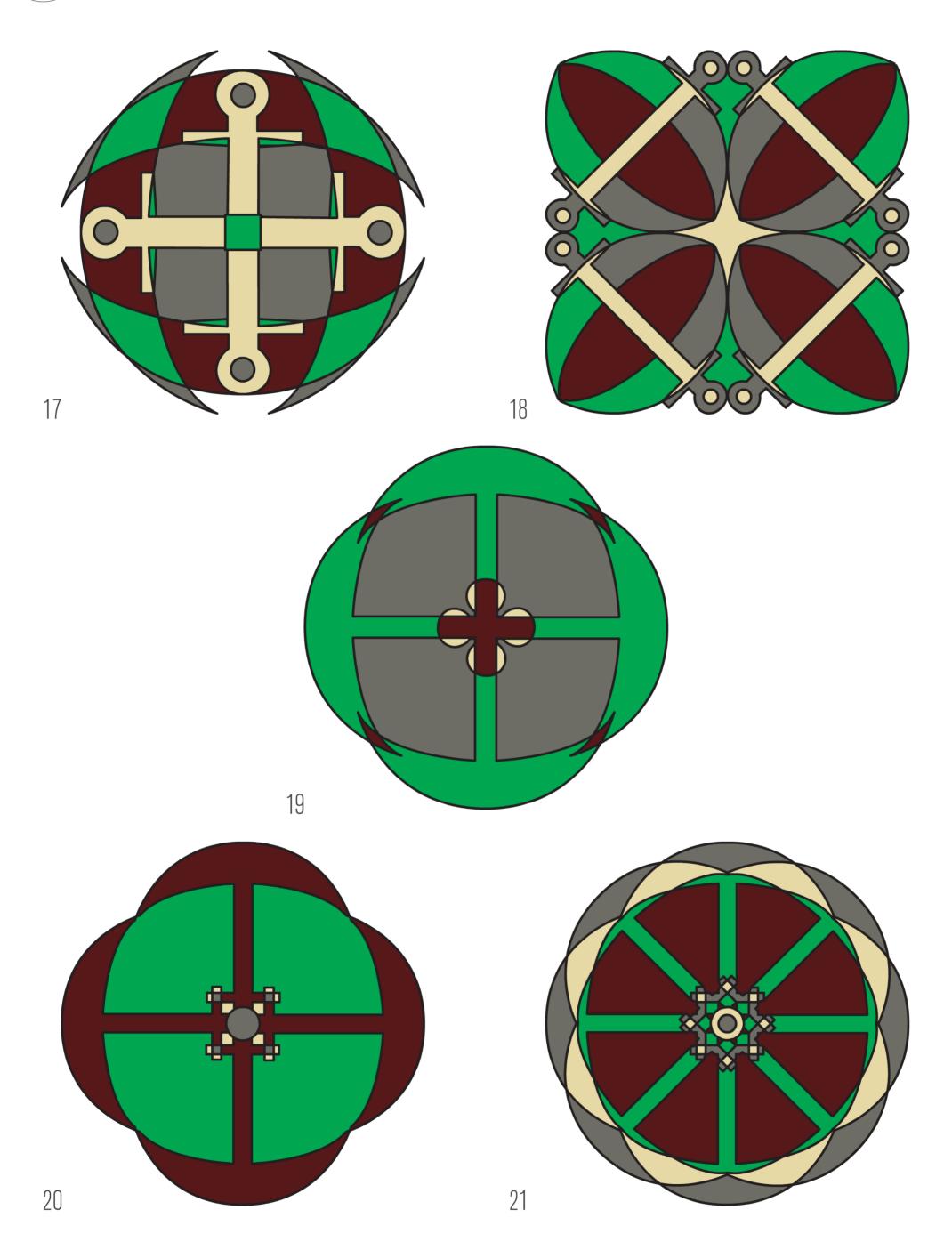


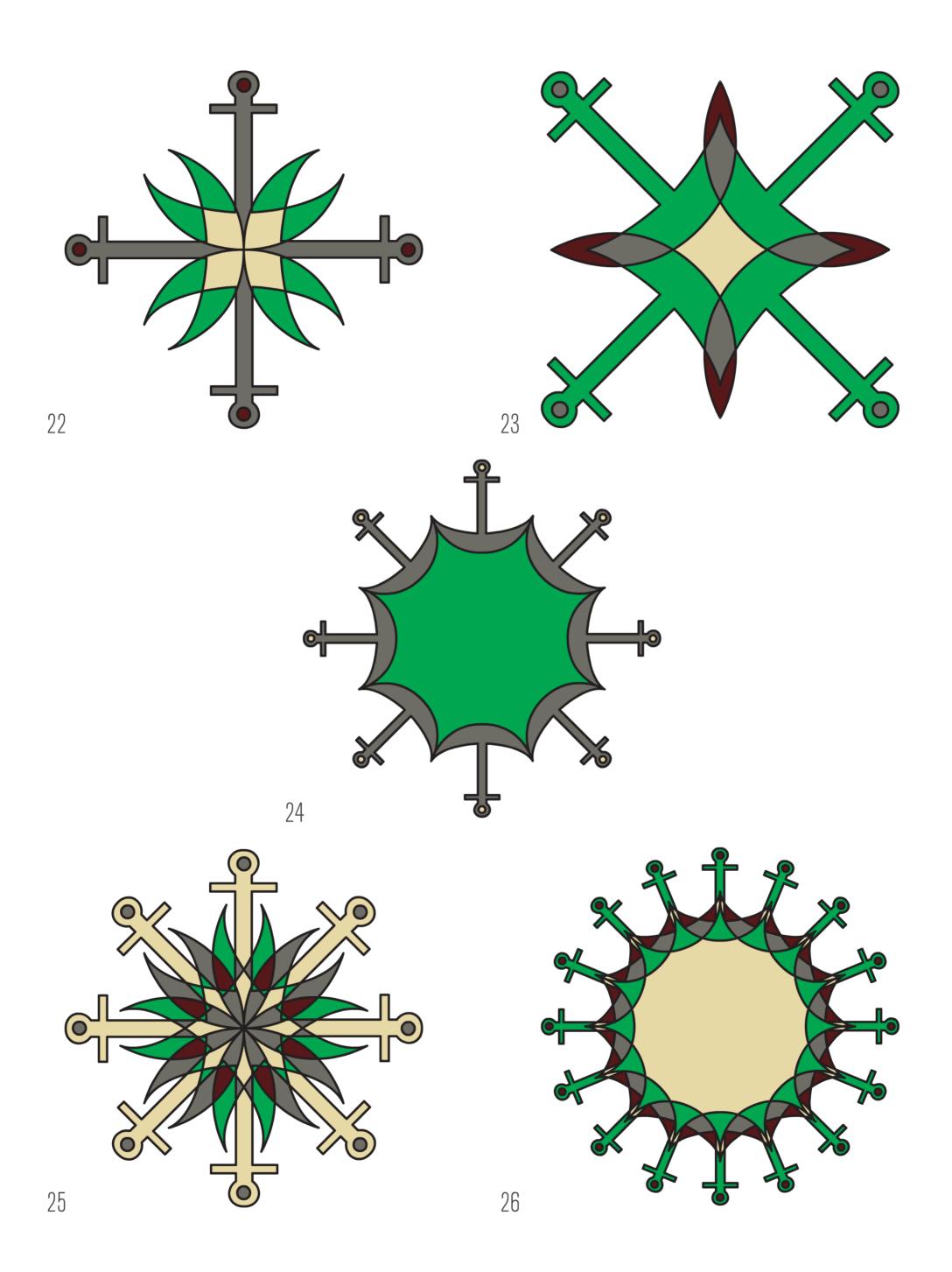




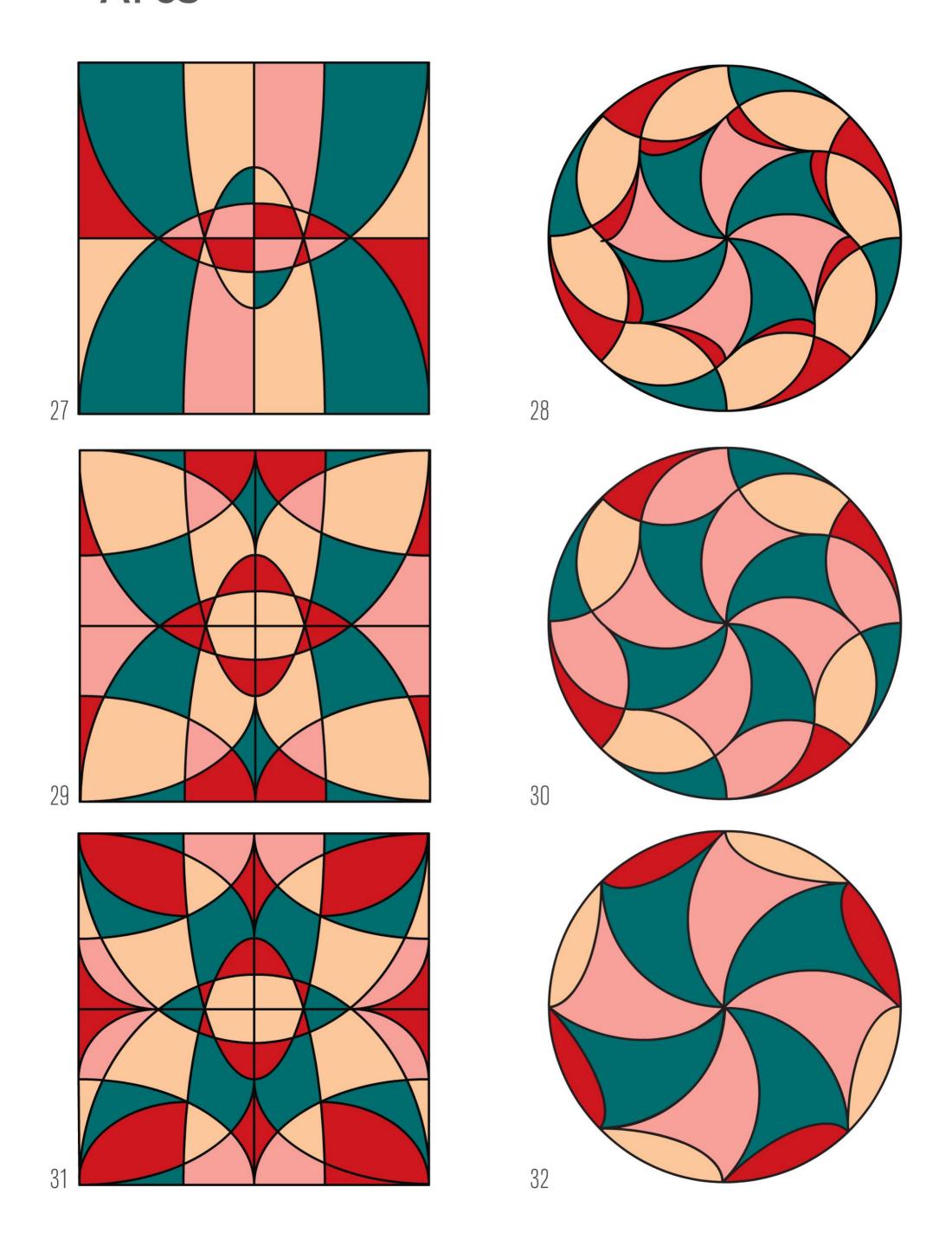


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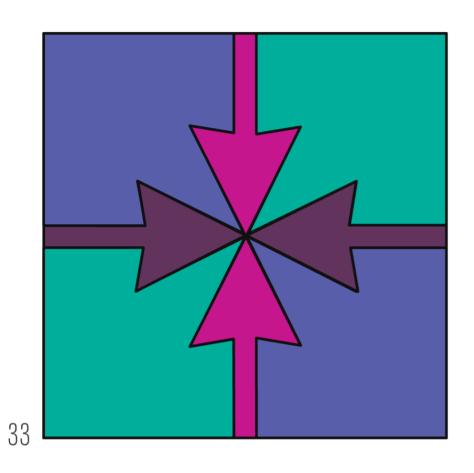


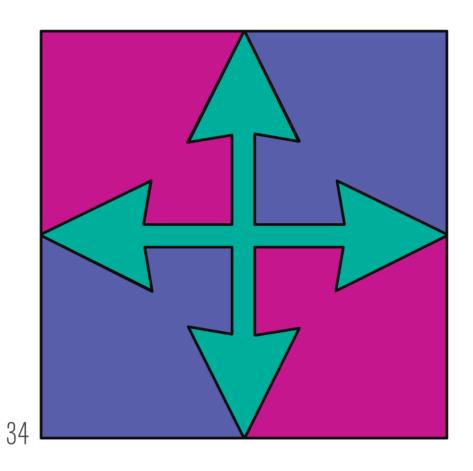


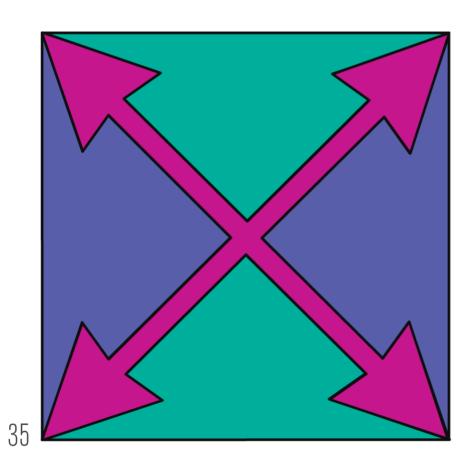
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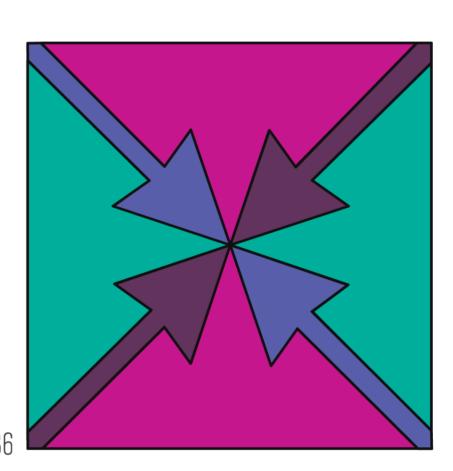


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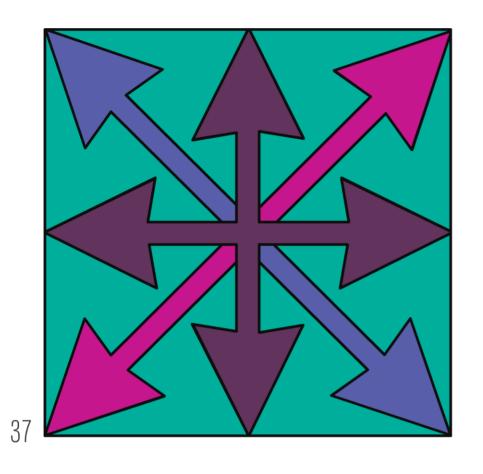


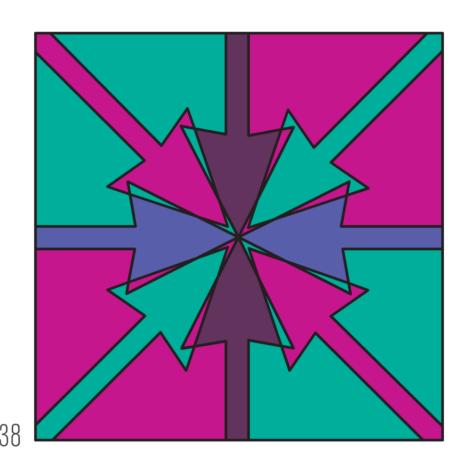


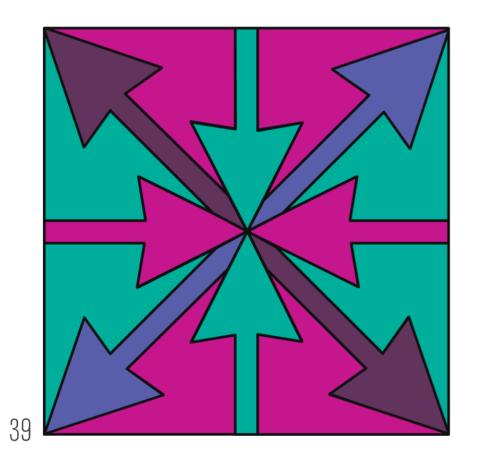


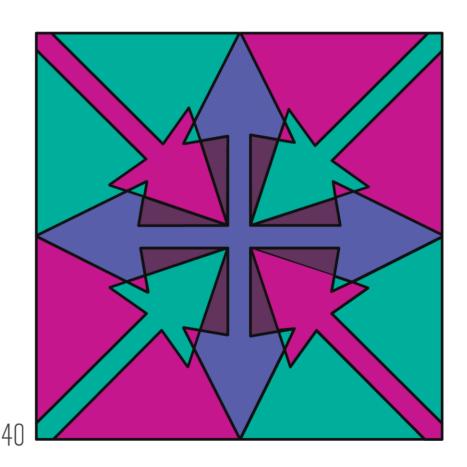


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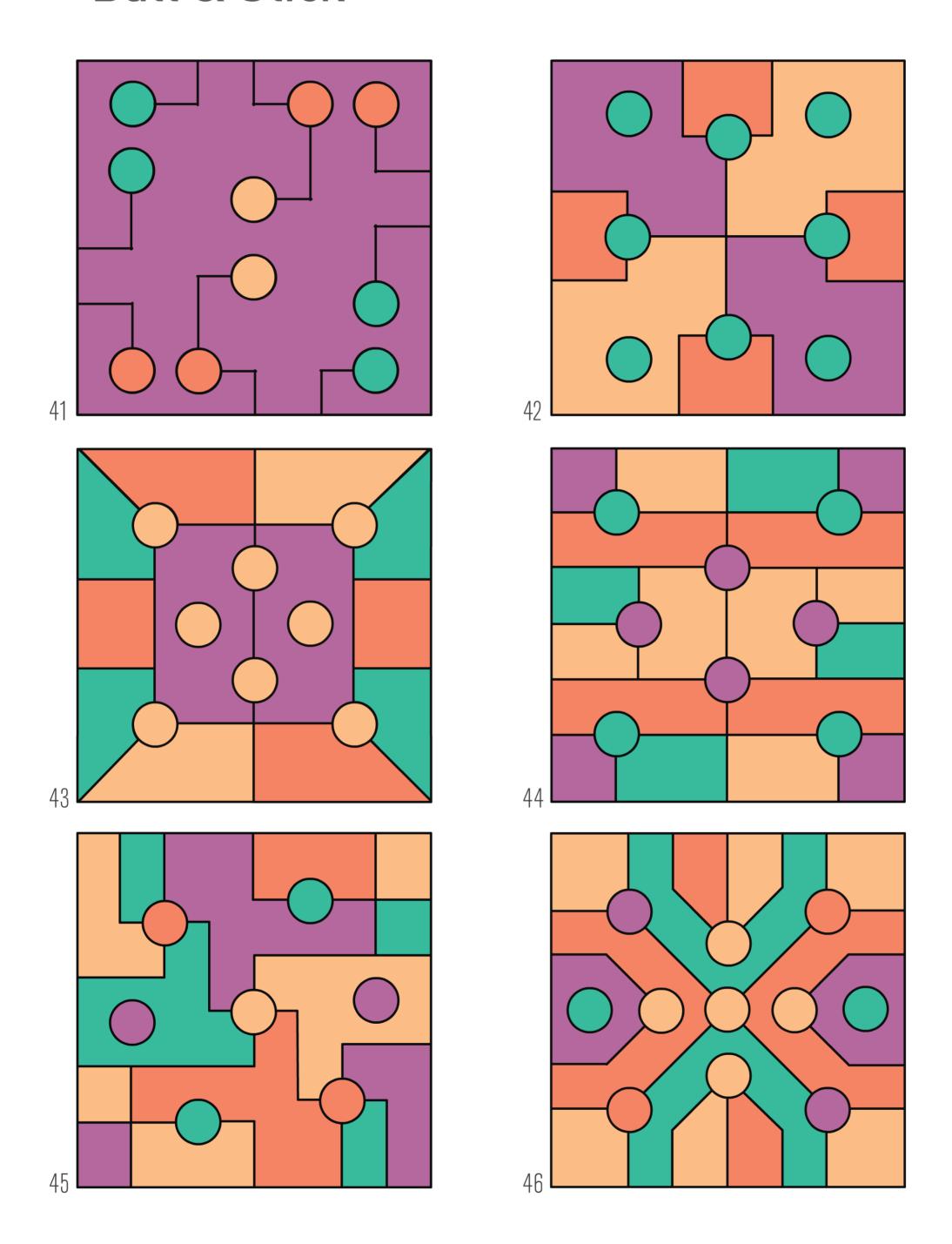




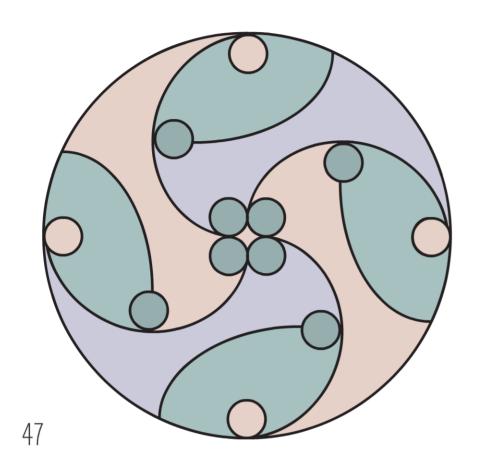


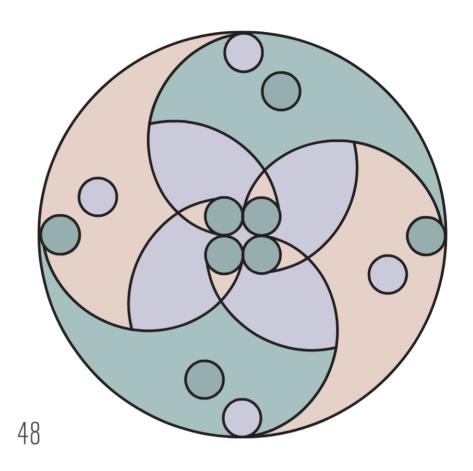


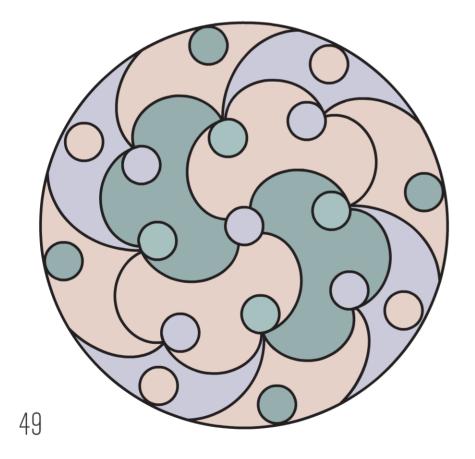
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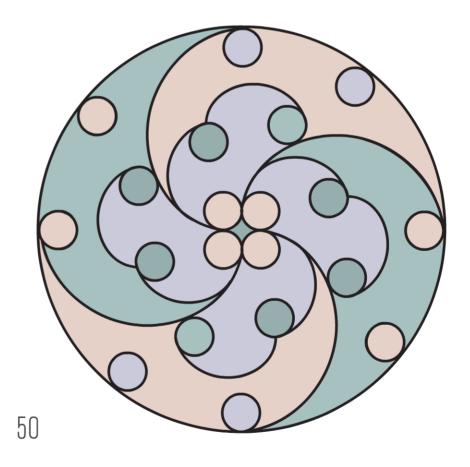


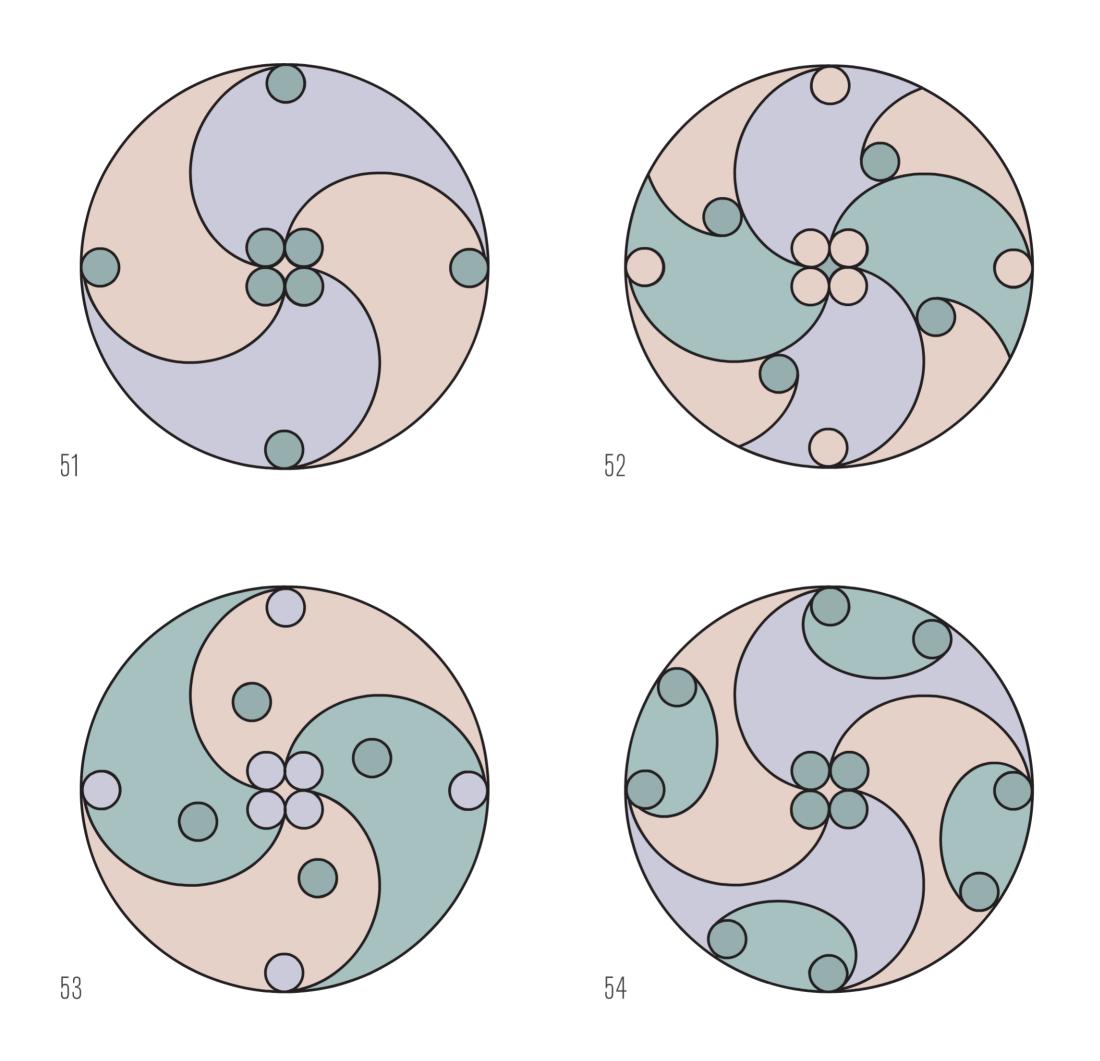
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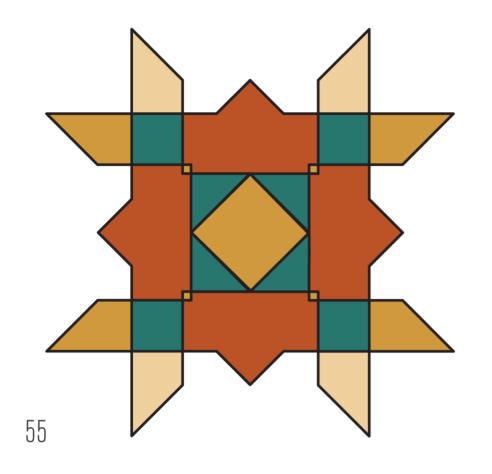


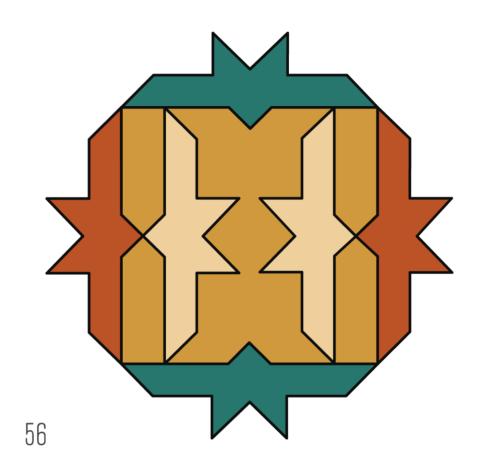


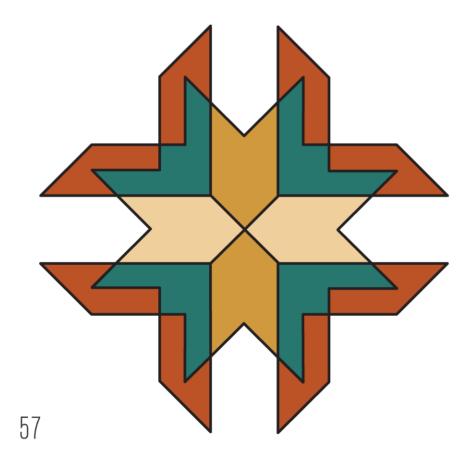


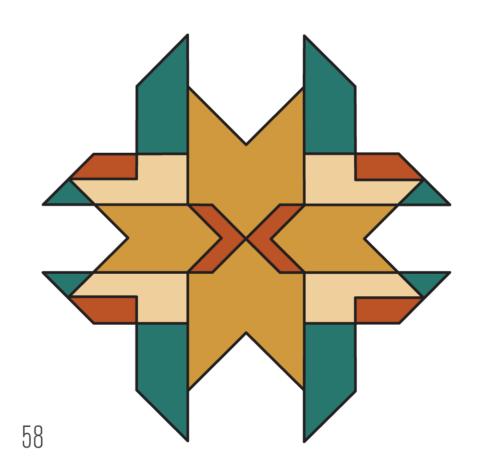


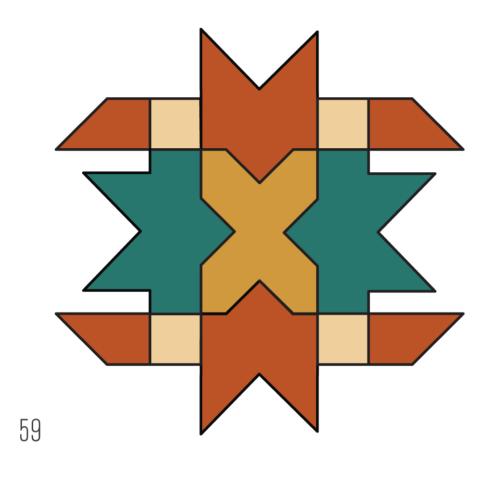
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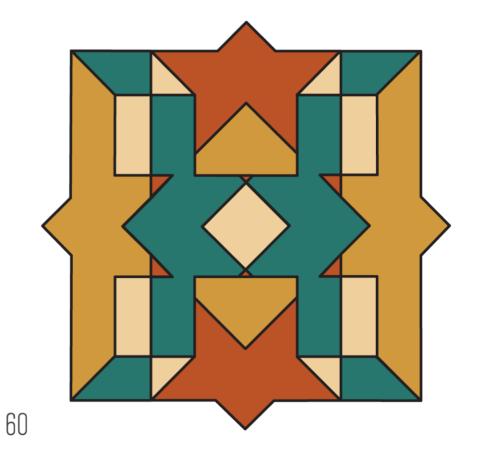


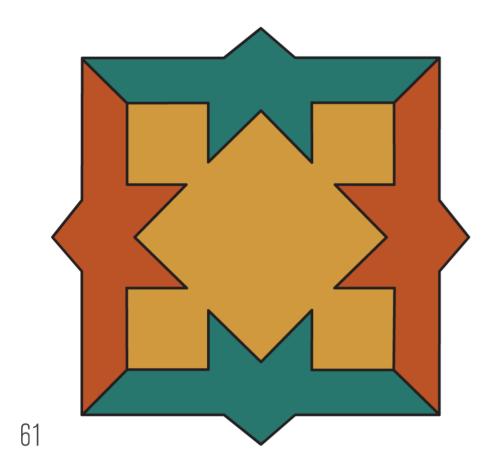


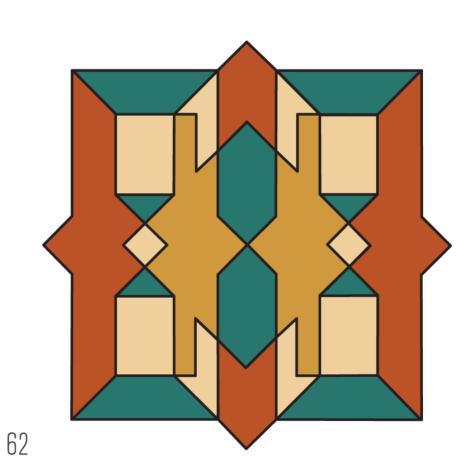




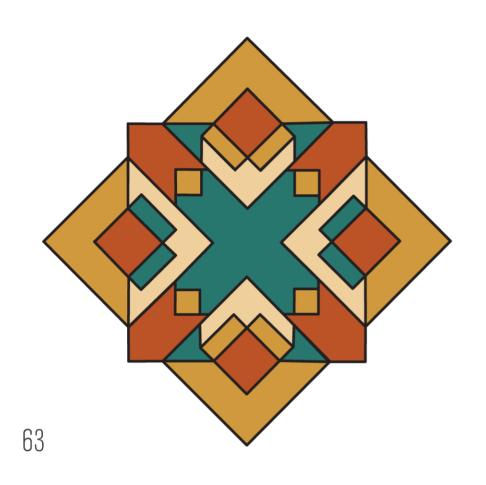


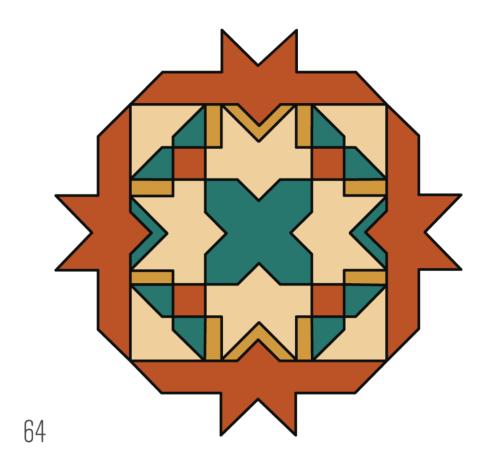


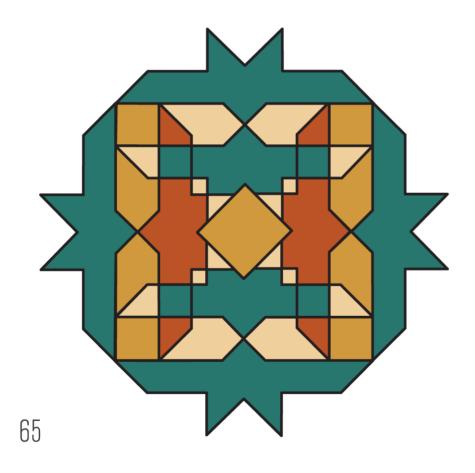


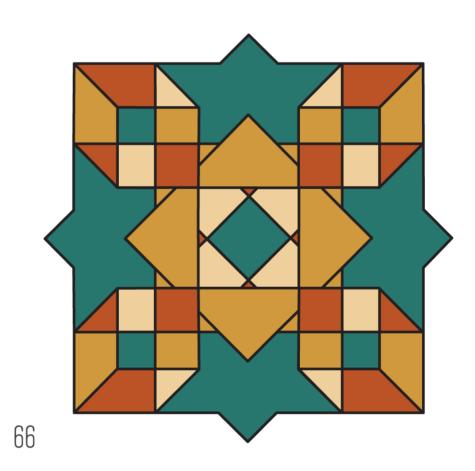


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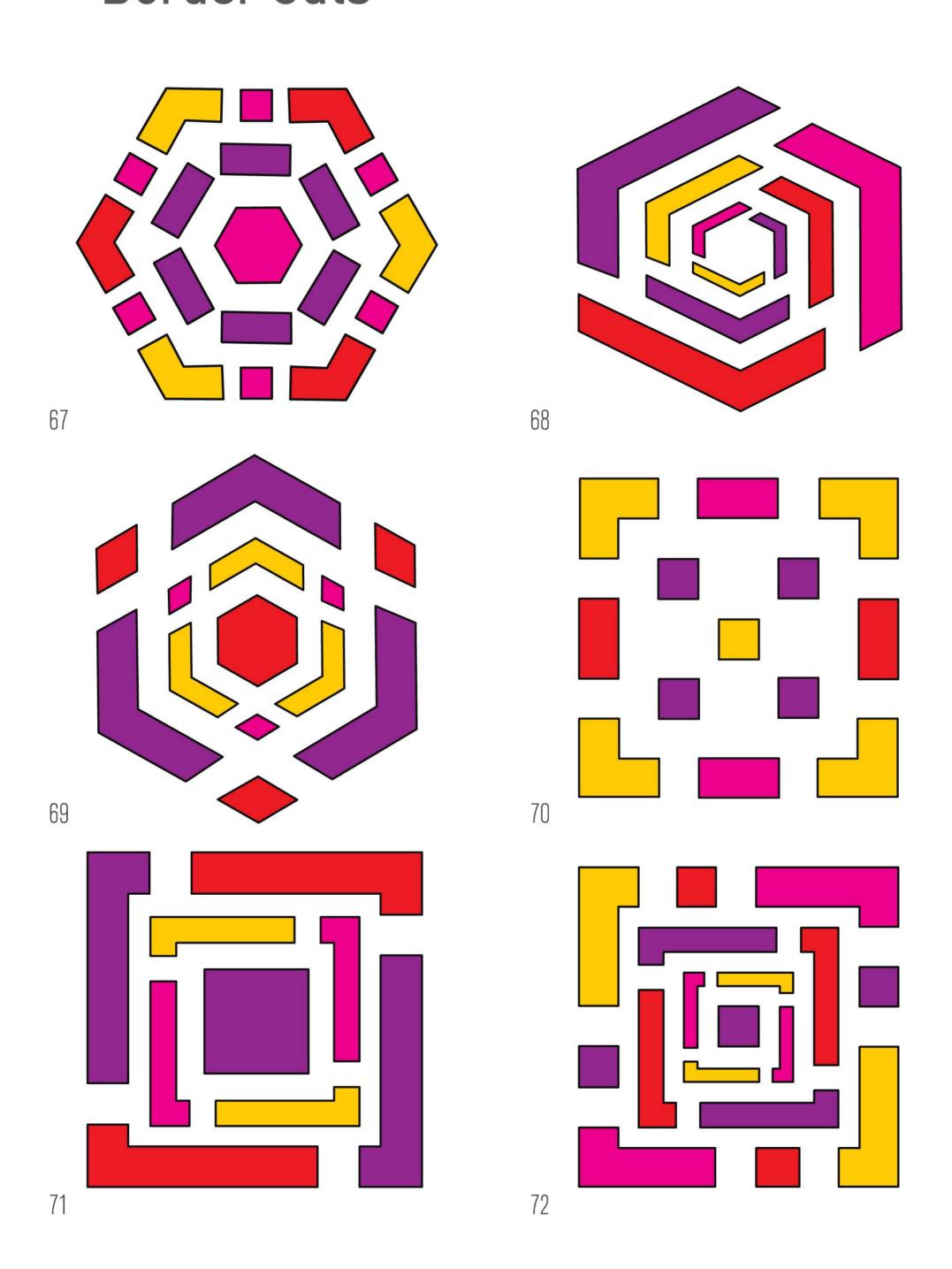




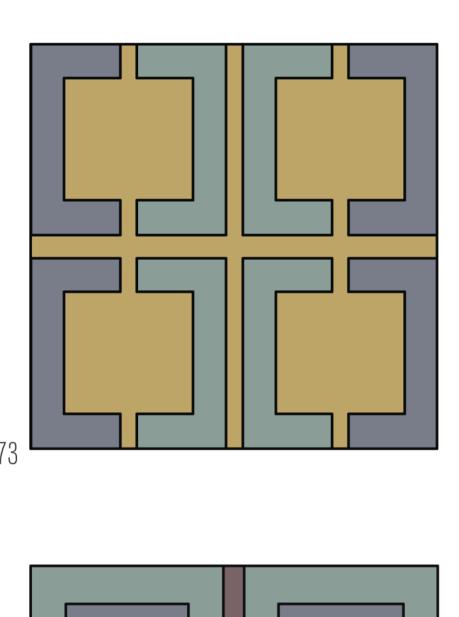


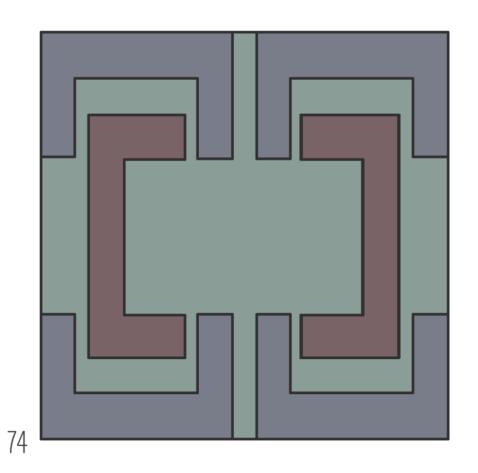


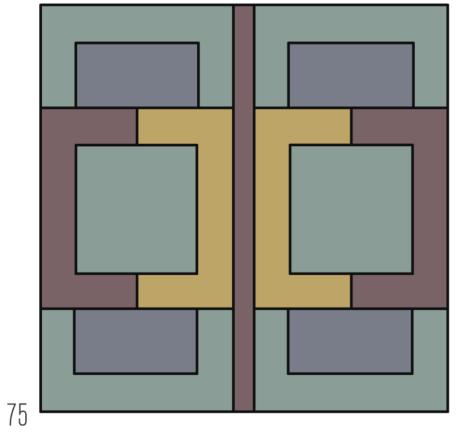
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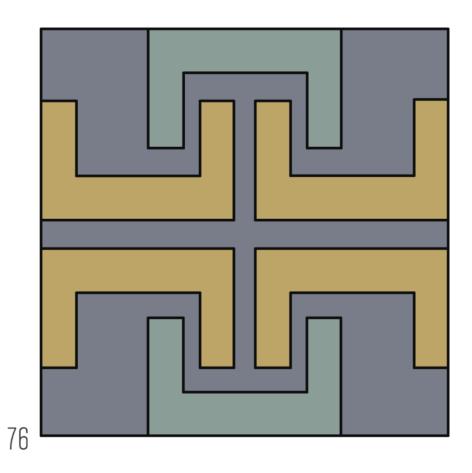


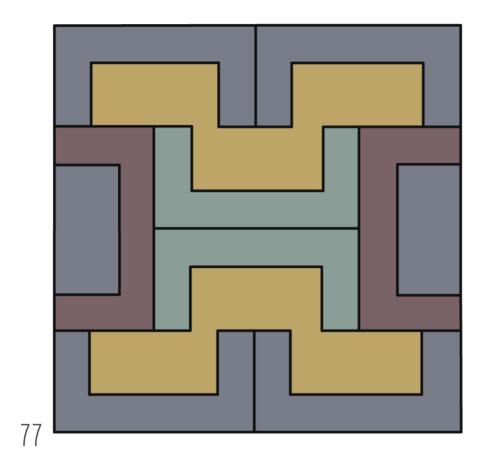
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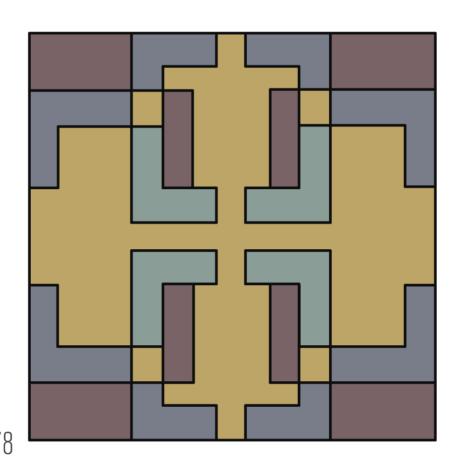


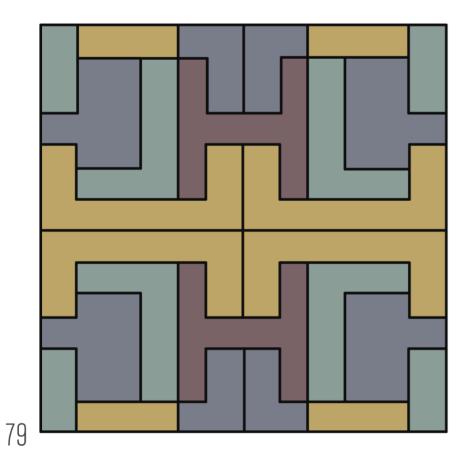


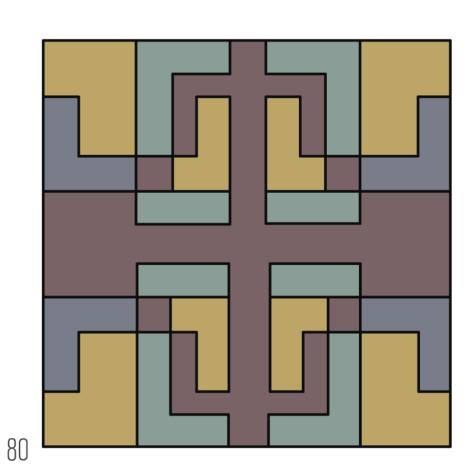




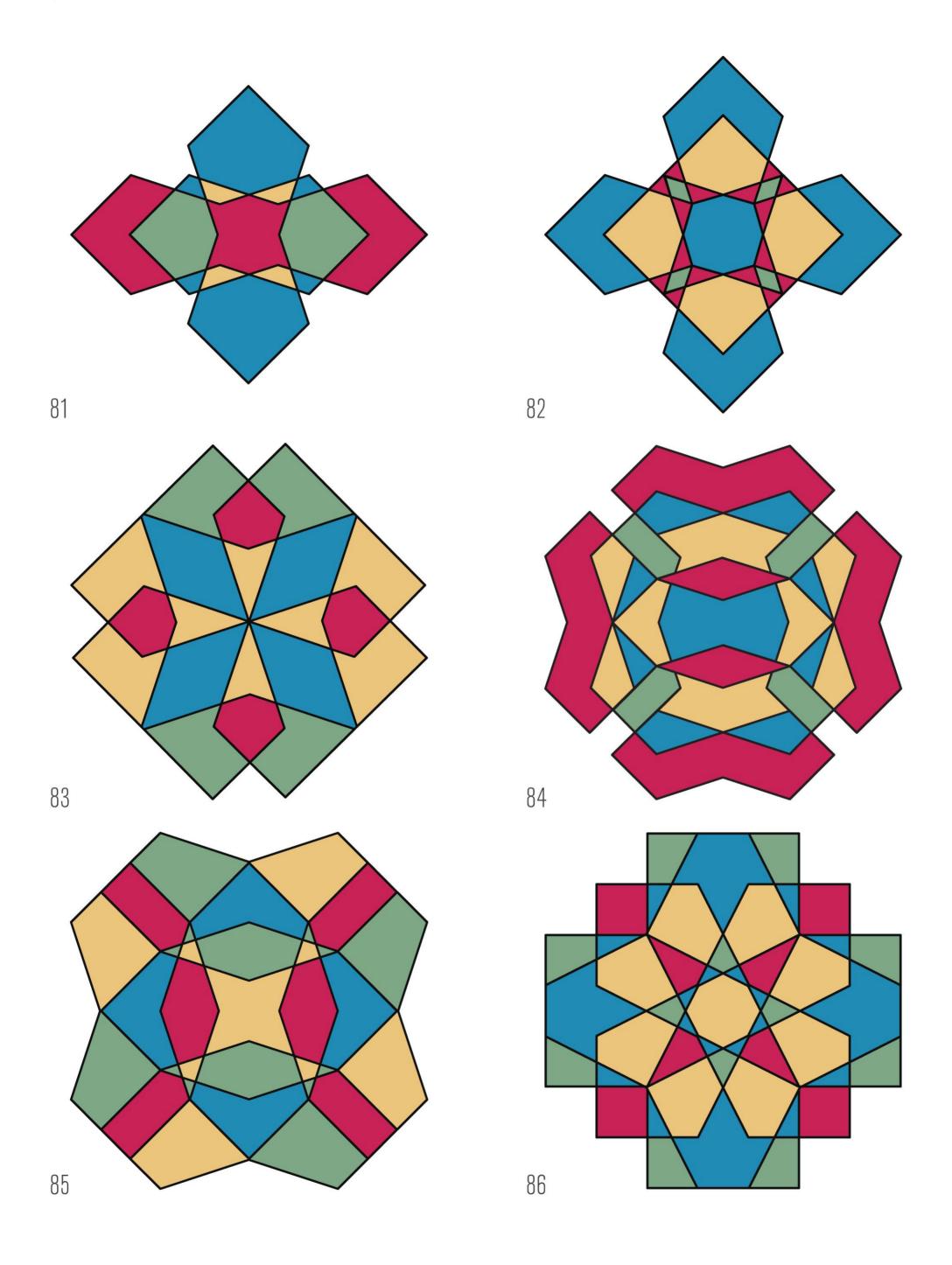


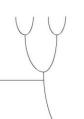




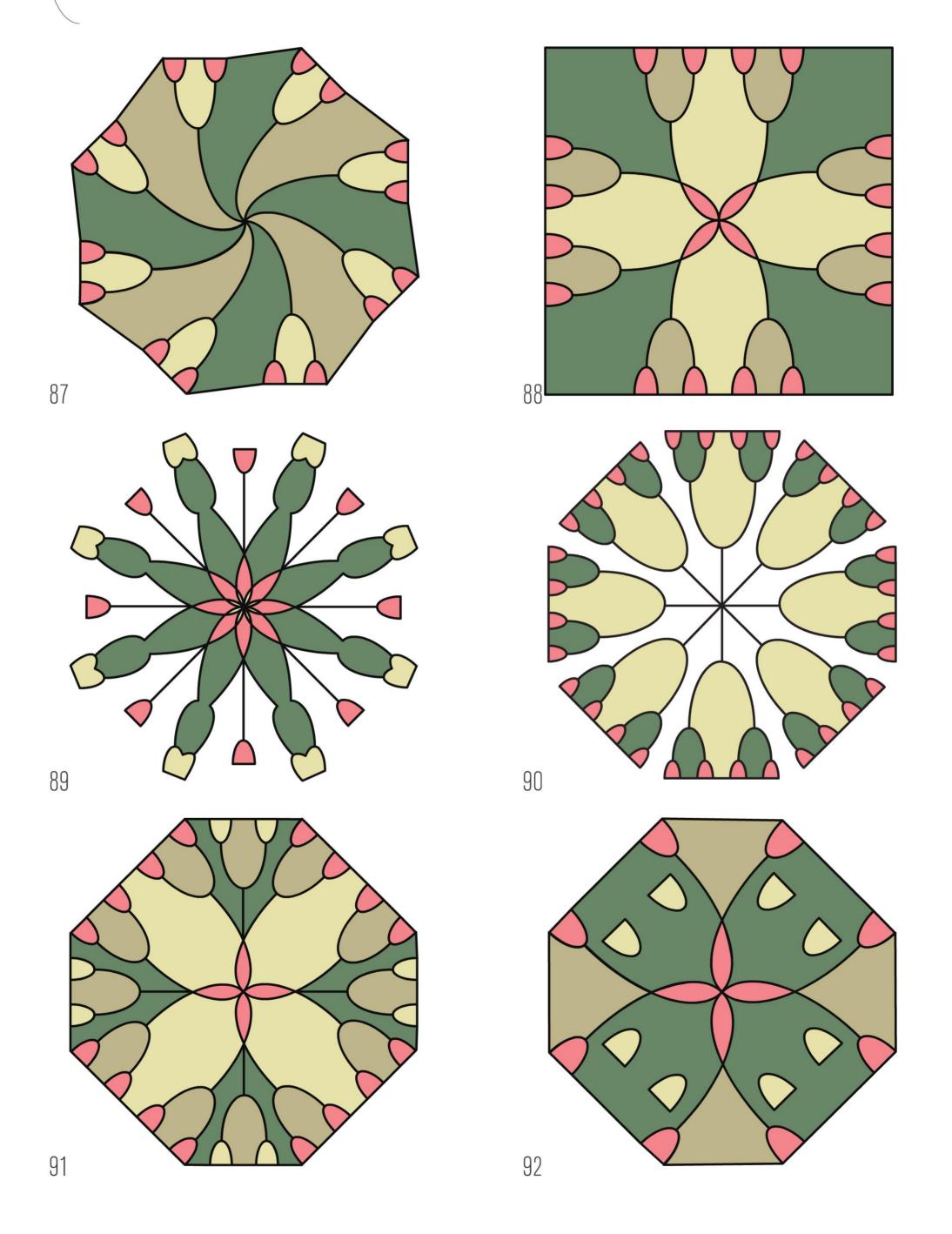


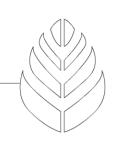
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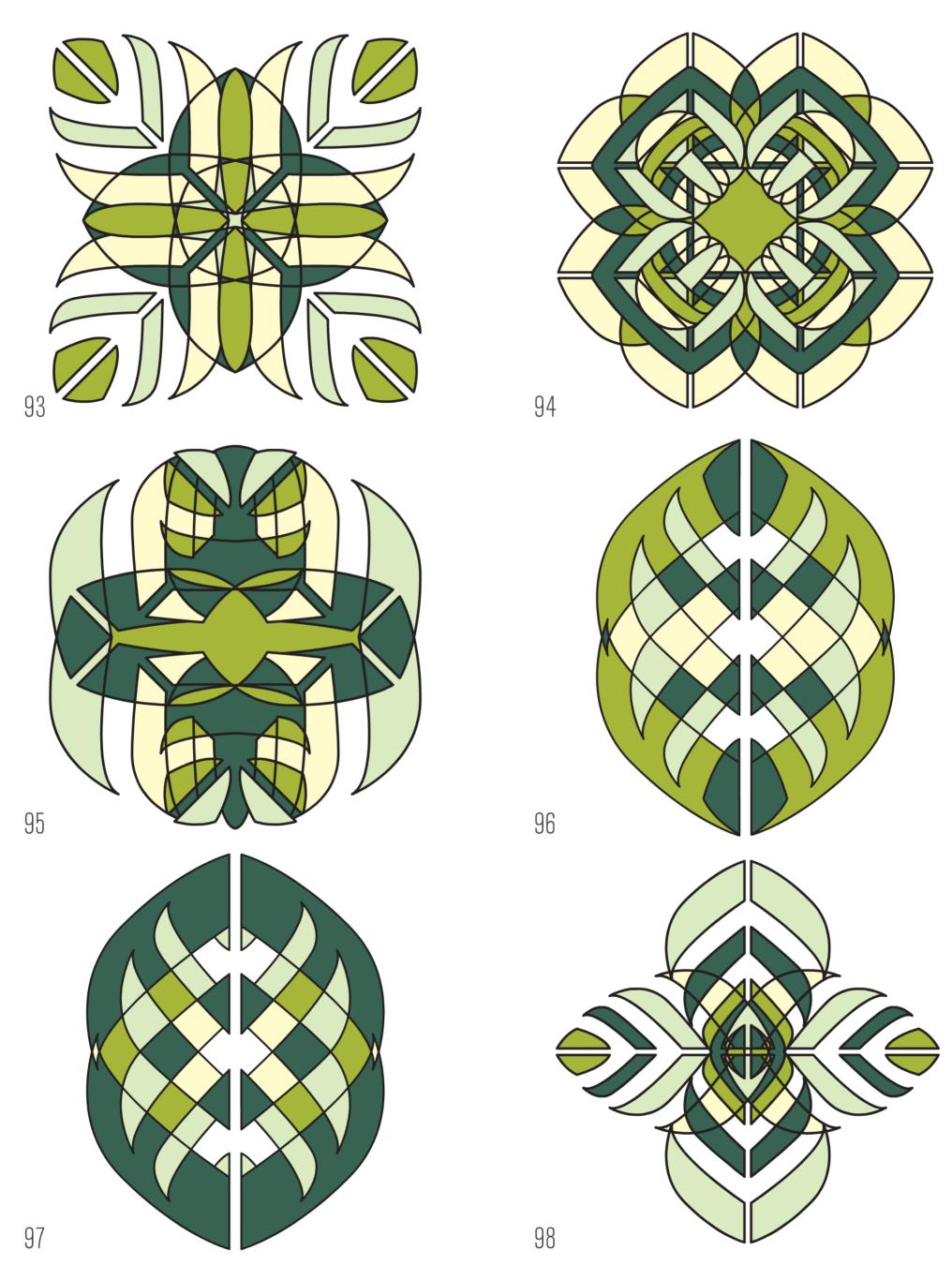


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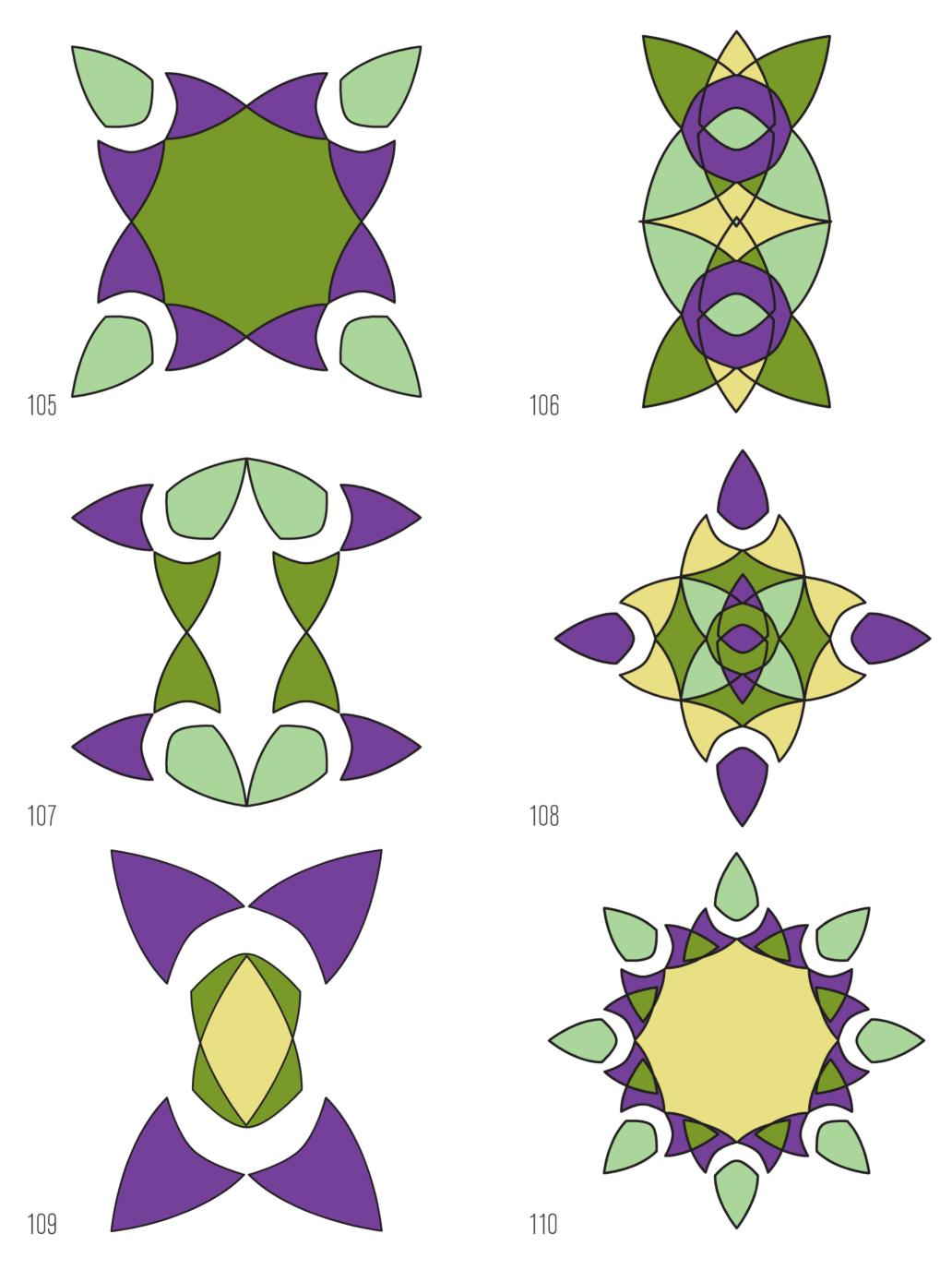


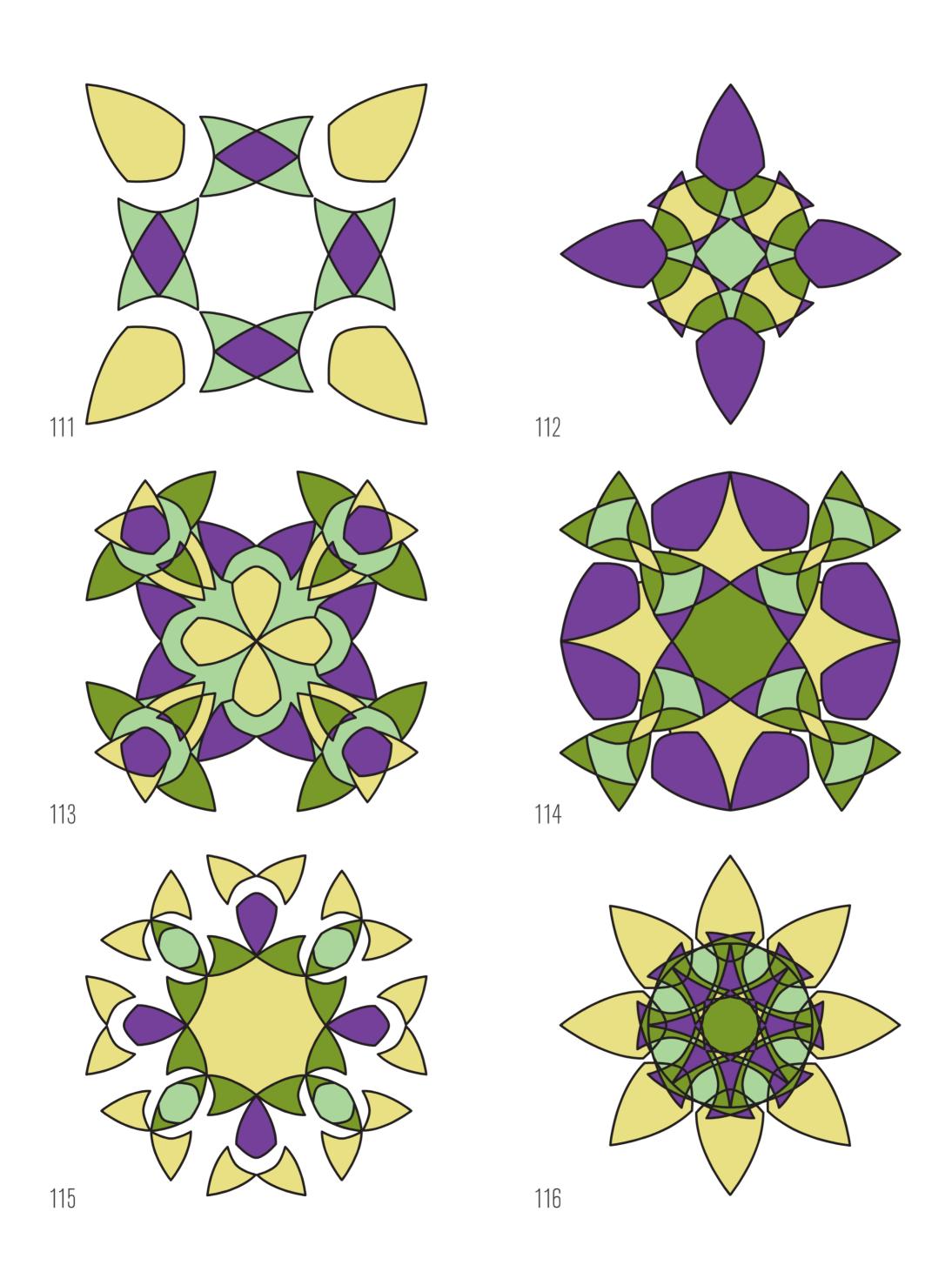
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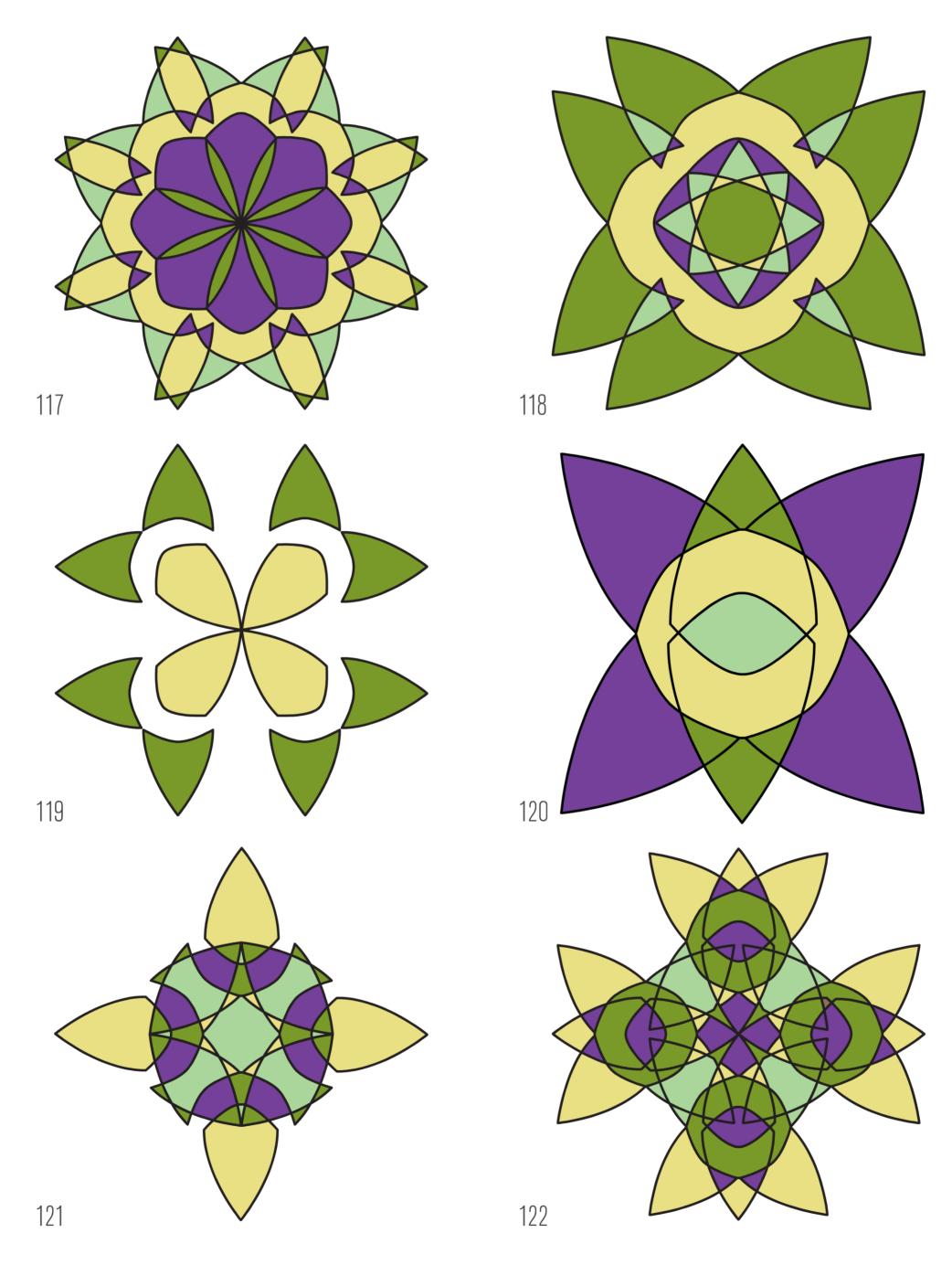


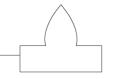




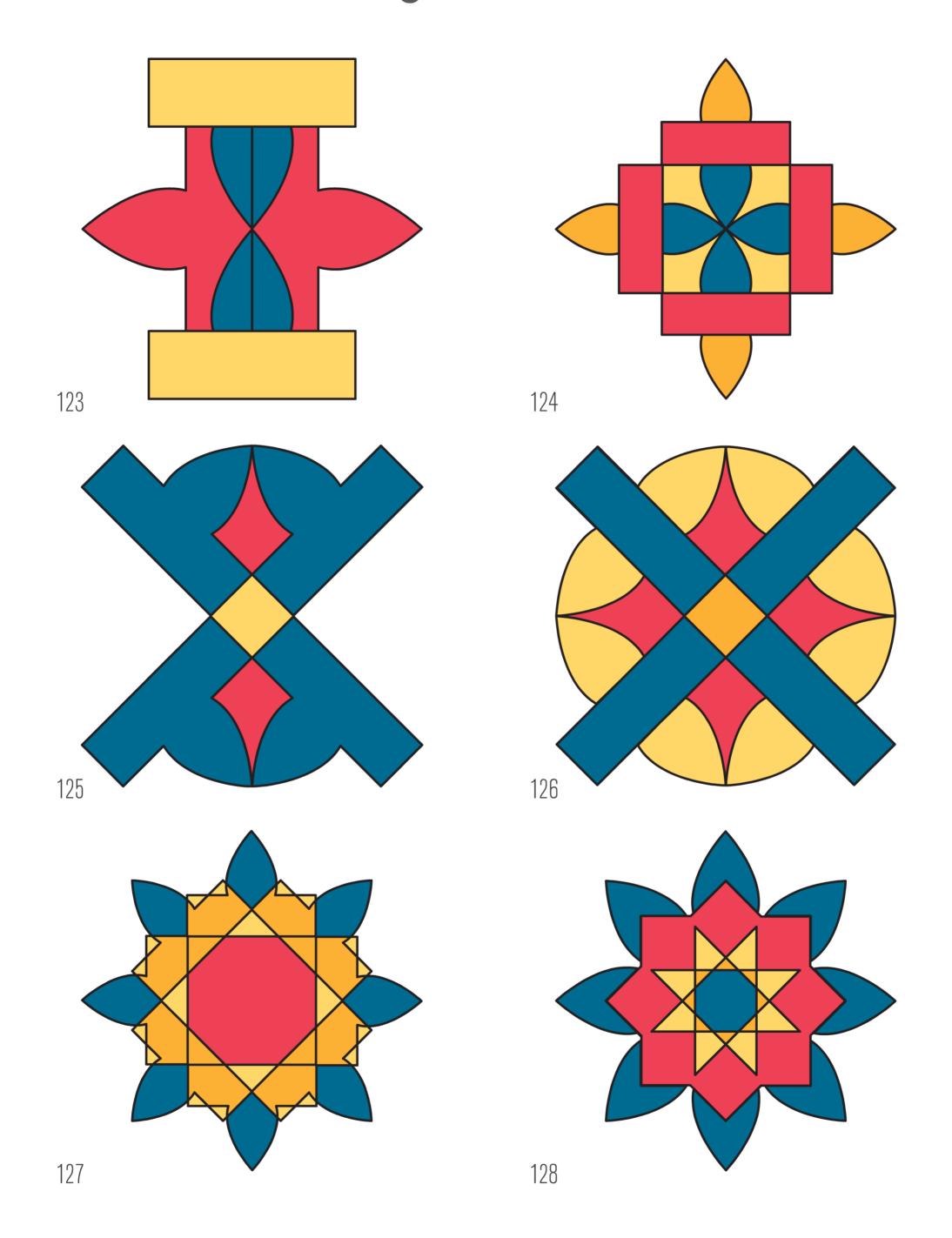


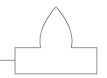




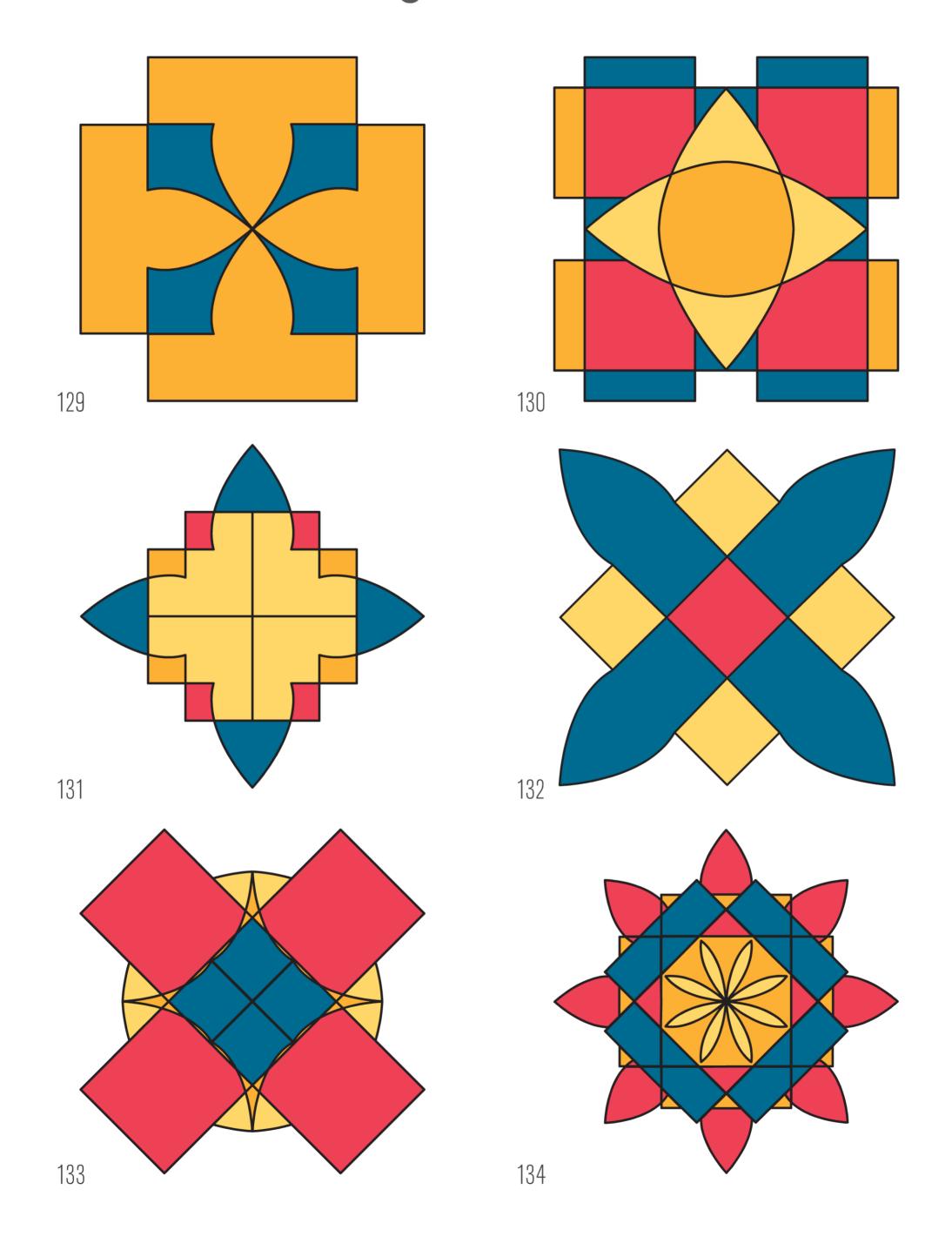


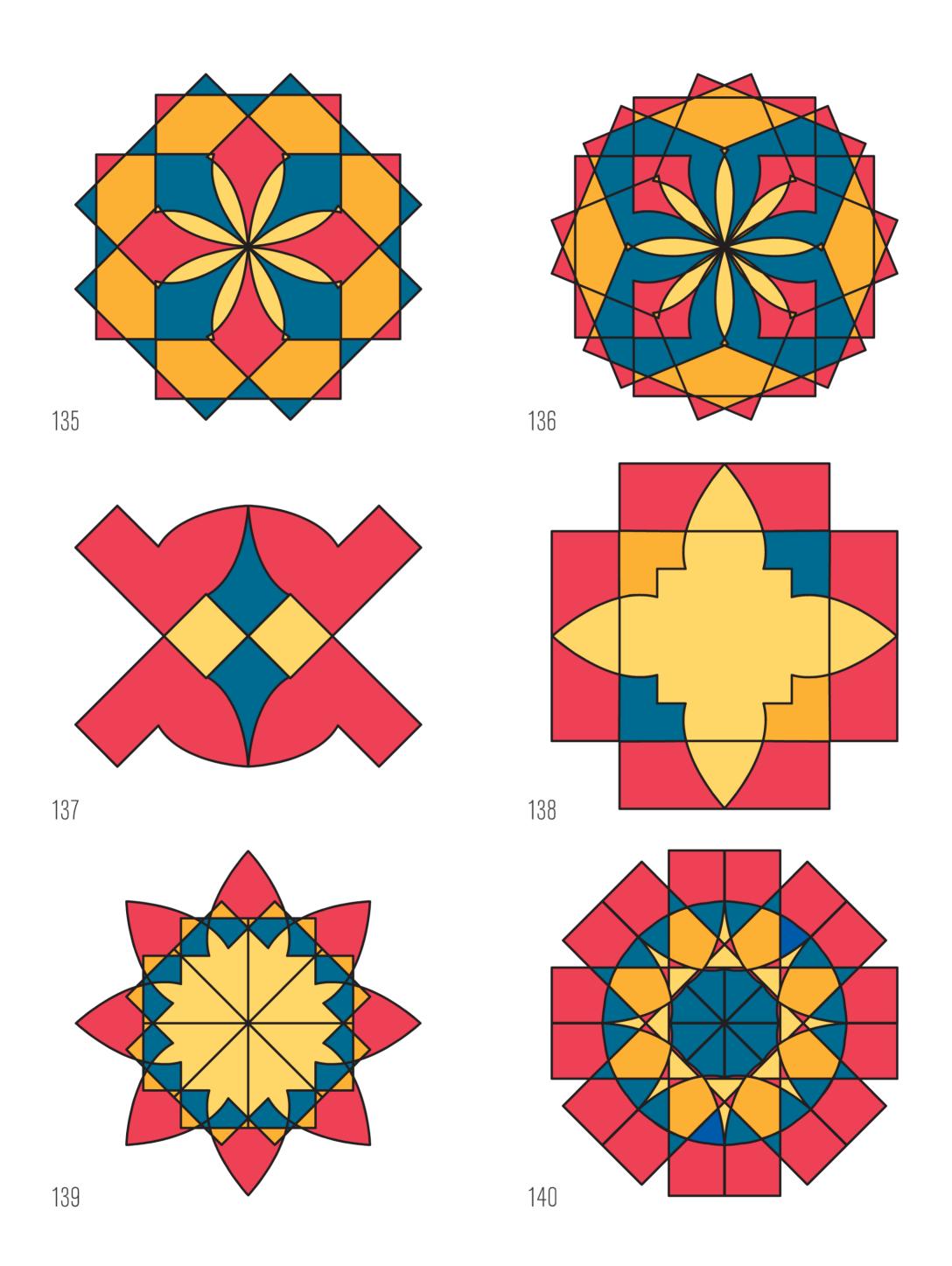
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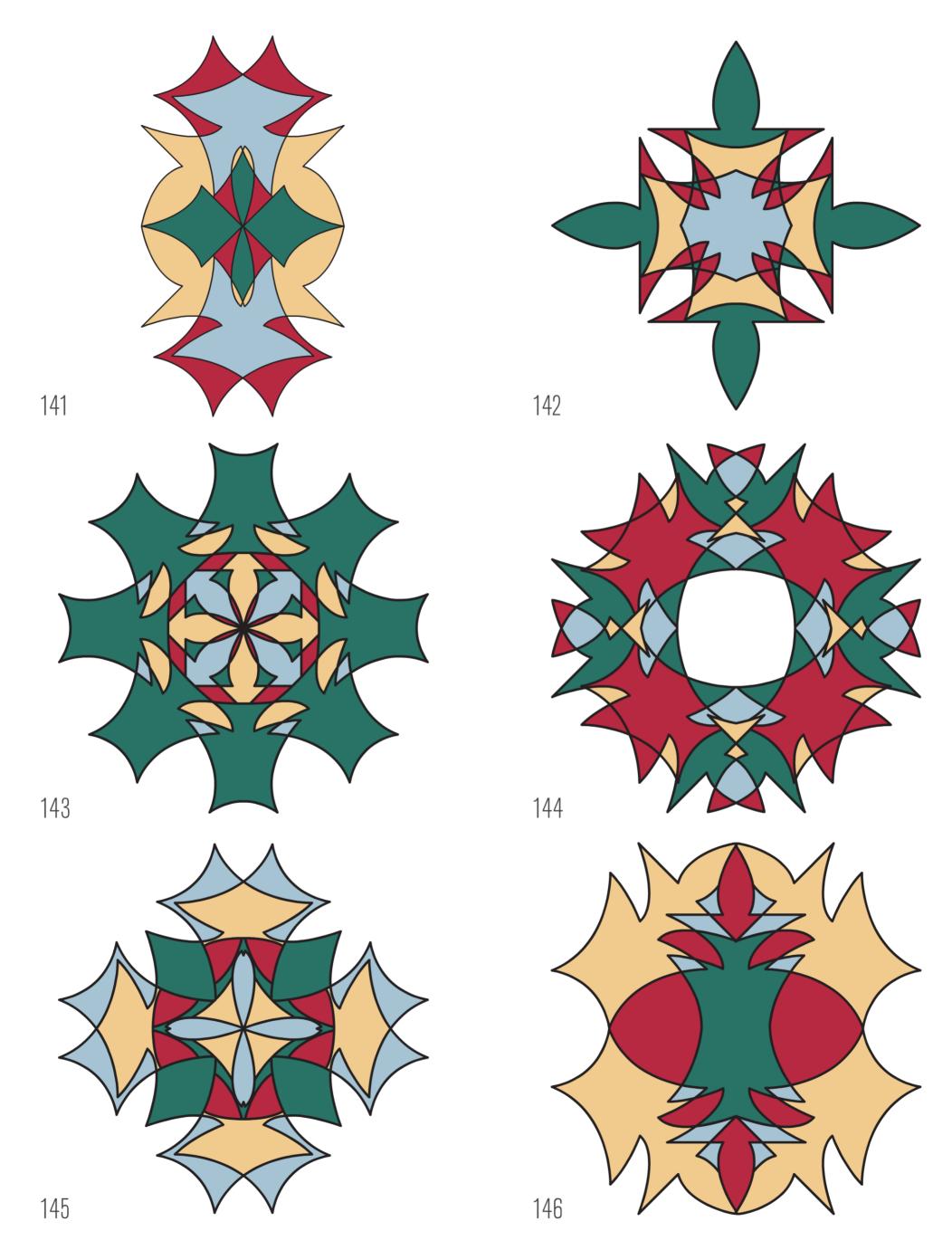
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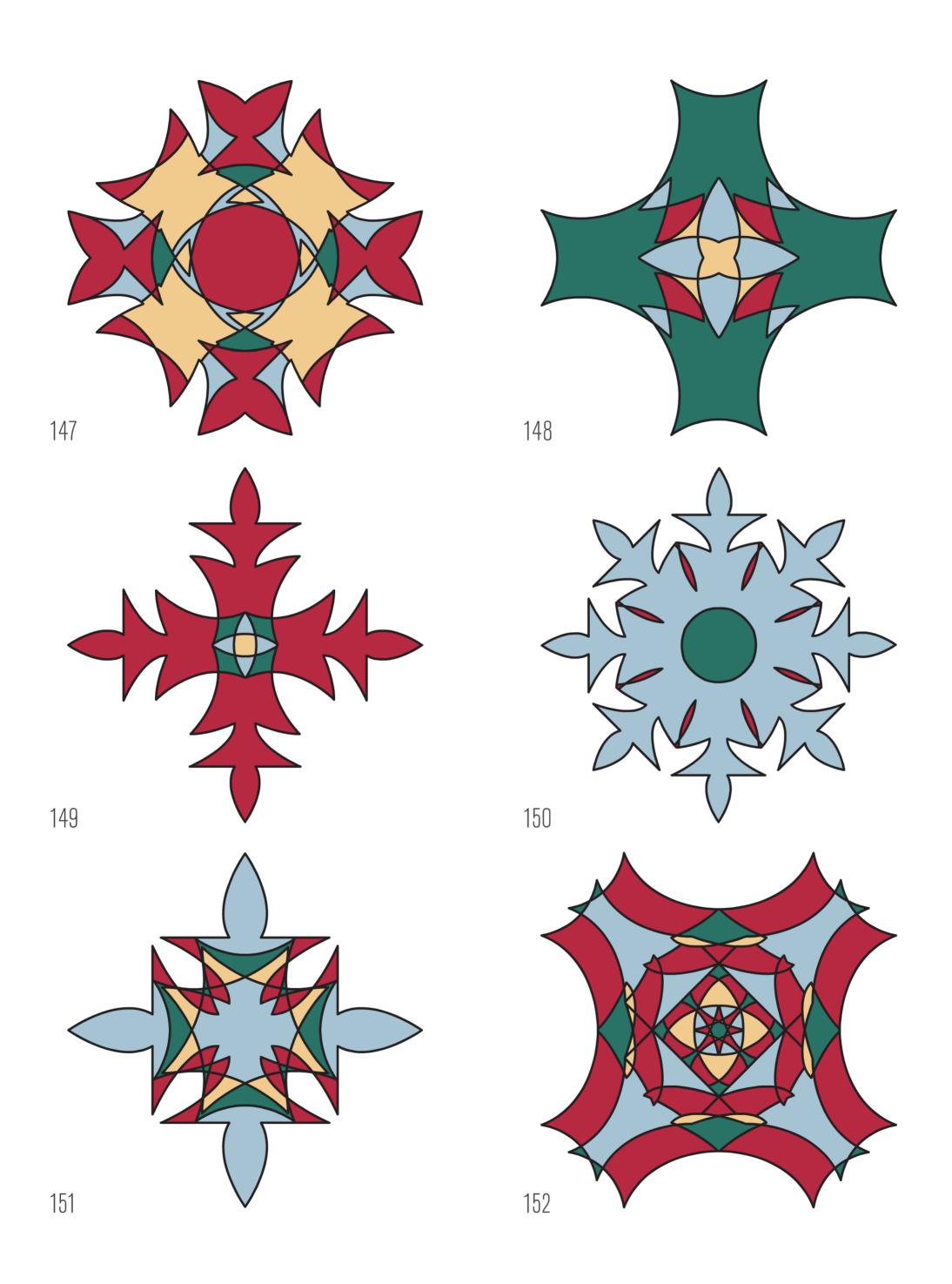






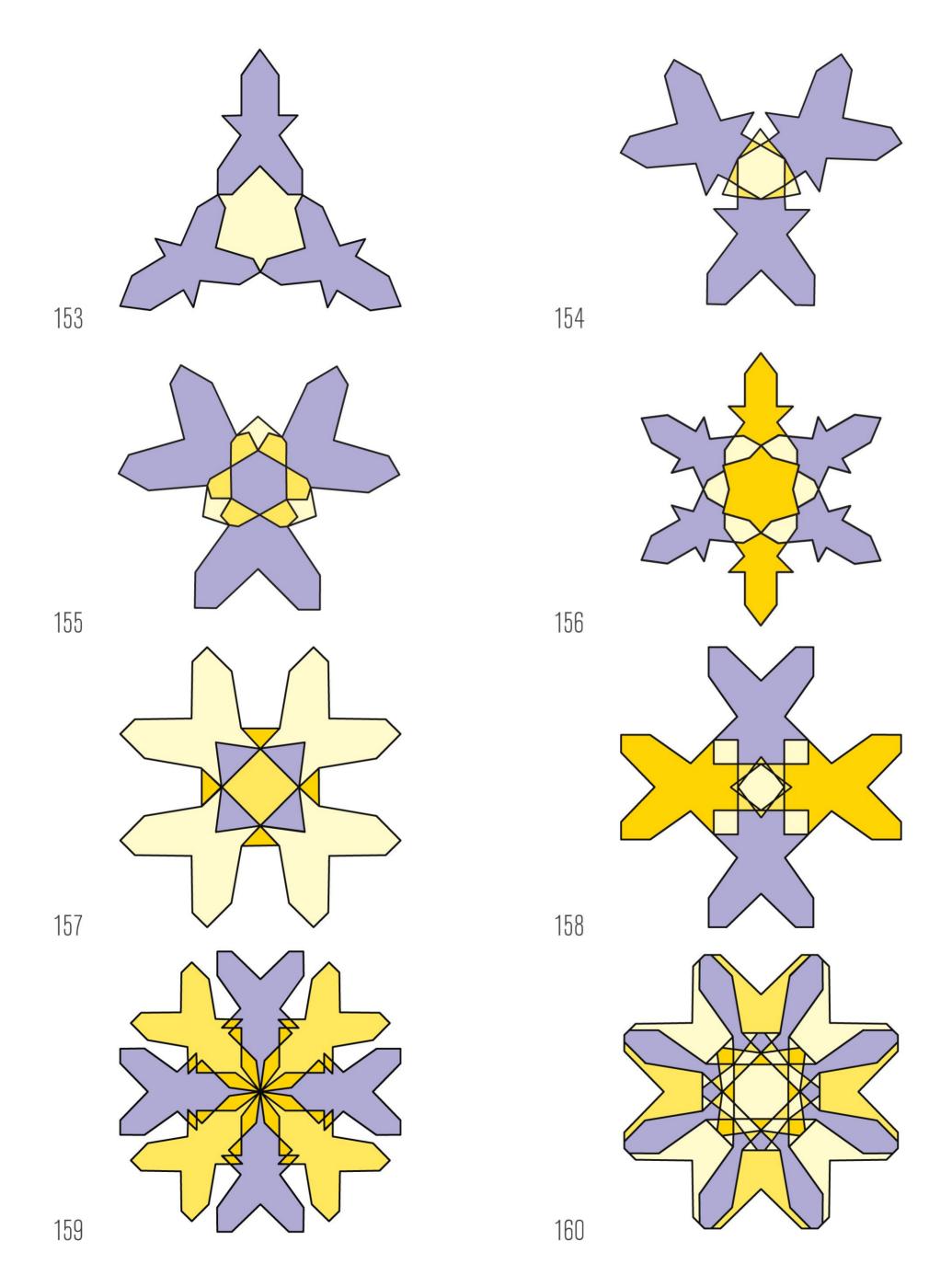
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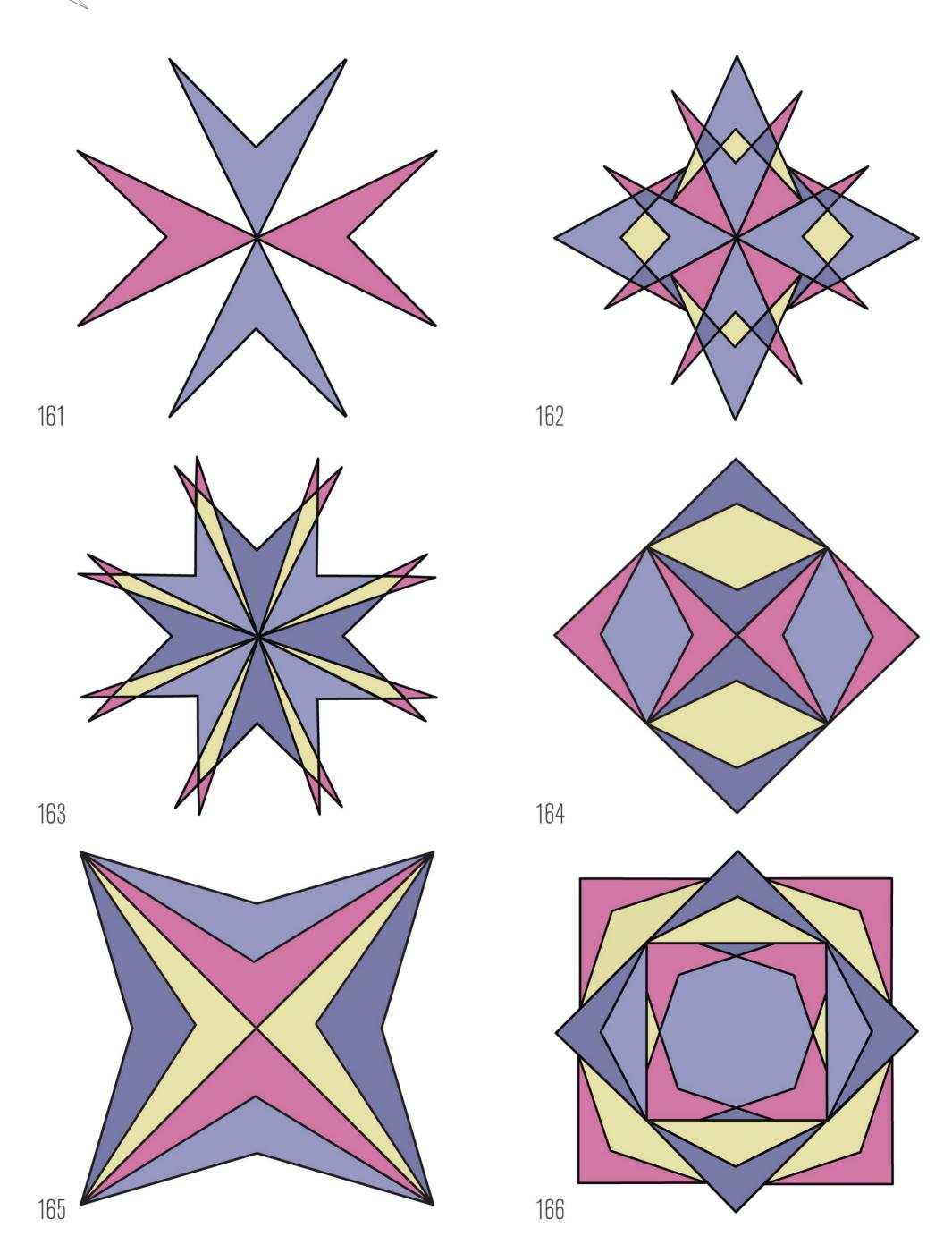




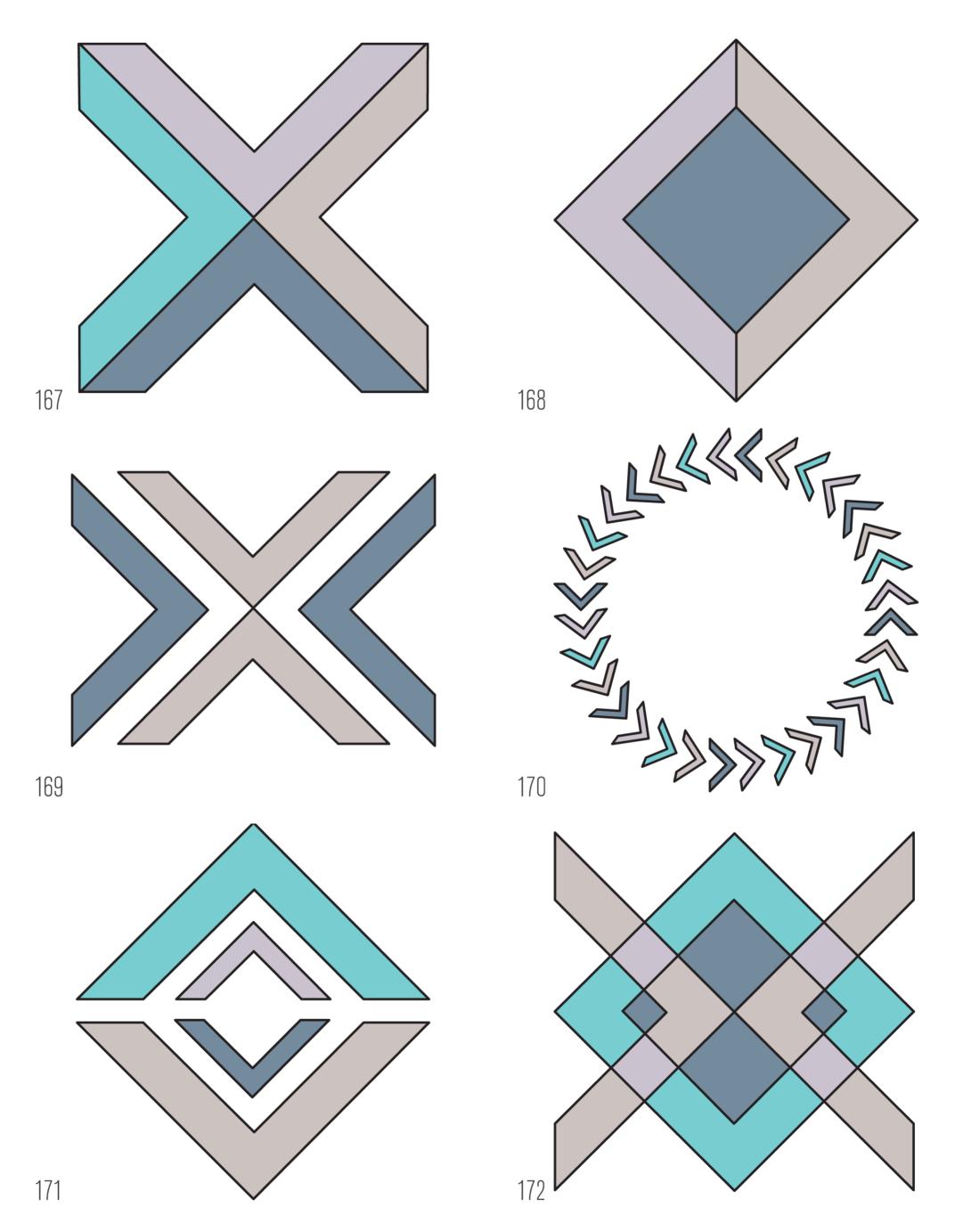
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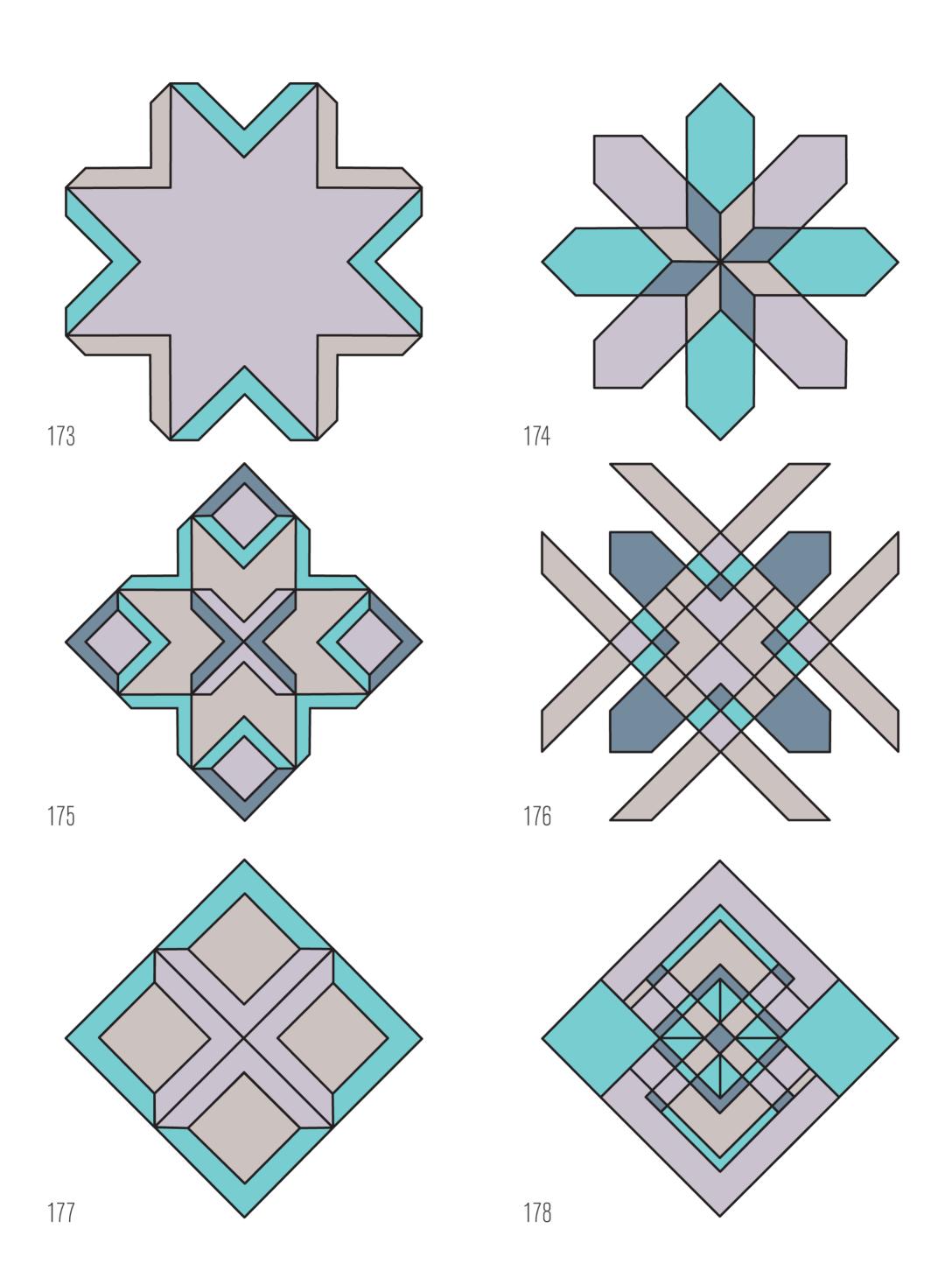


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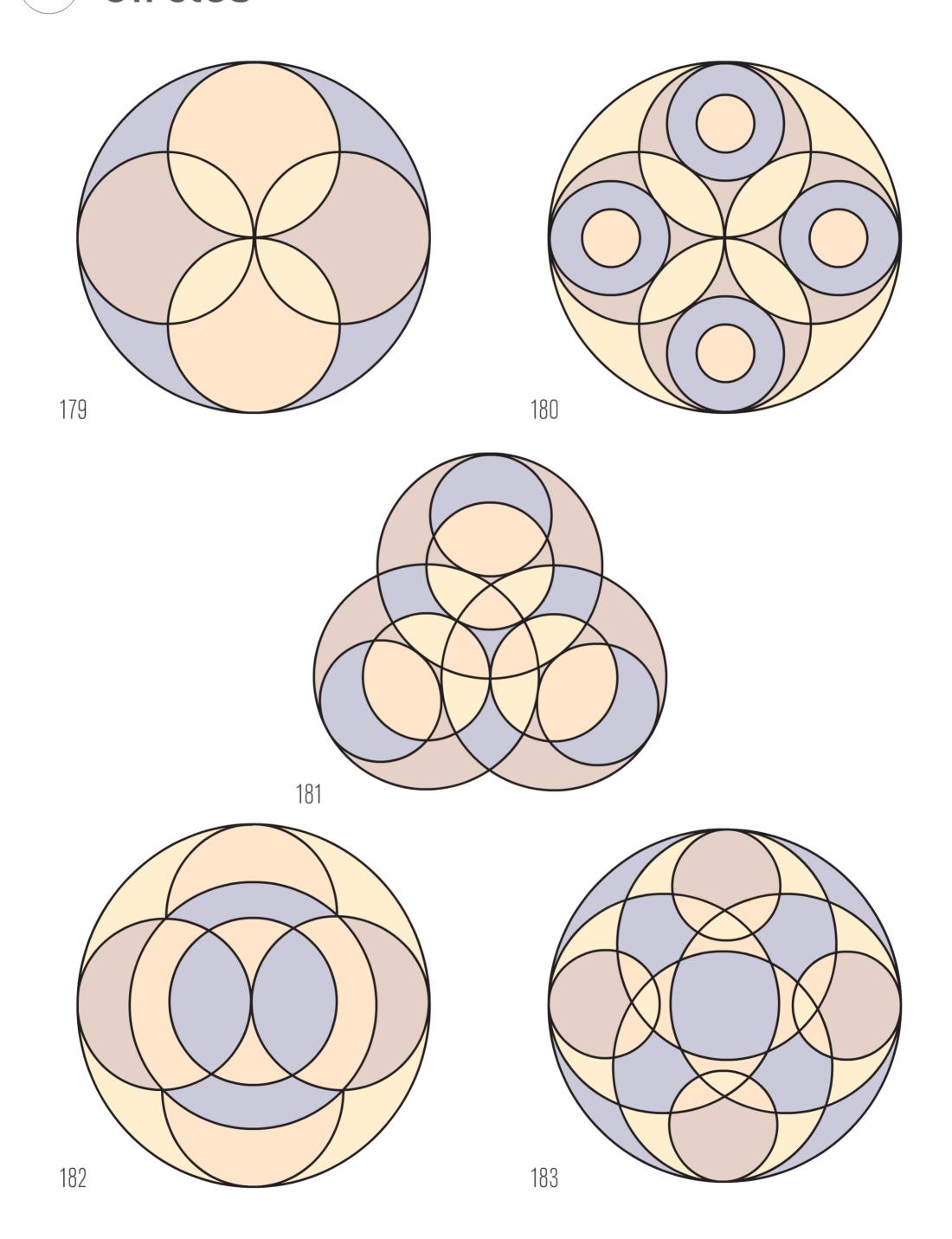


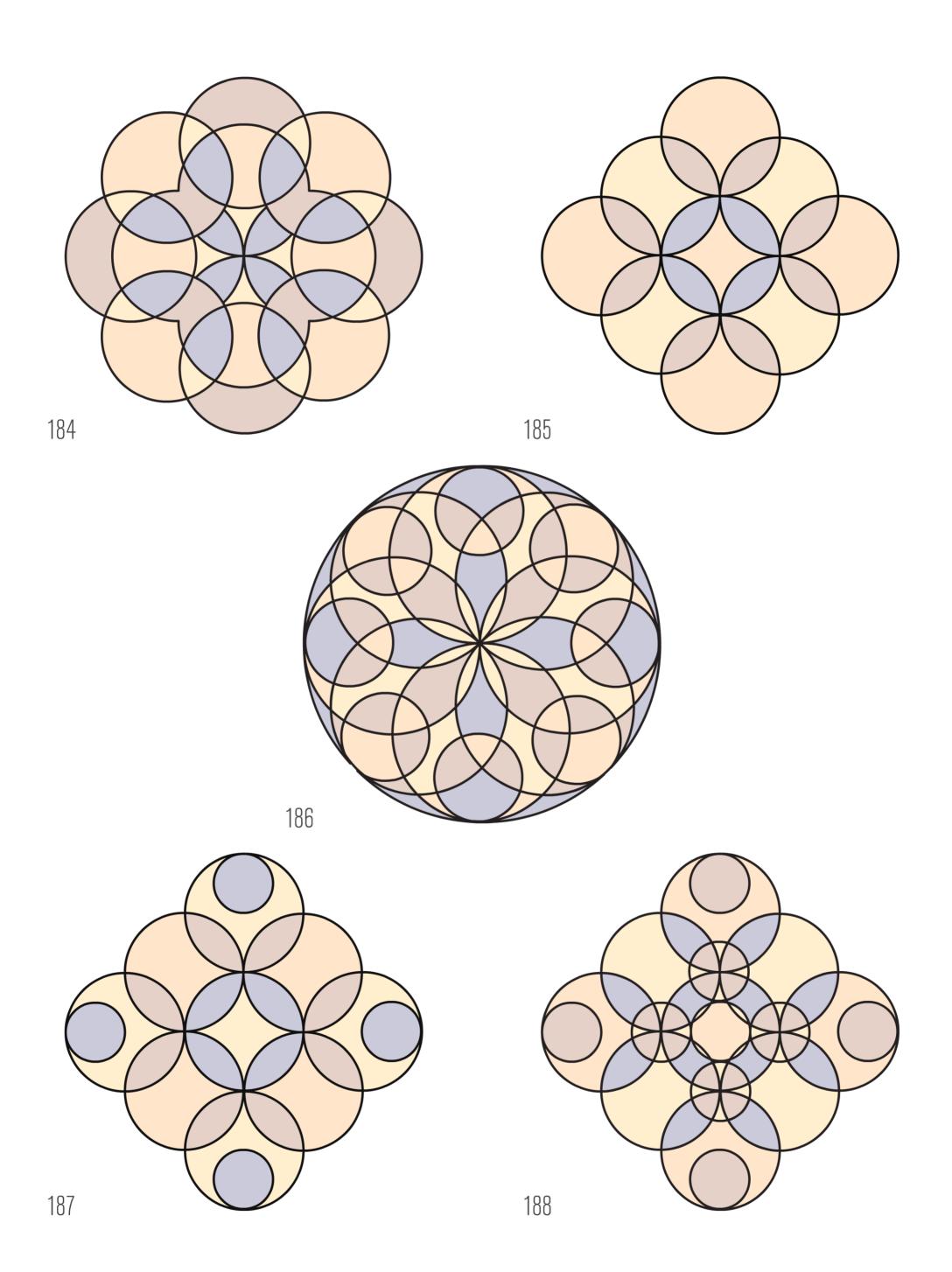
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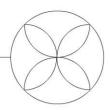




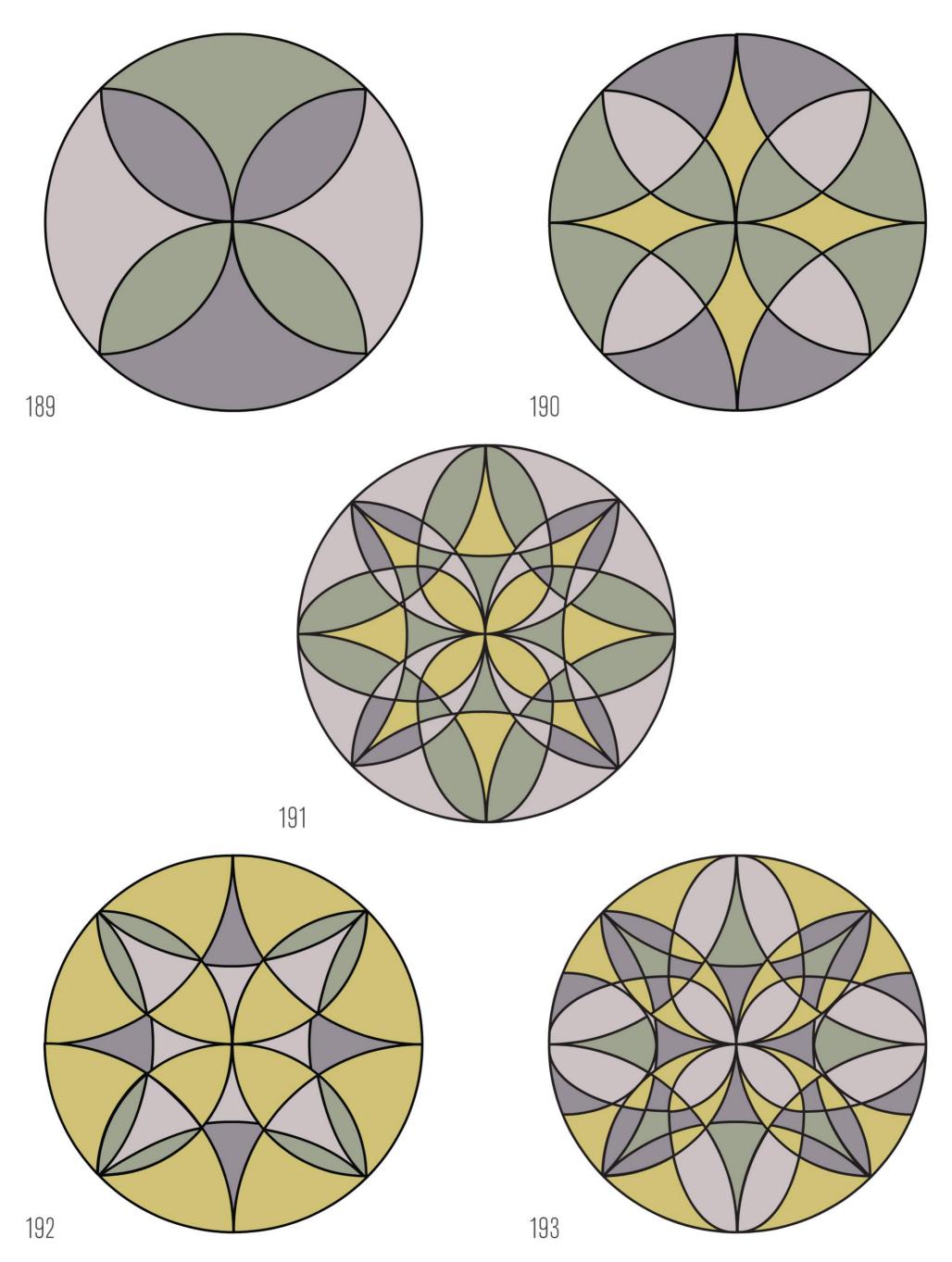
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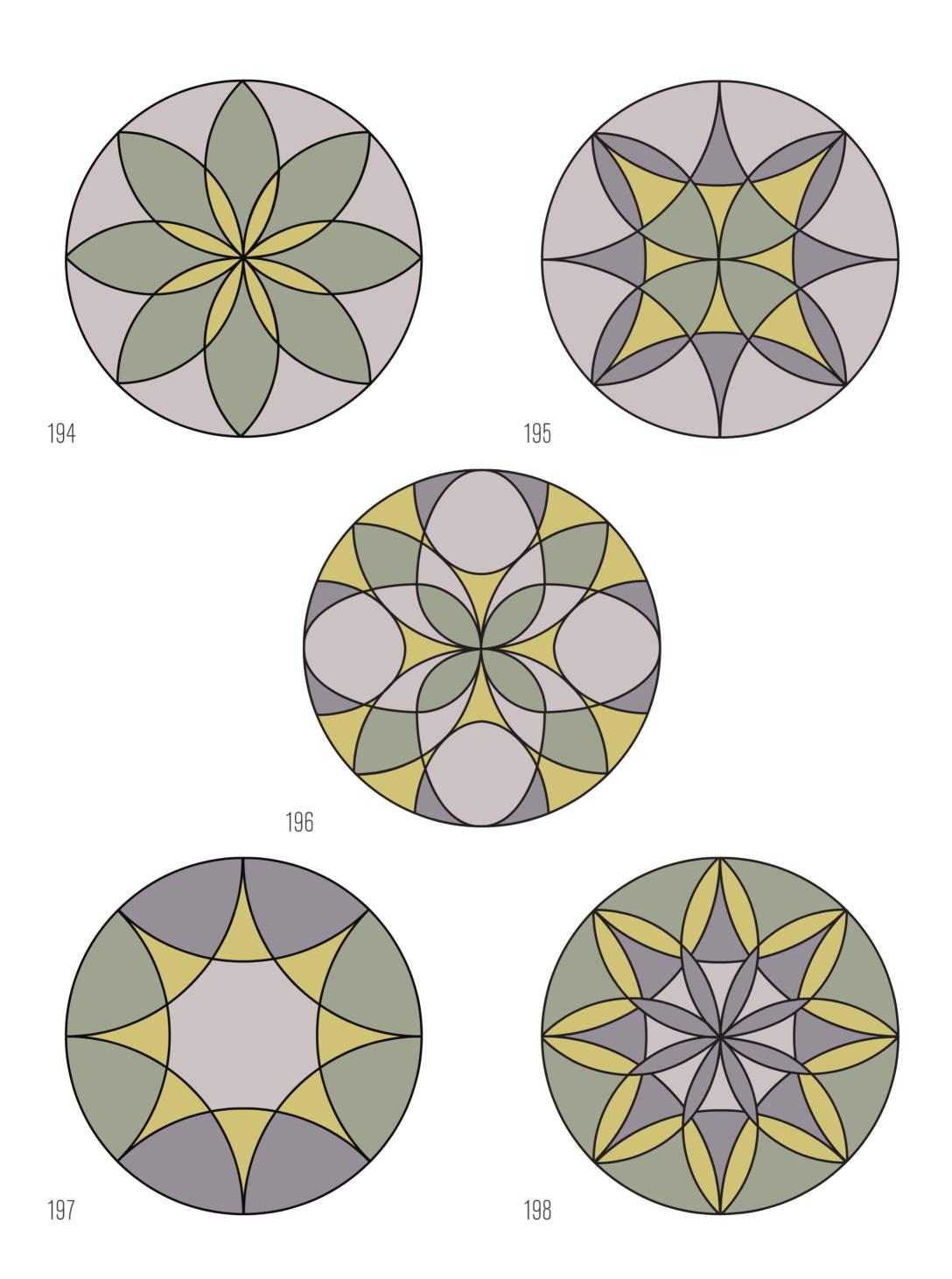




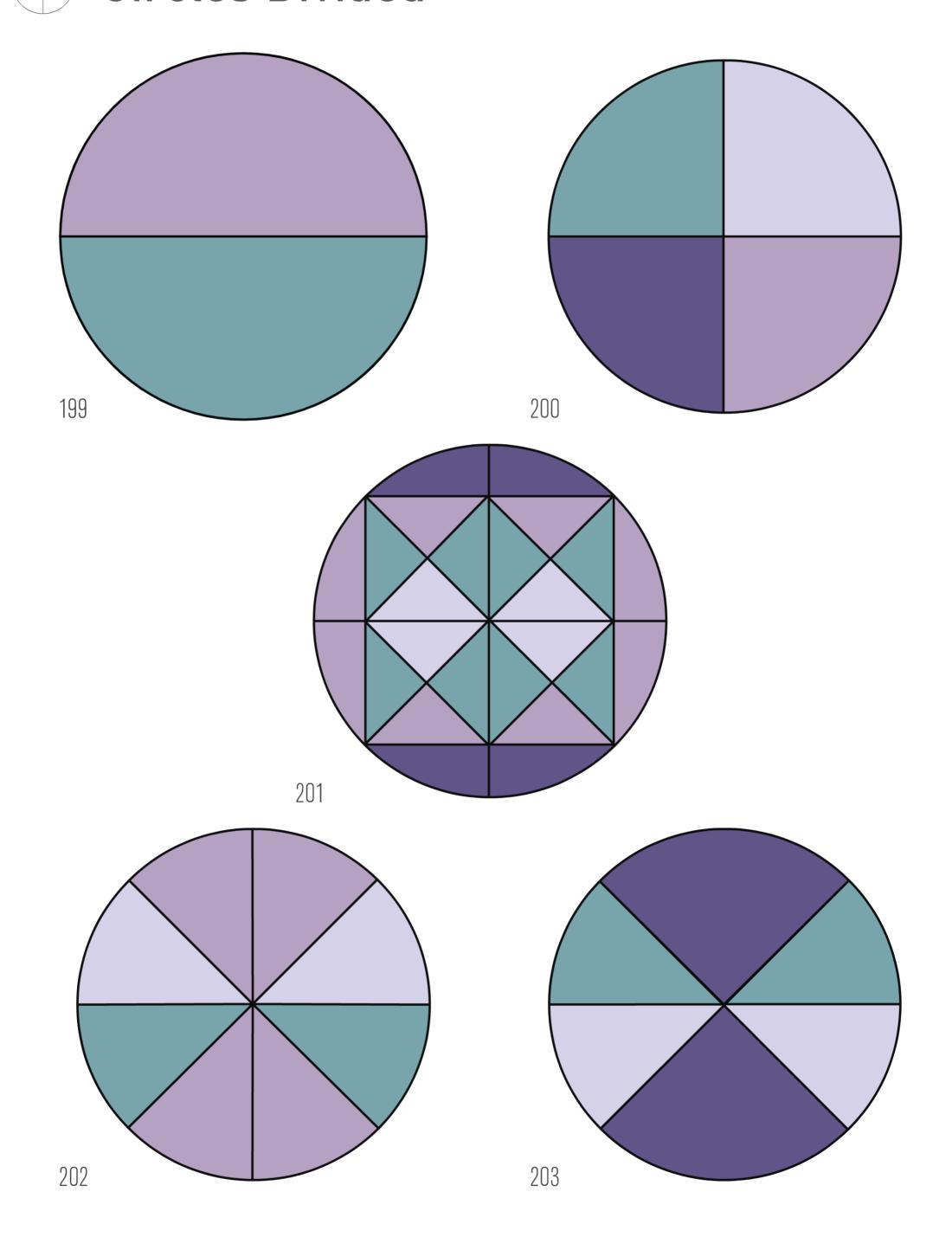


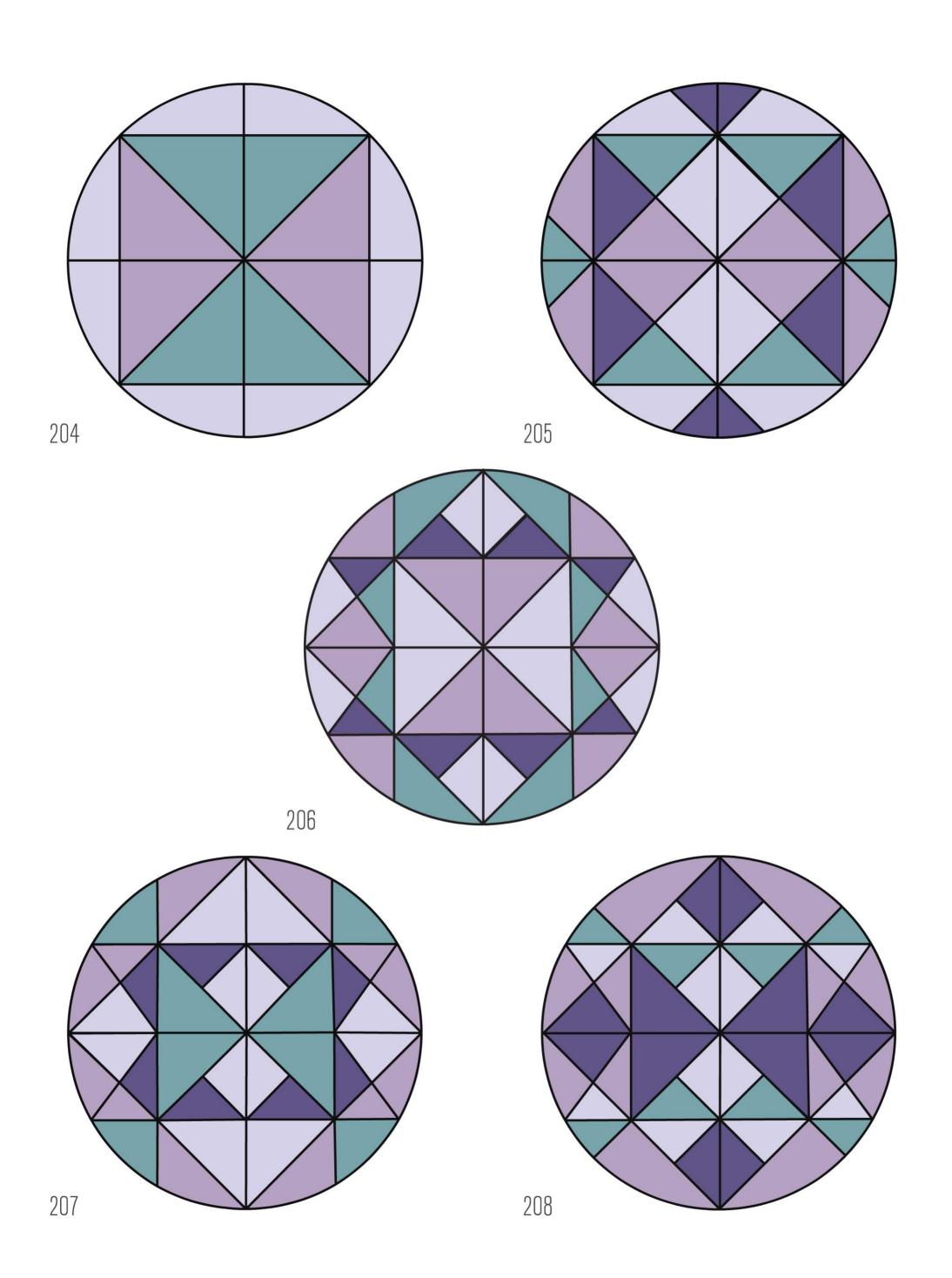
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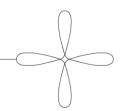




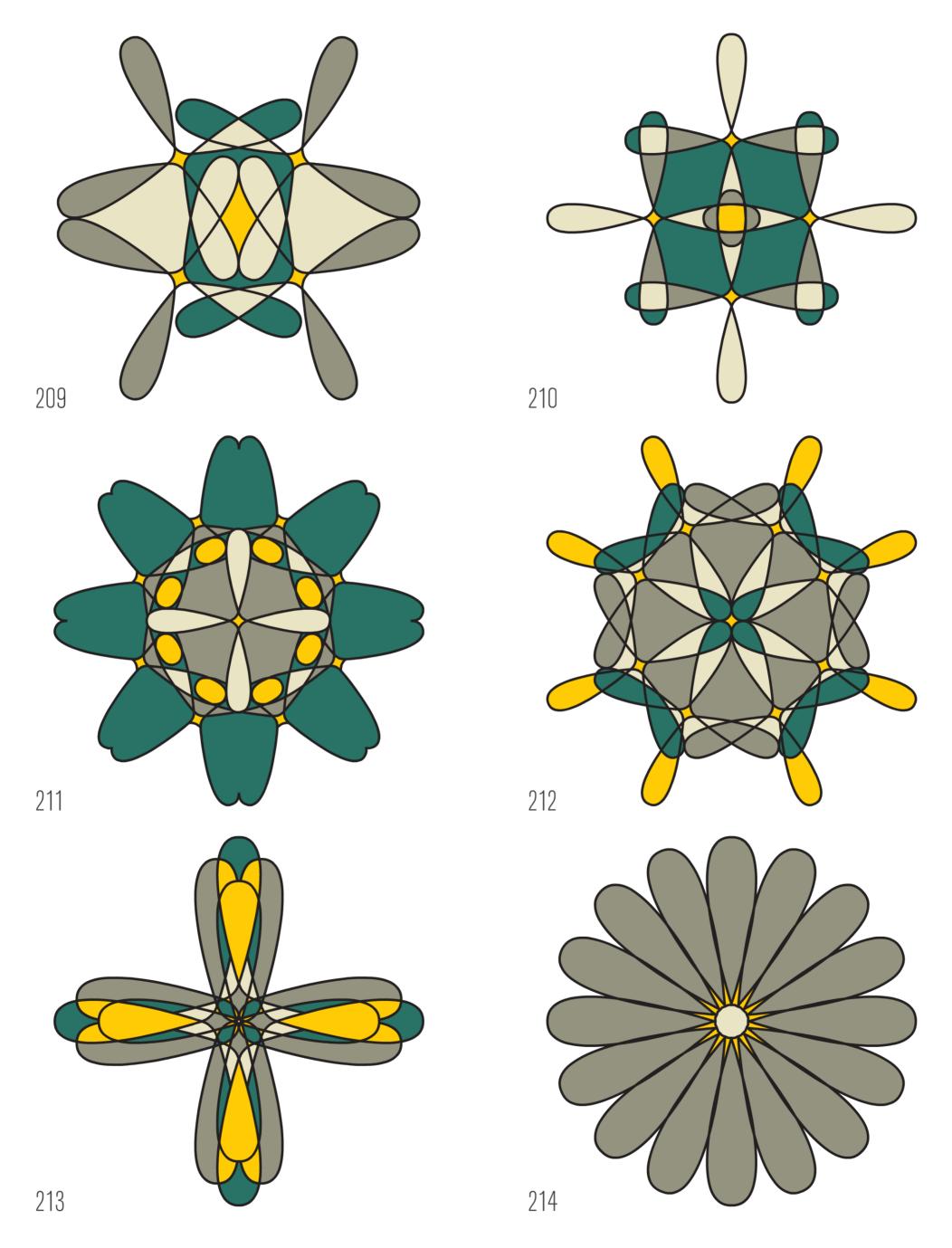
Circles Divided





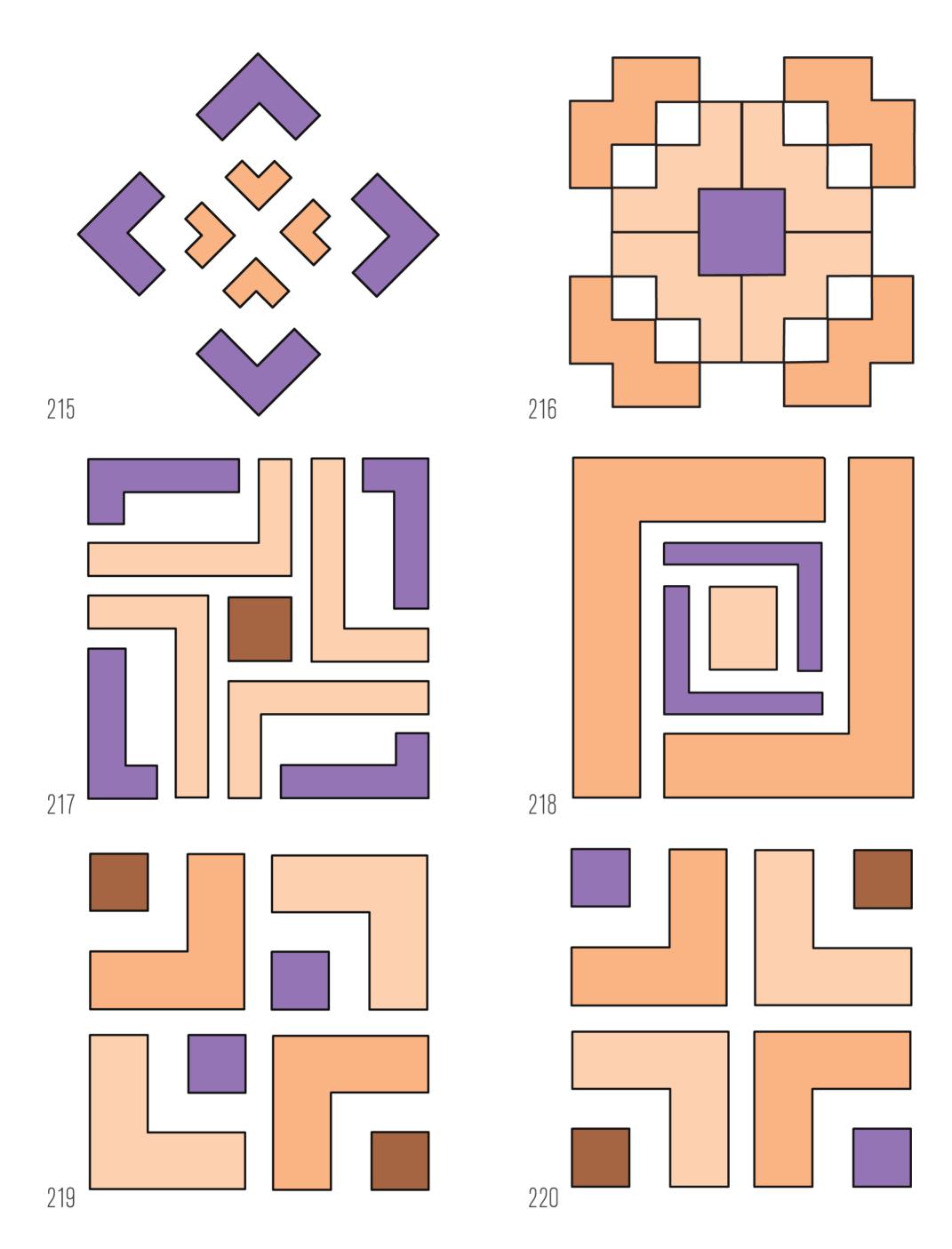


Clover Loop

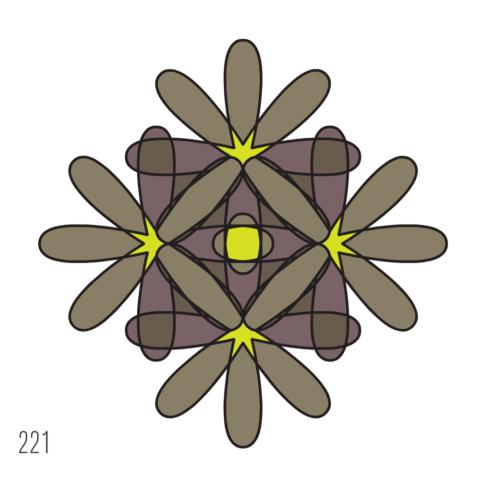


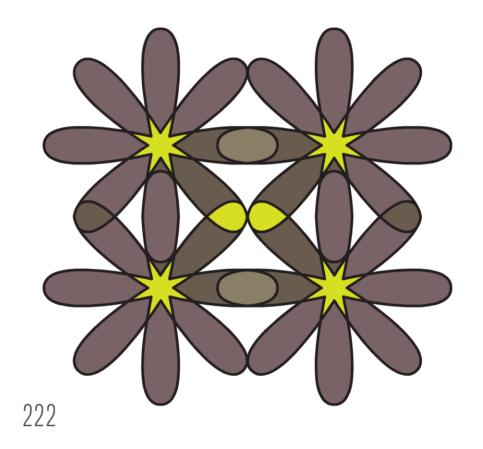


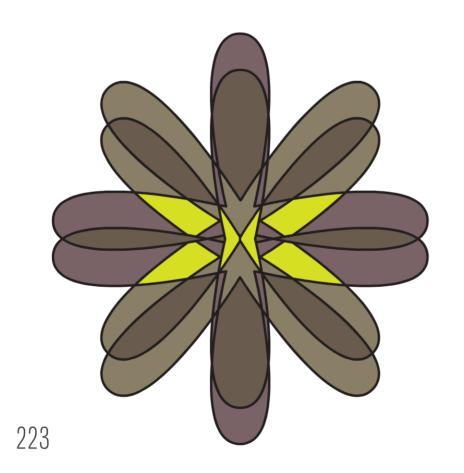
Corners

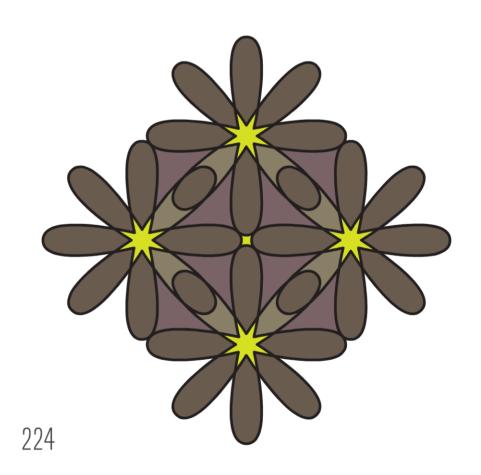


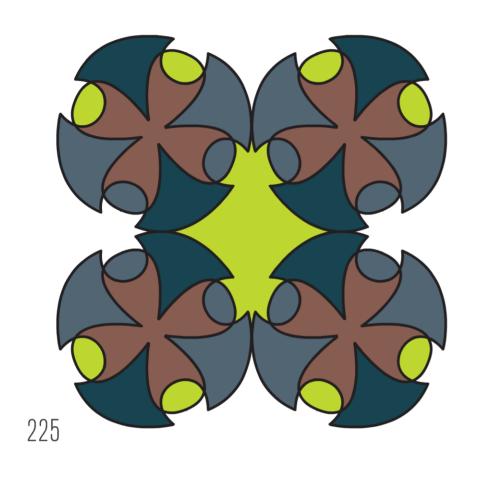


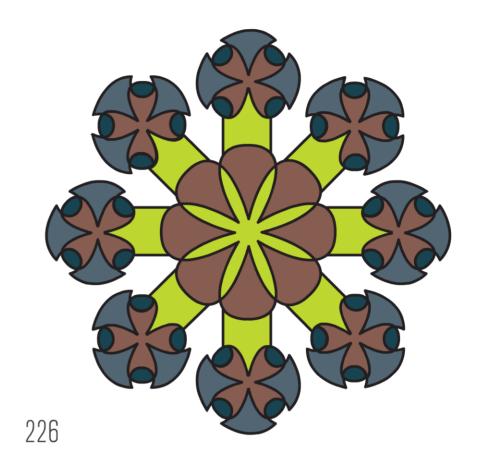


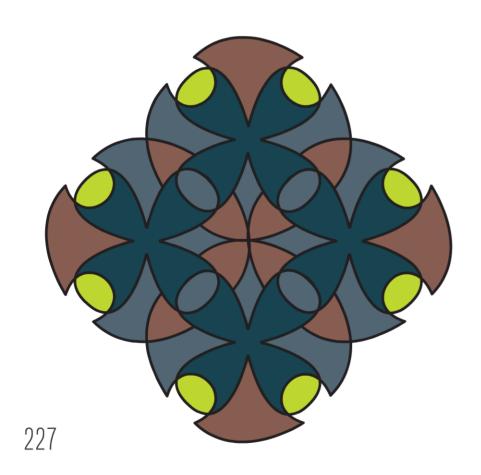


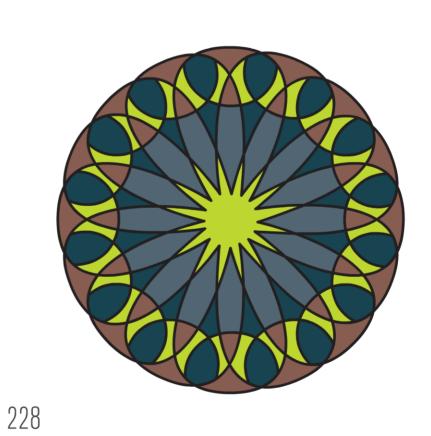




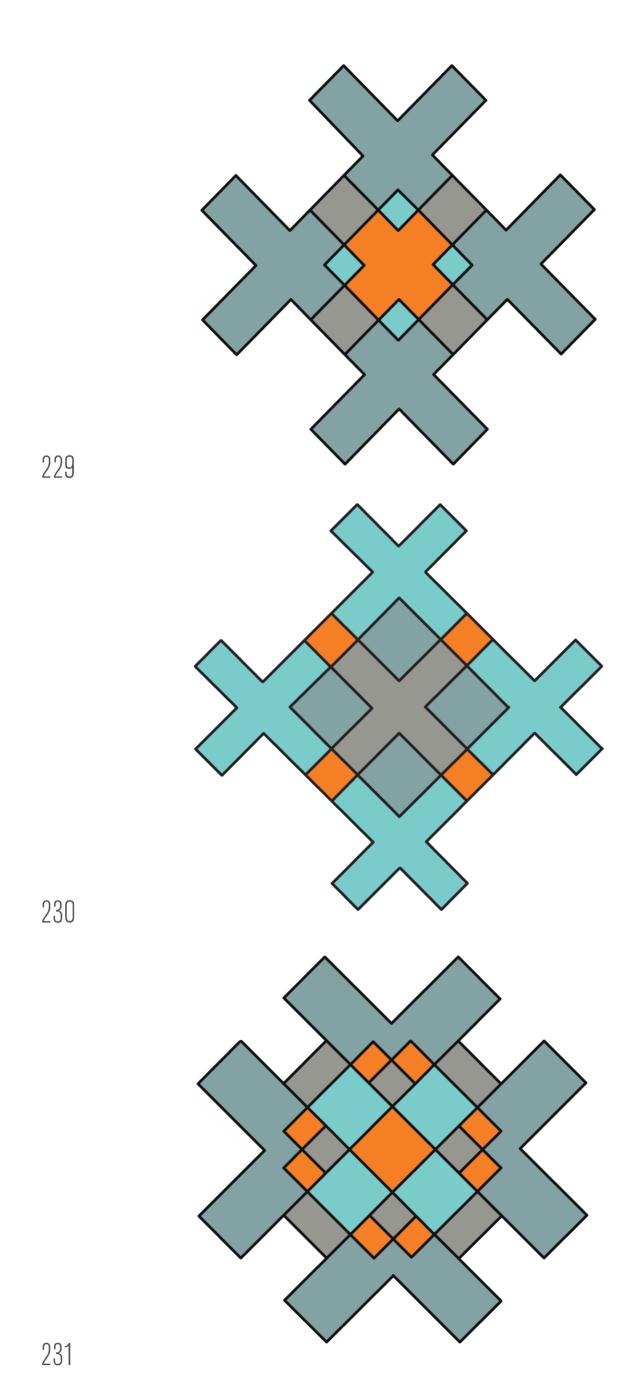


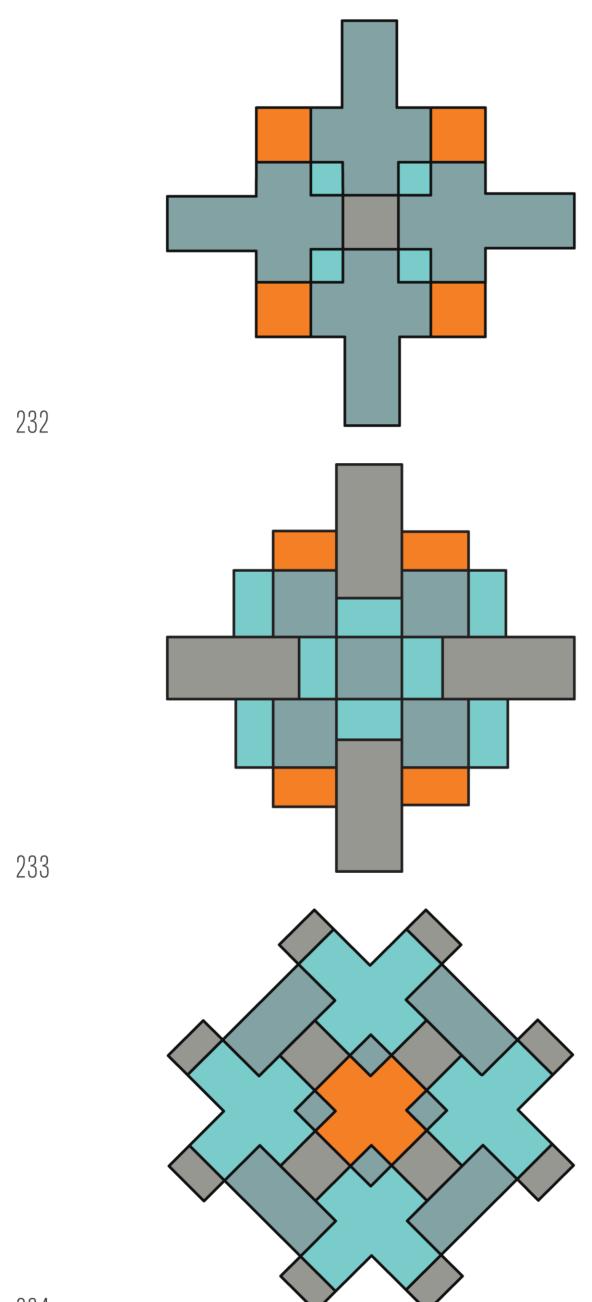




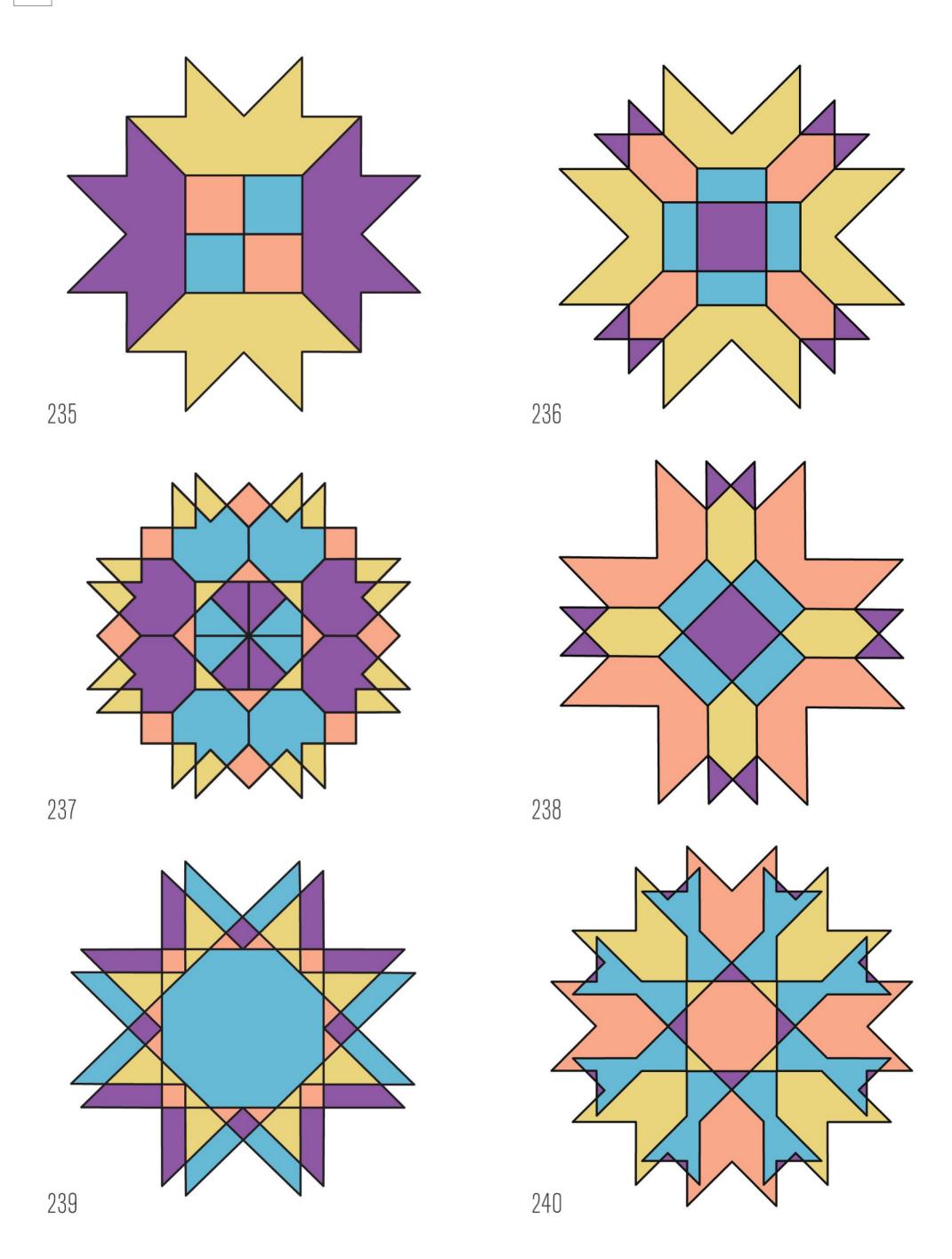


- Crosses

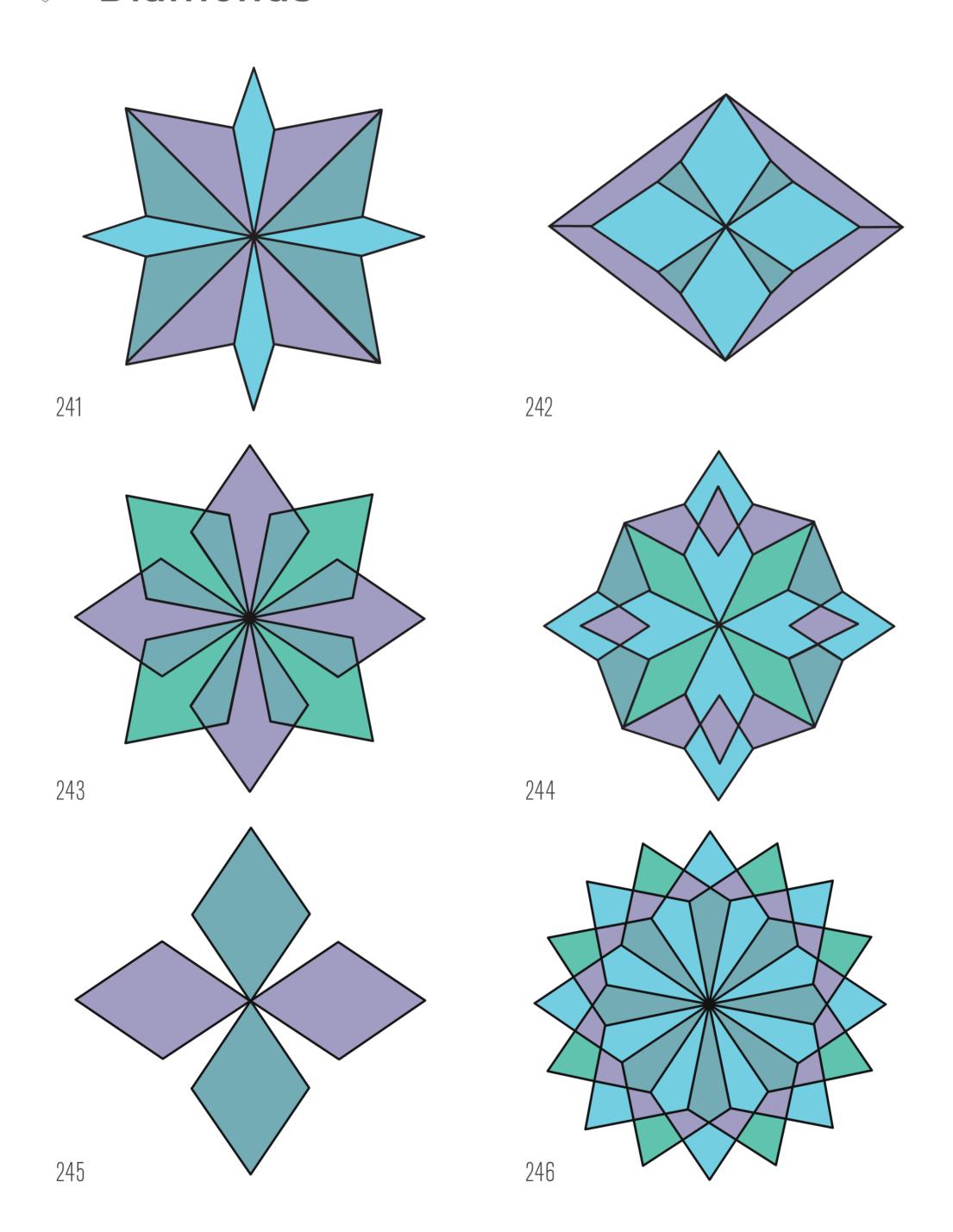




Crowns

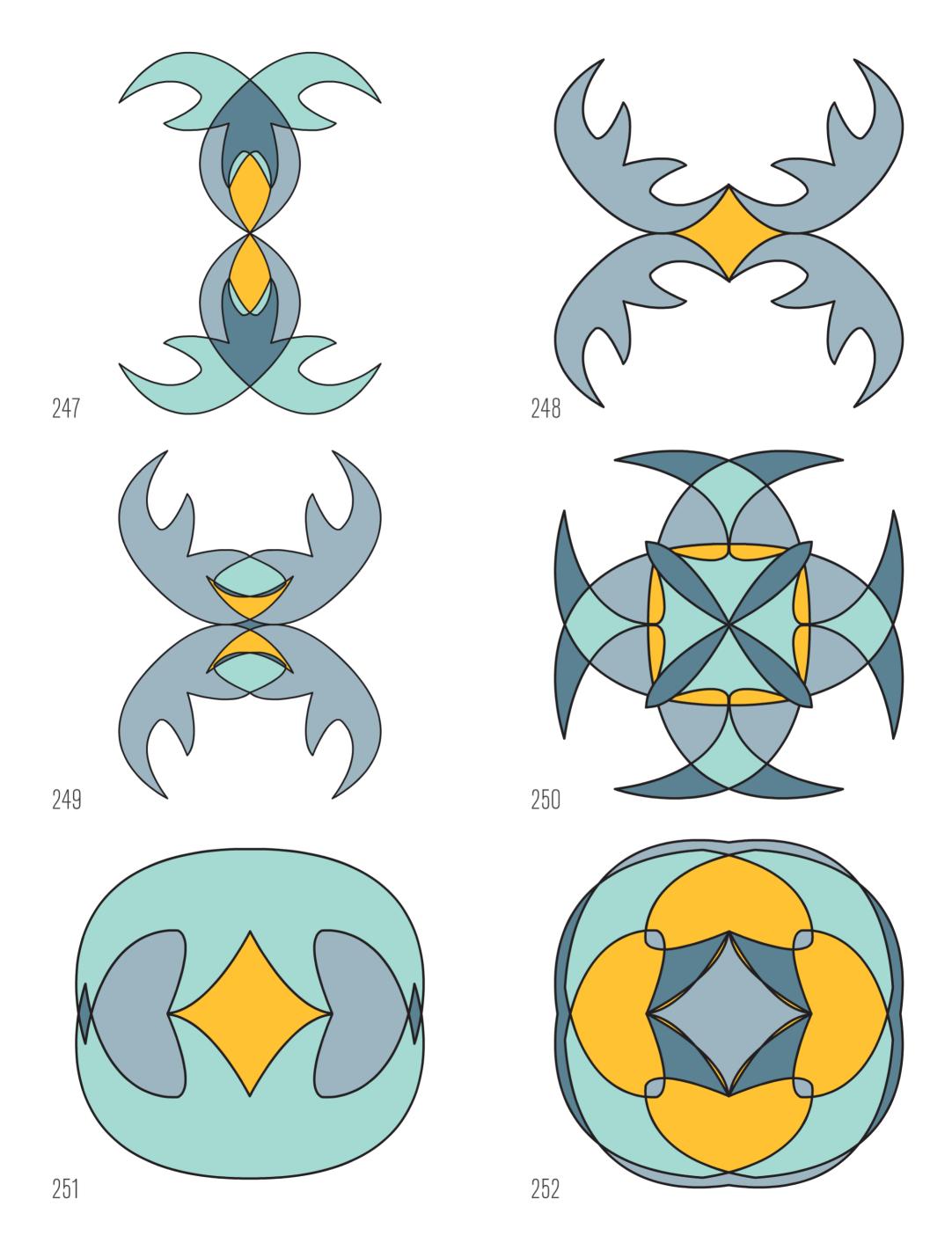


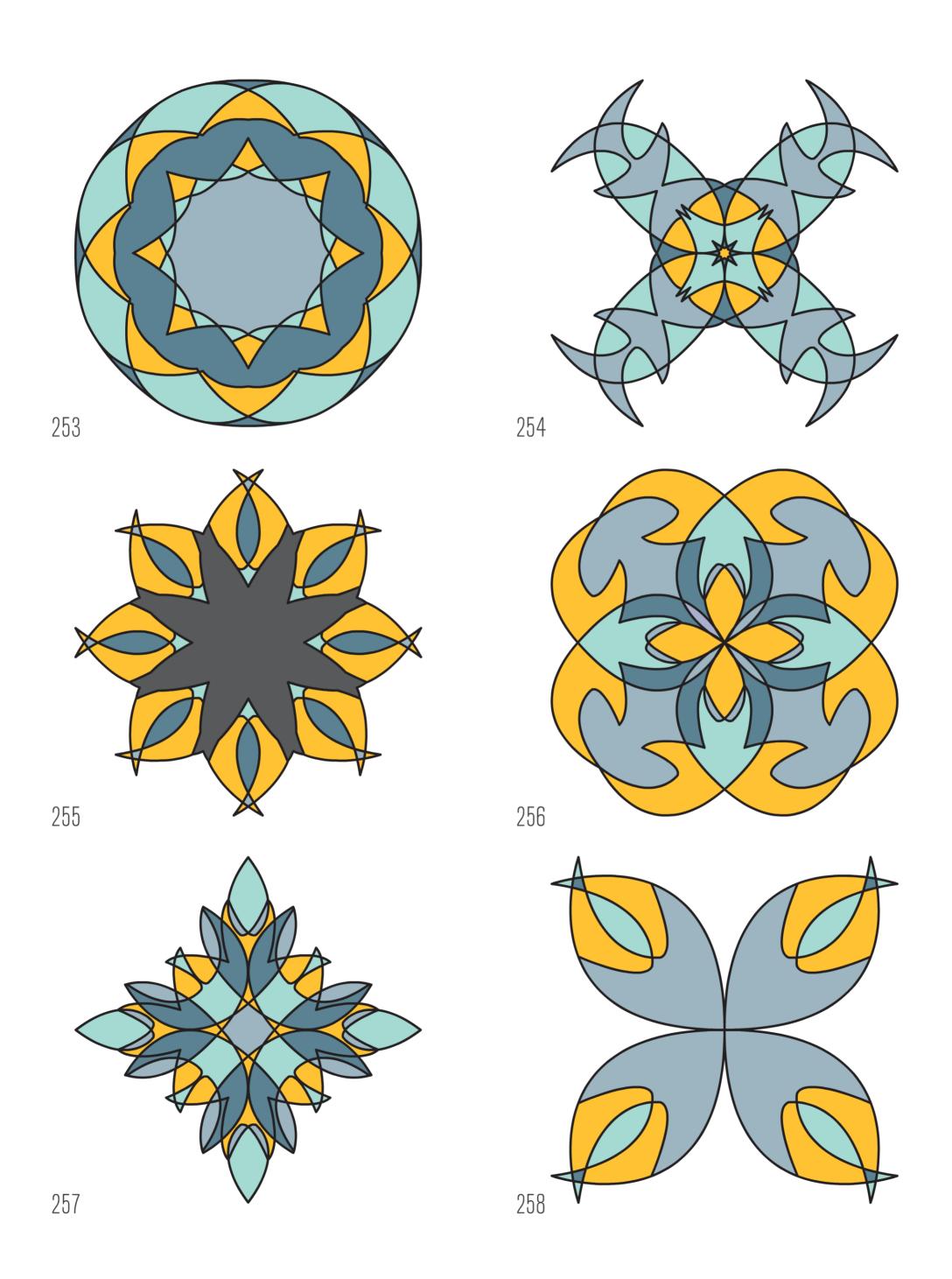
Diamonds





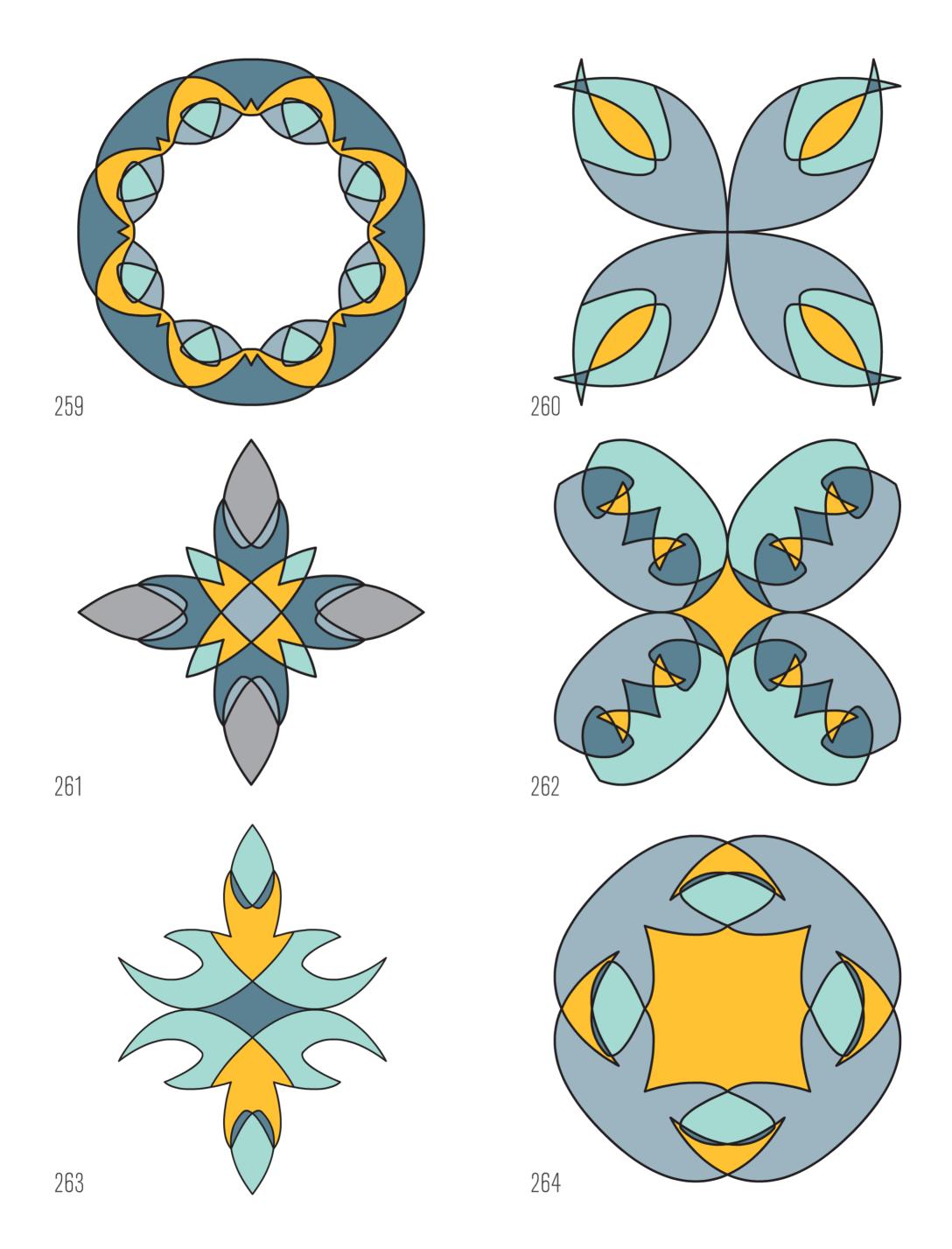
Double Horn



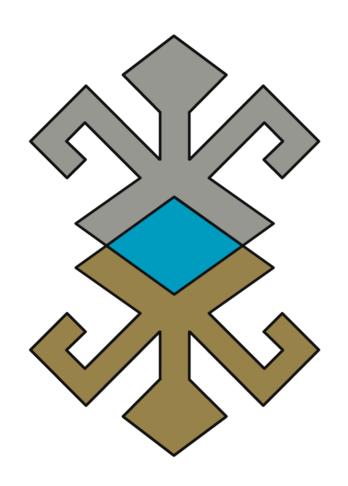


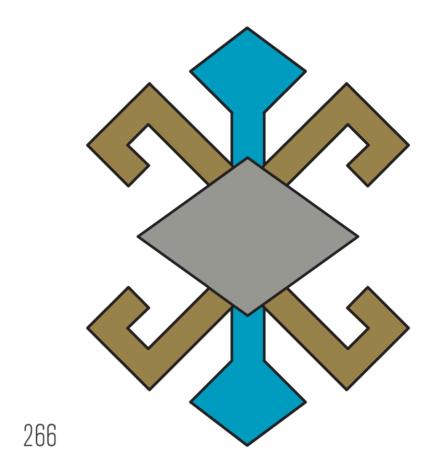


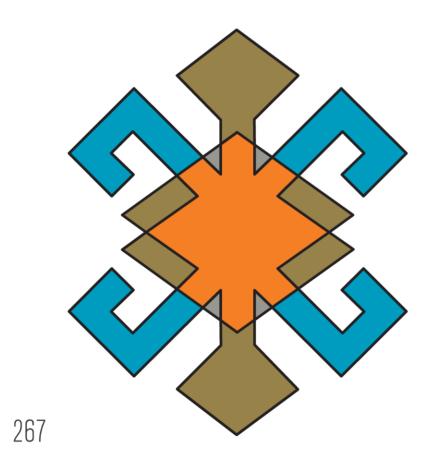
Double Horn

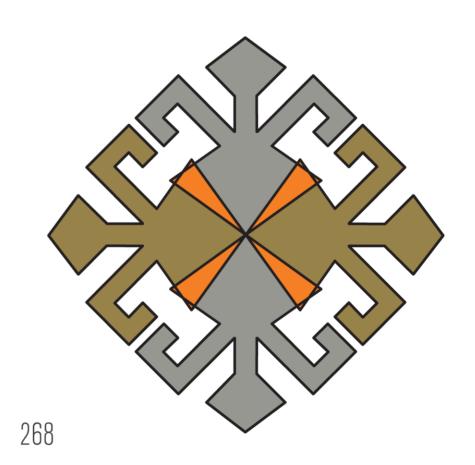


Down at Arms

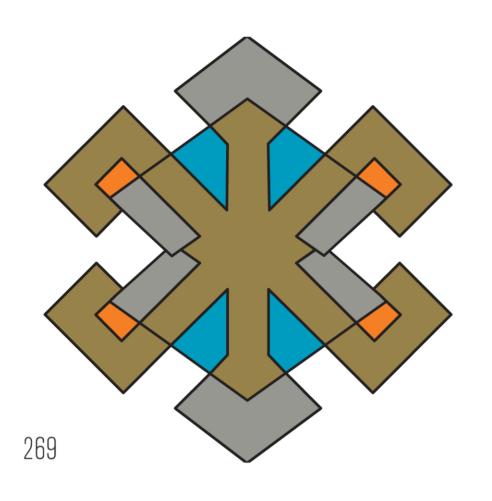


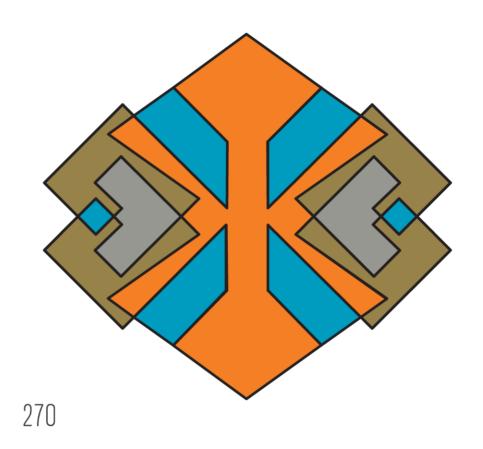


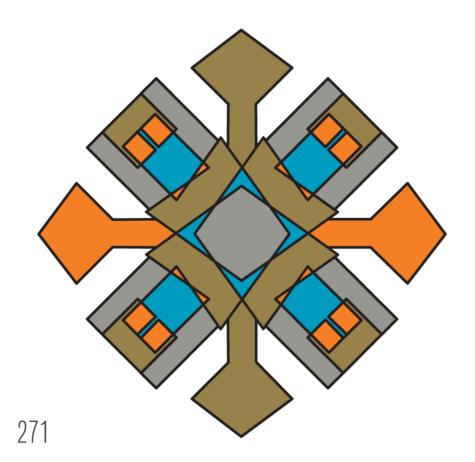


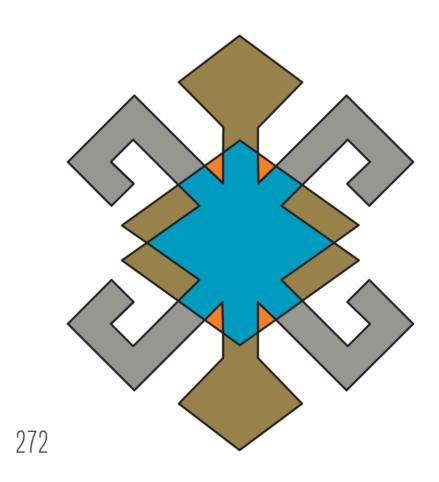


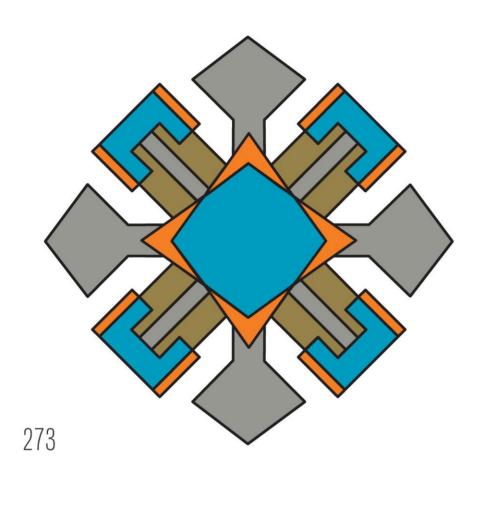
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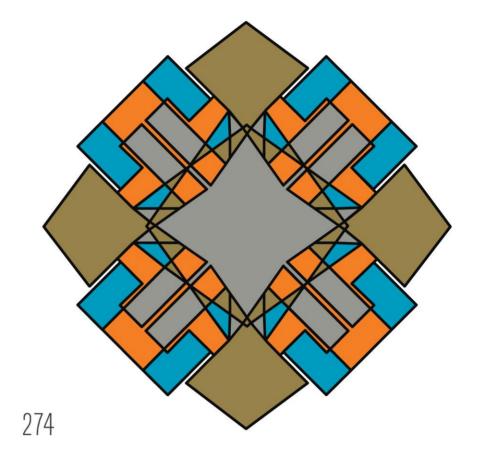


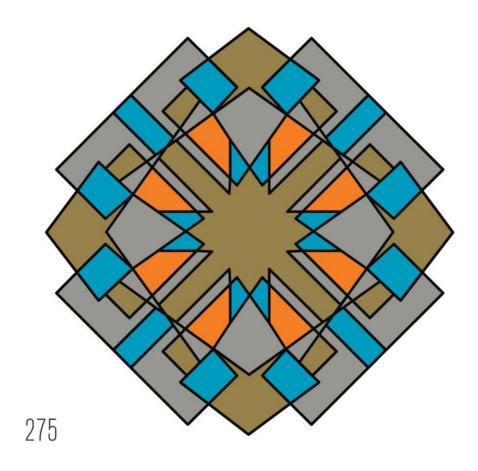


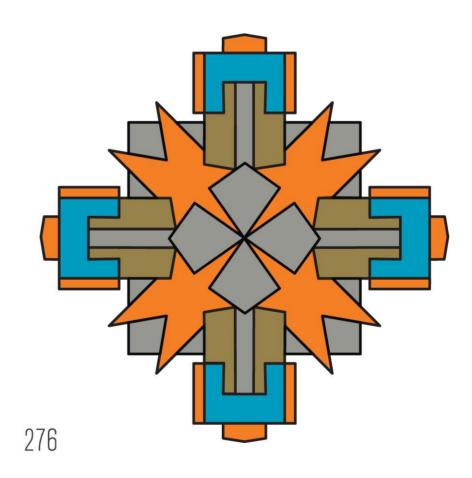




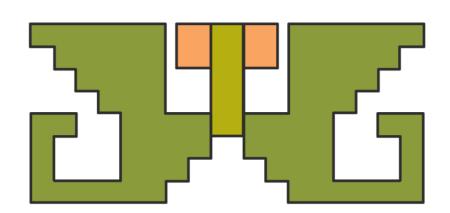


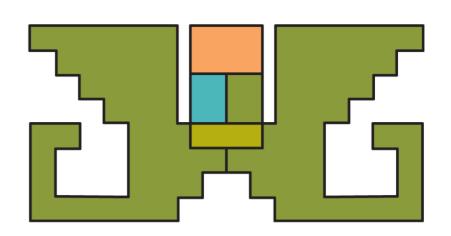




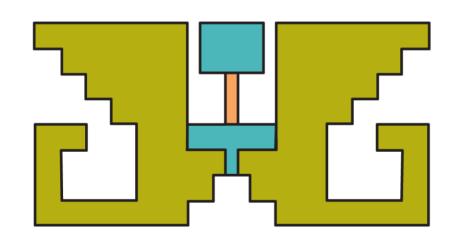


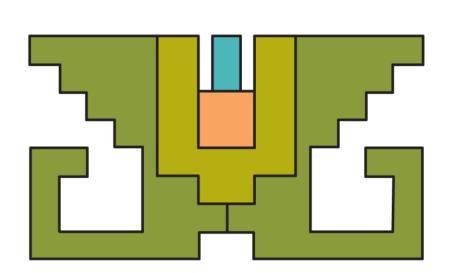
Dragons



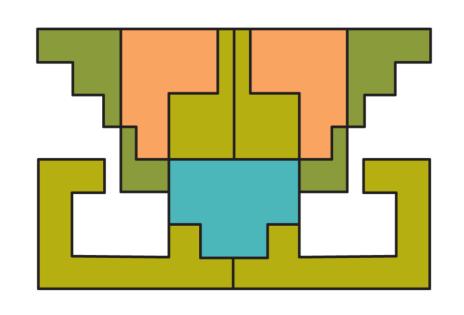


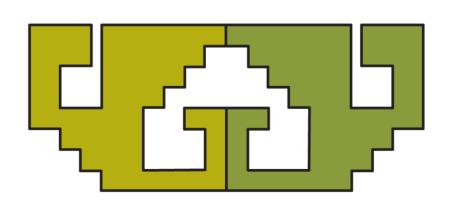
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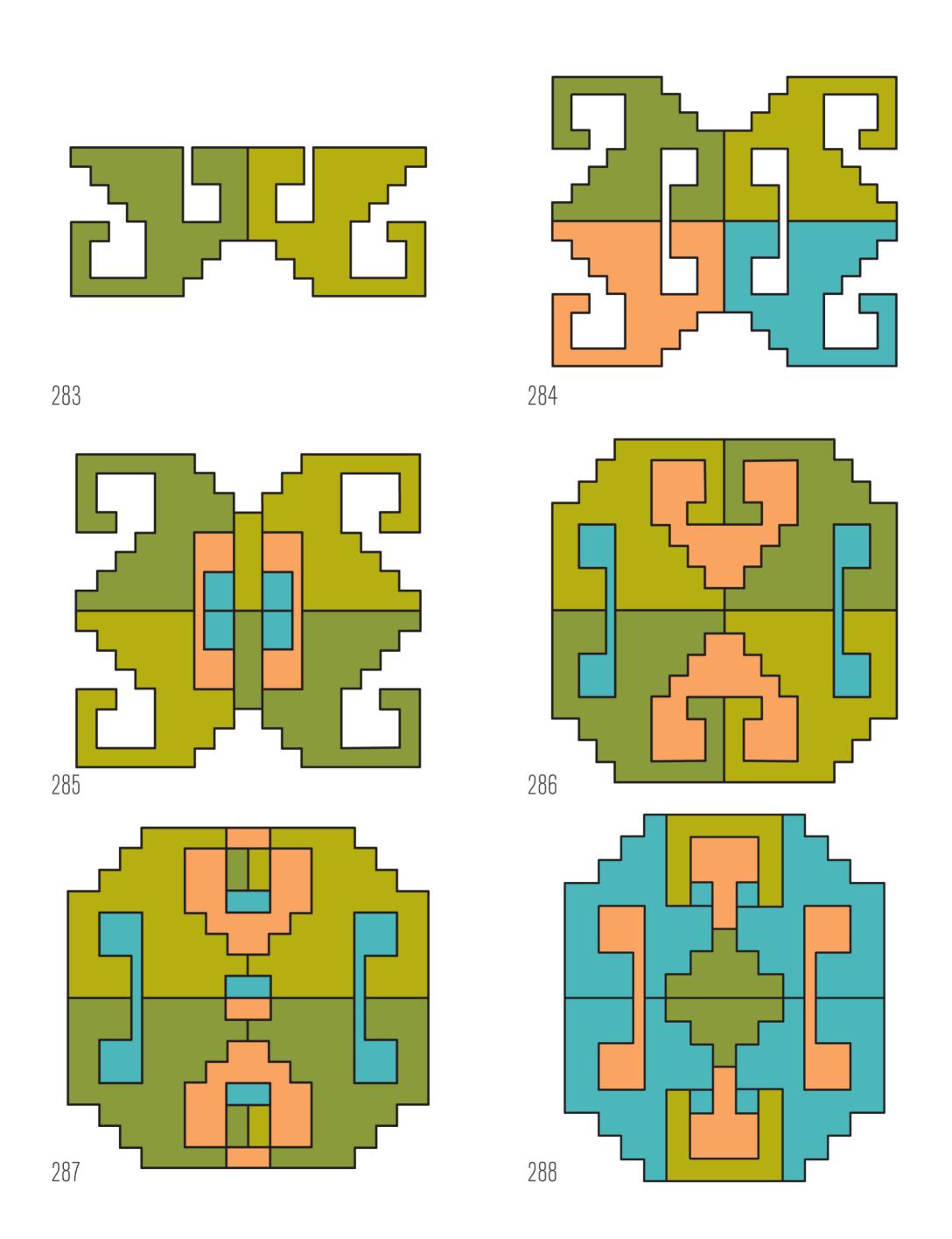




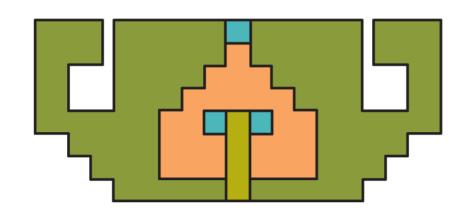
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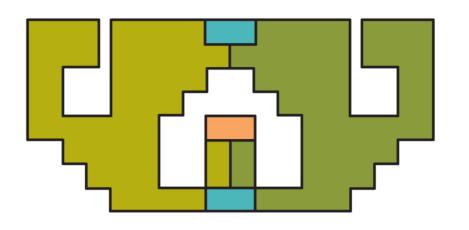




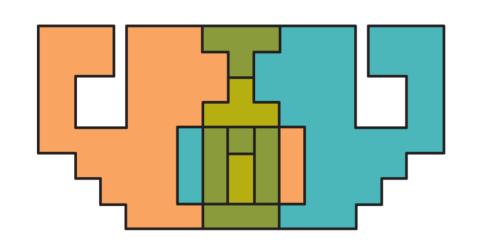


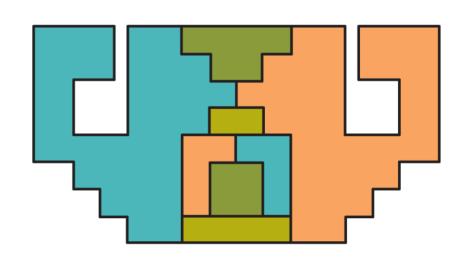
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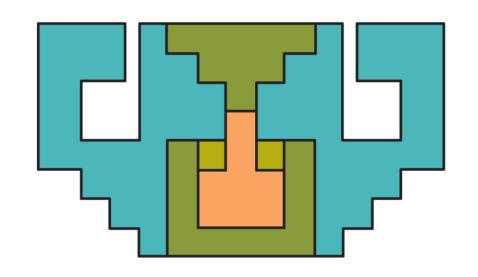


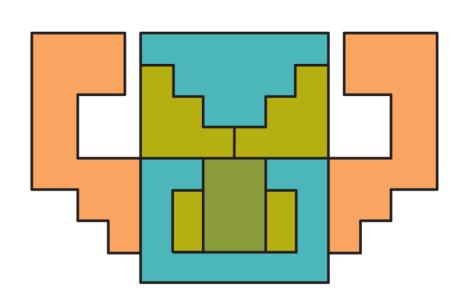
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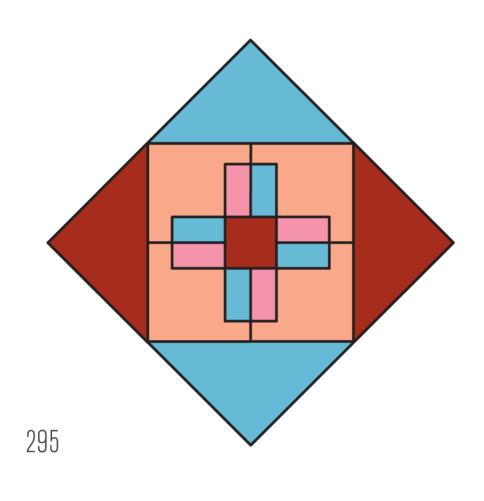


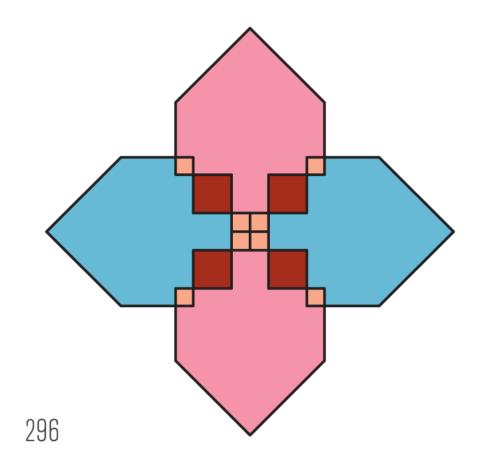
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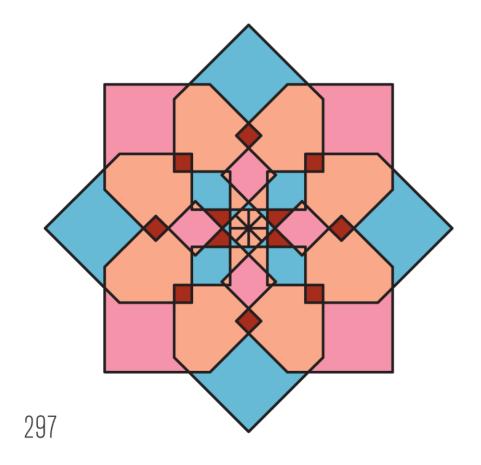


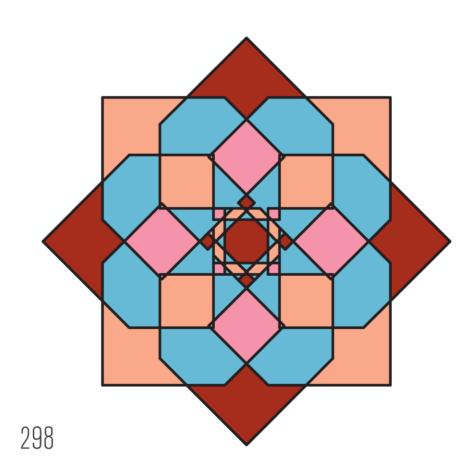




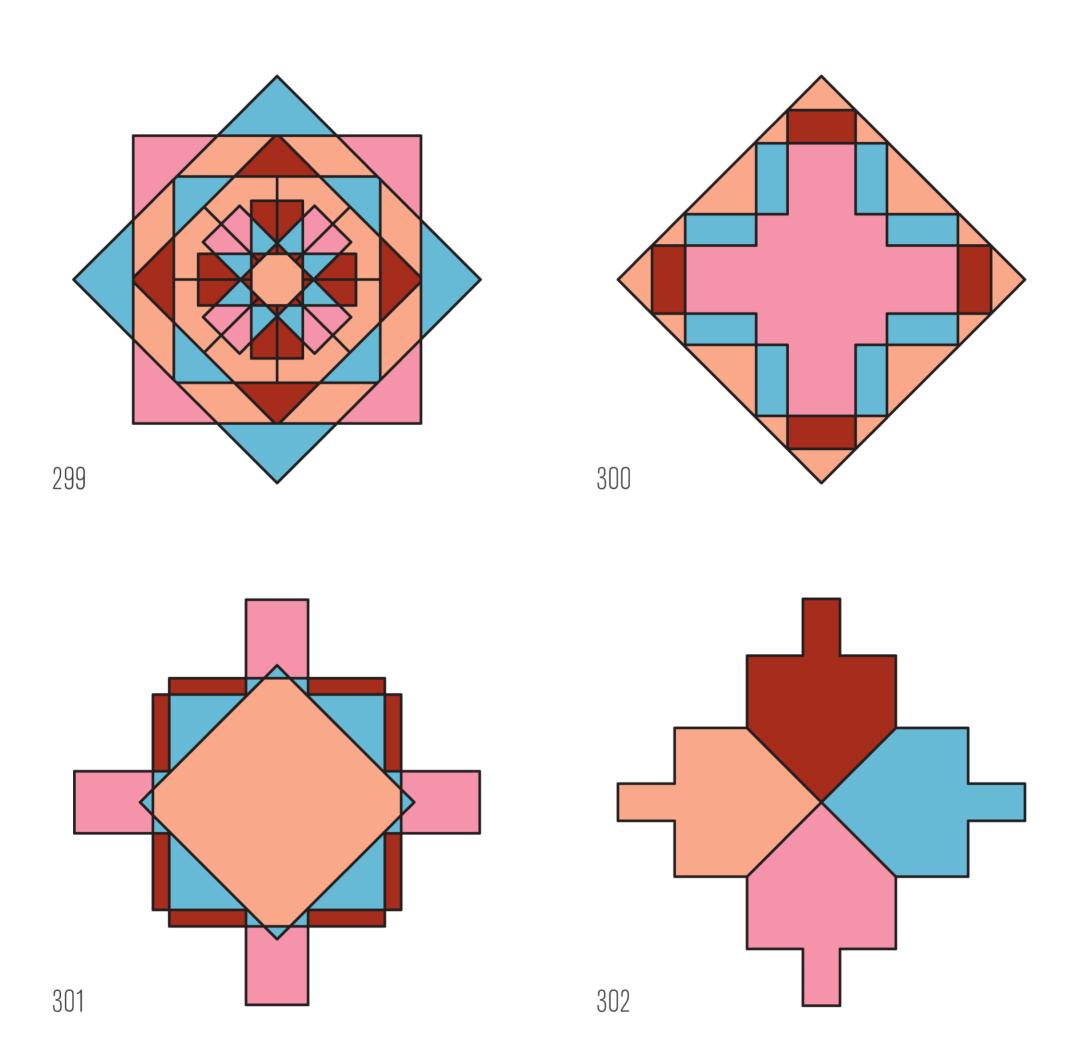


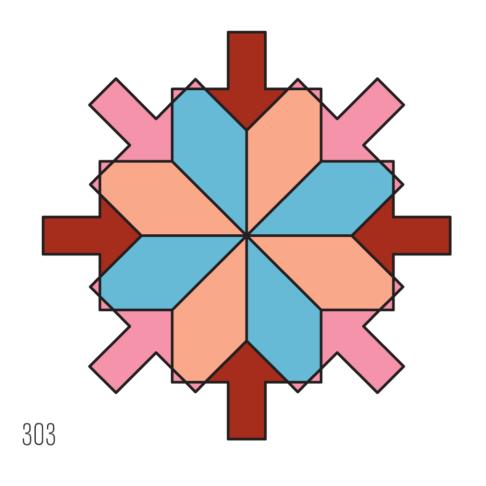


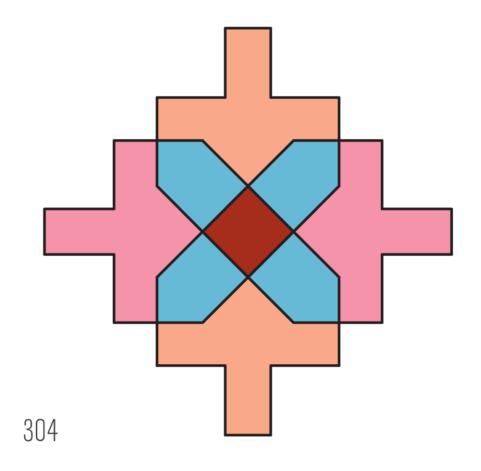


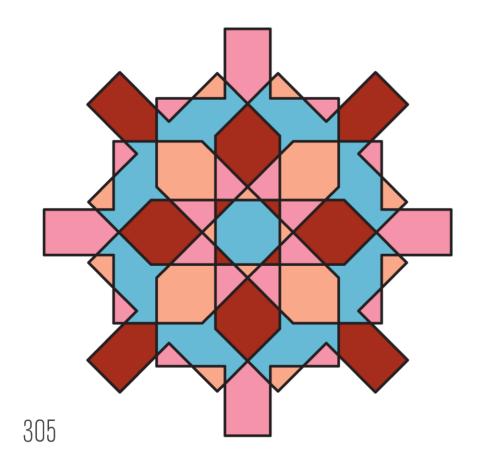


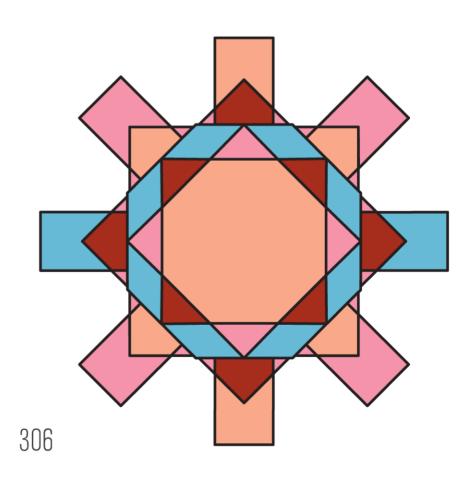
Dreidels



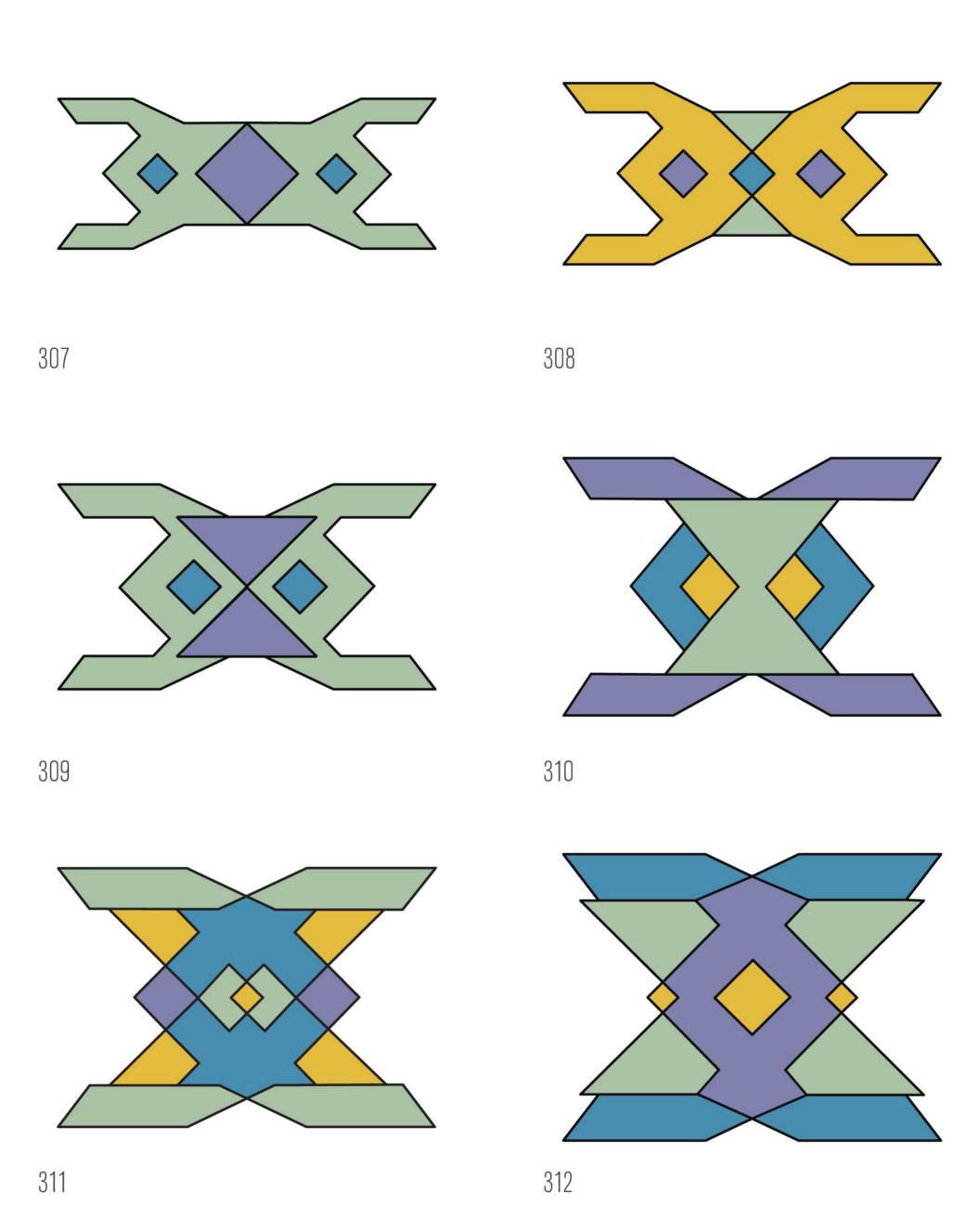


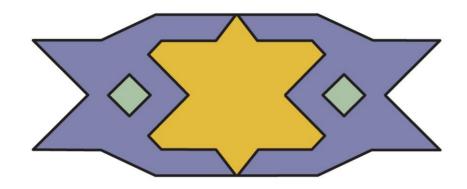


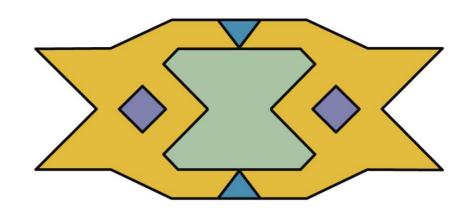


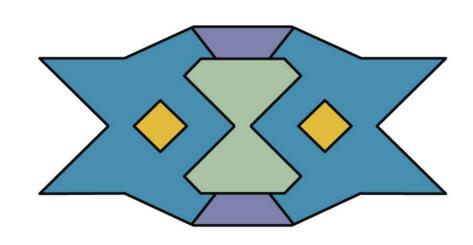


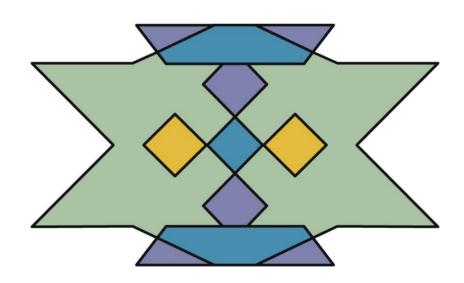
Eagle Eyes

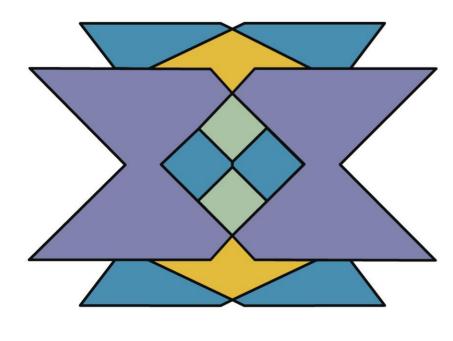


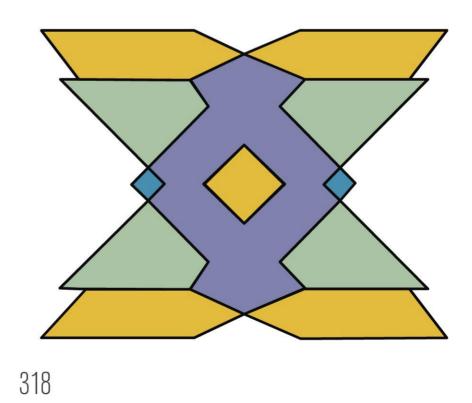




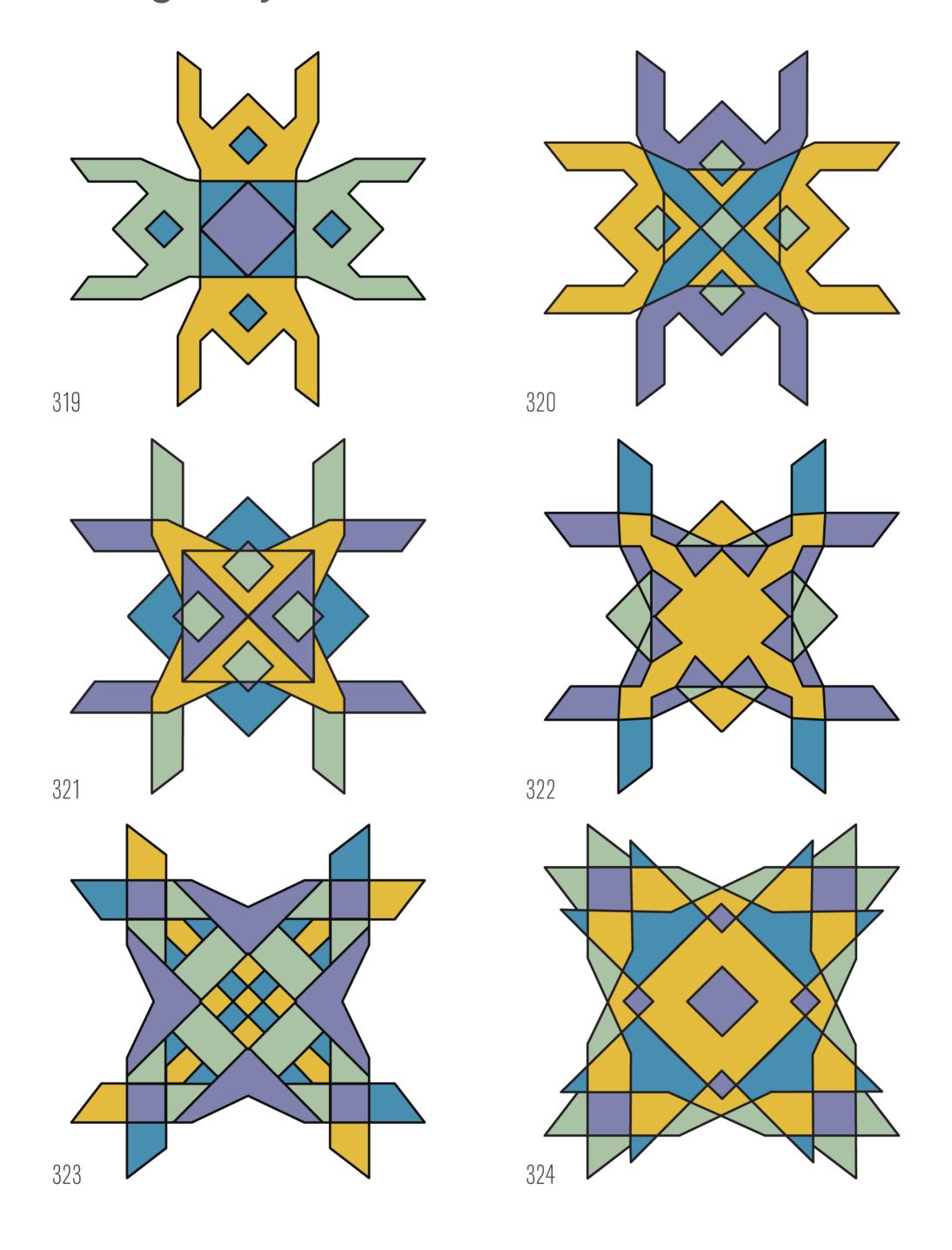


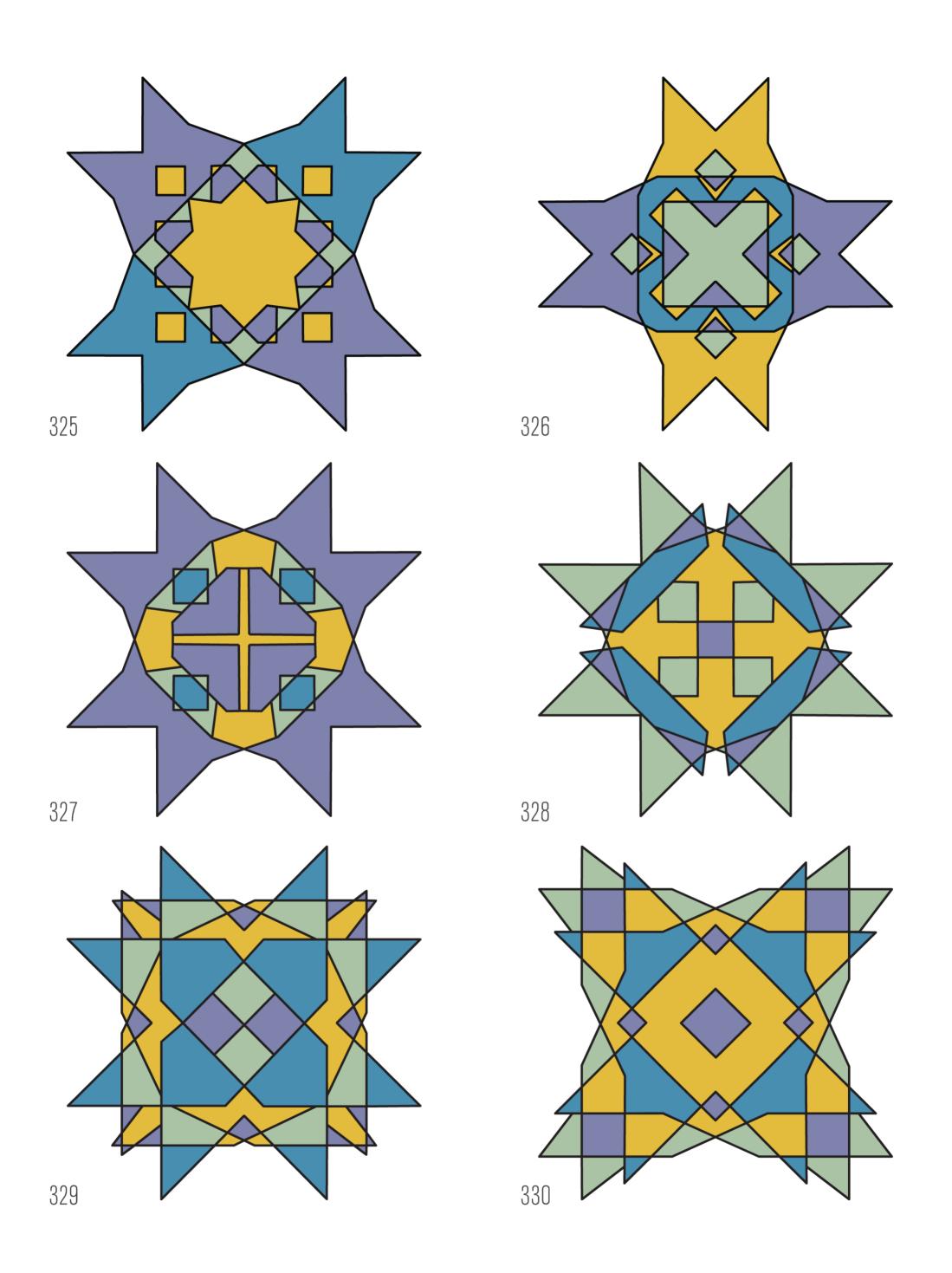




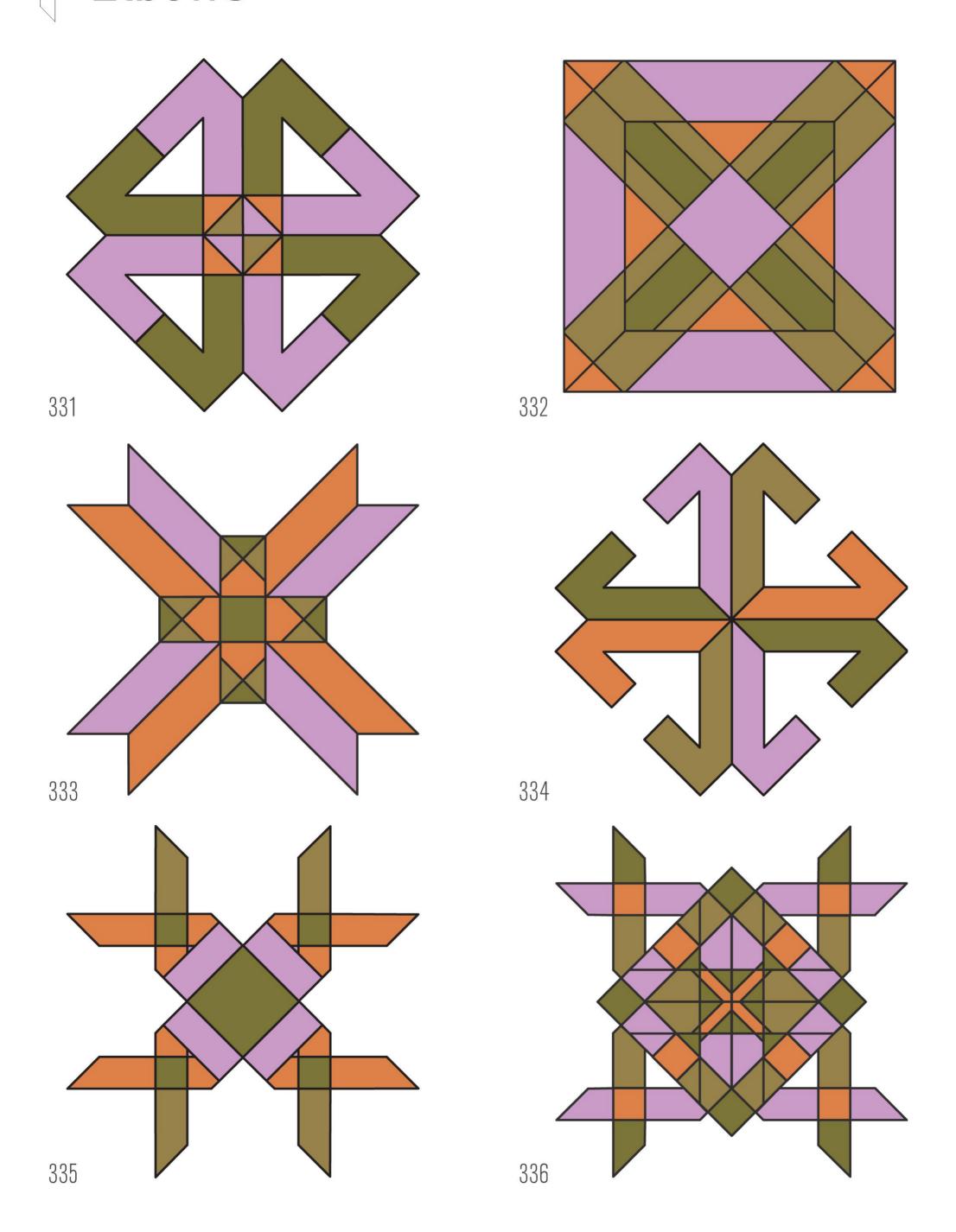


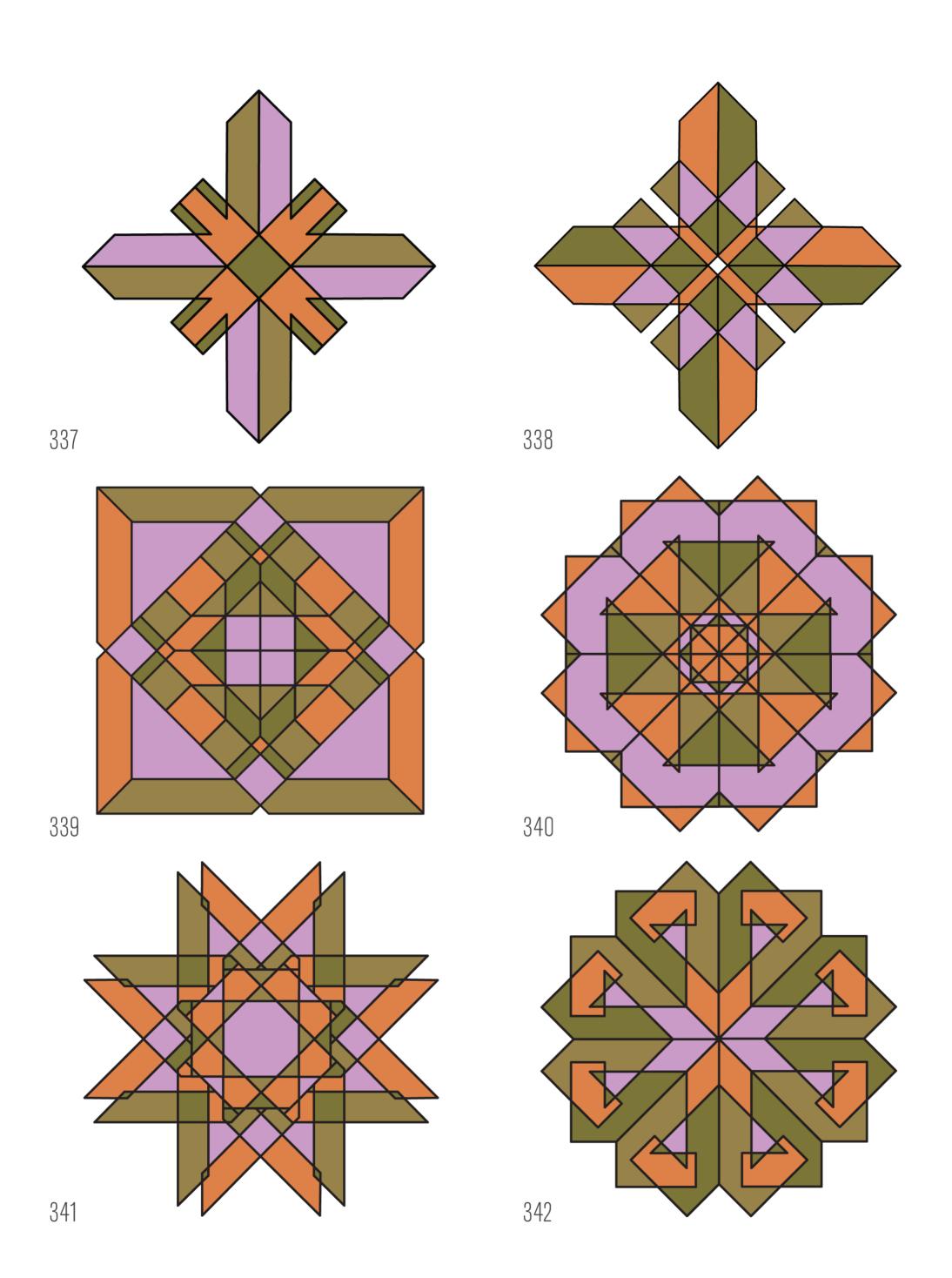
Eagle Eyes



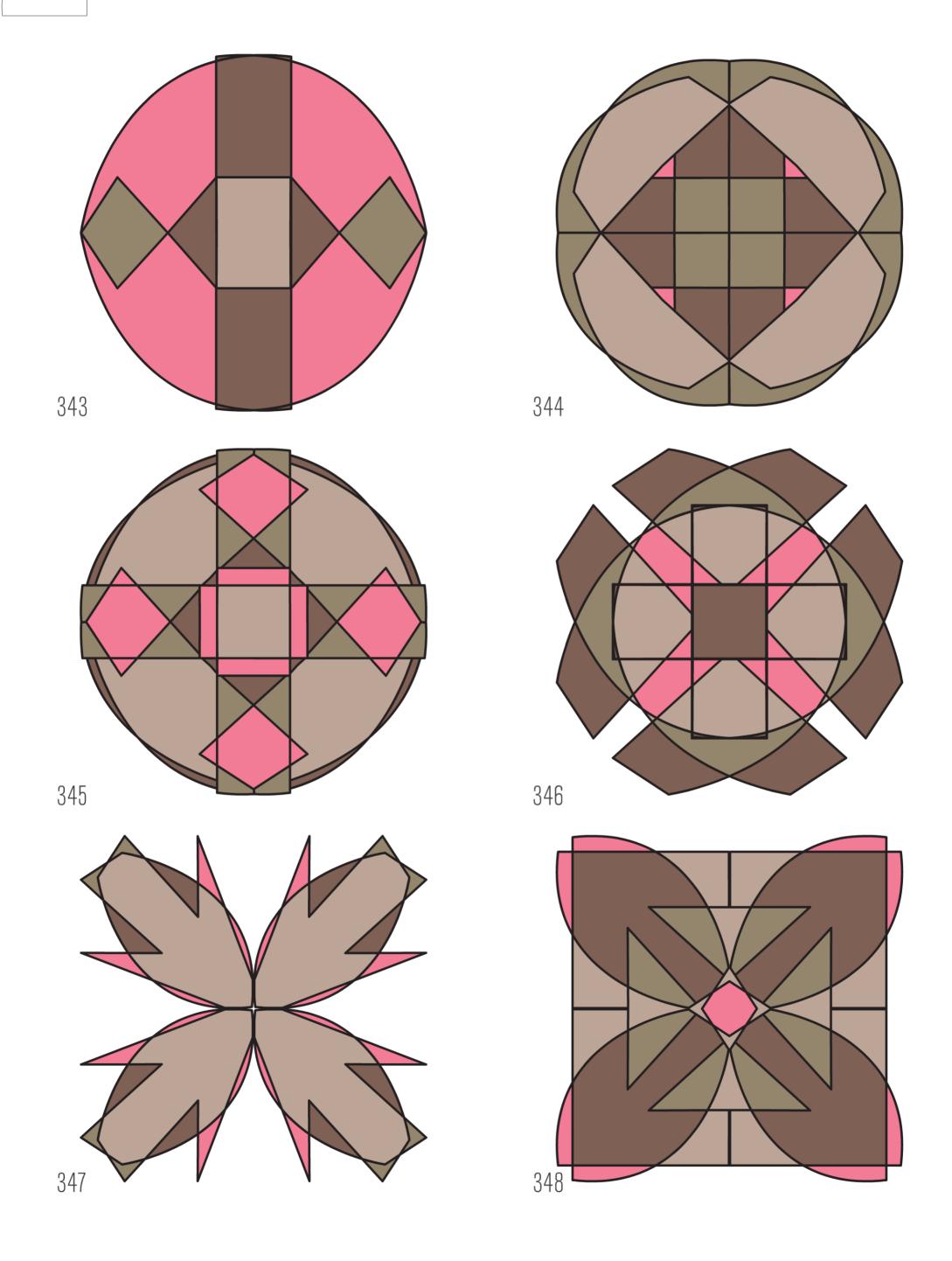


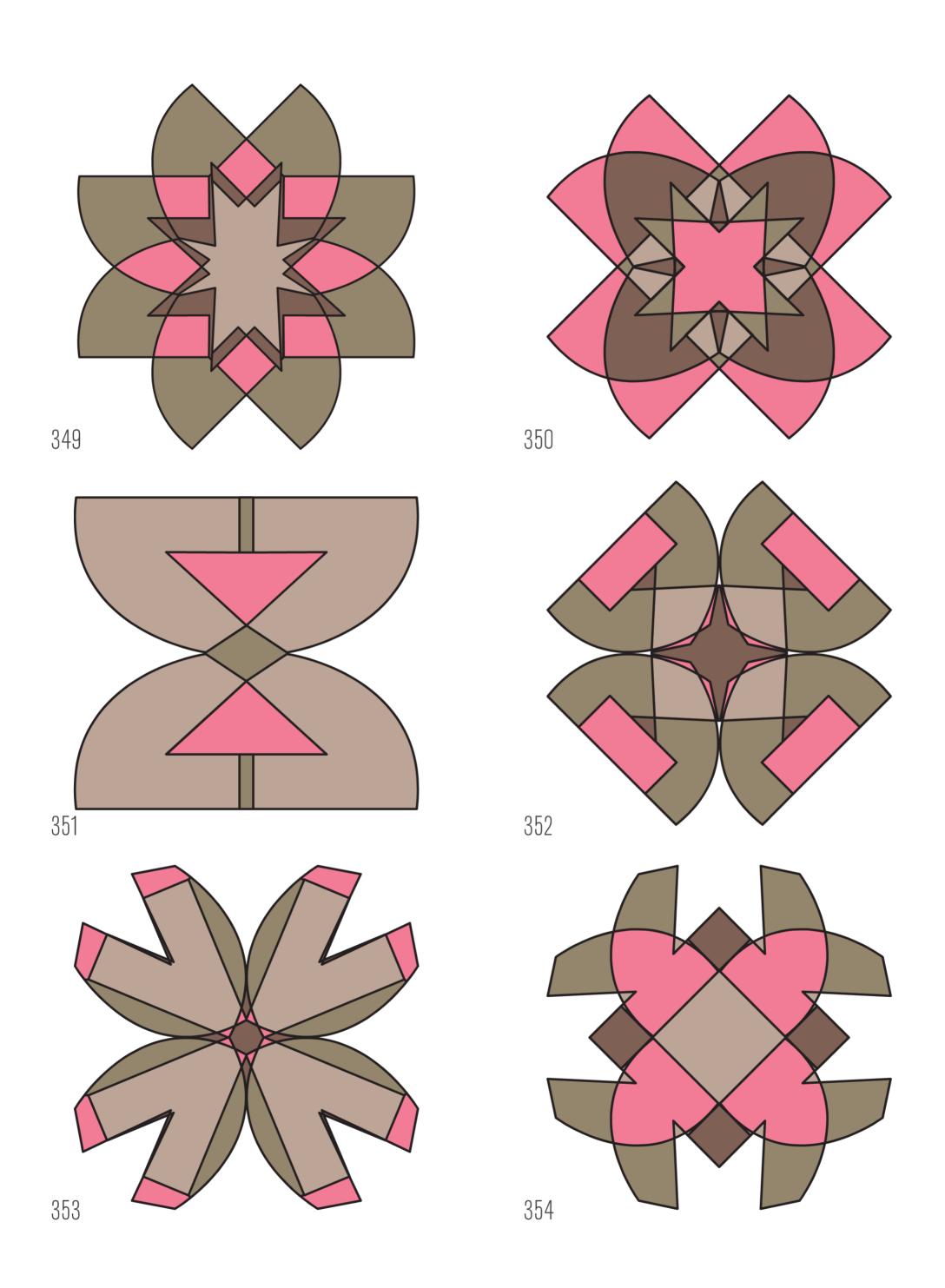
Elbows



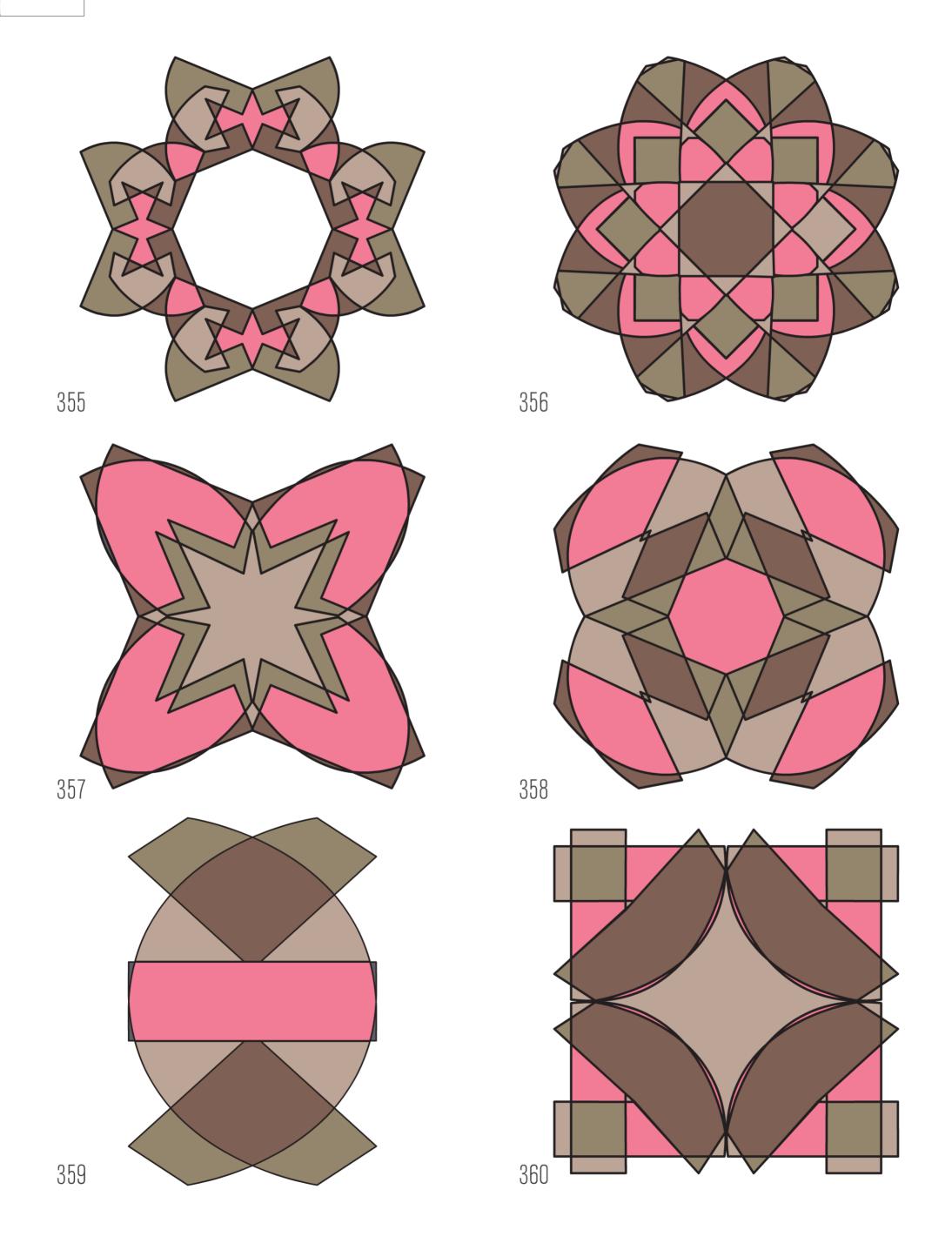


Elbows 2





Elbows 2



Fans

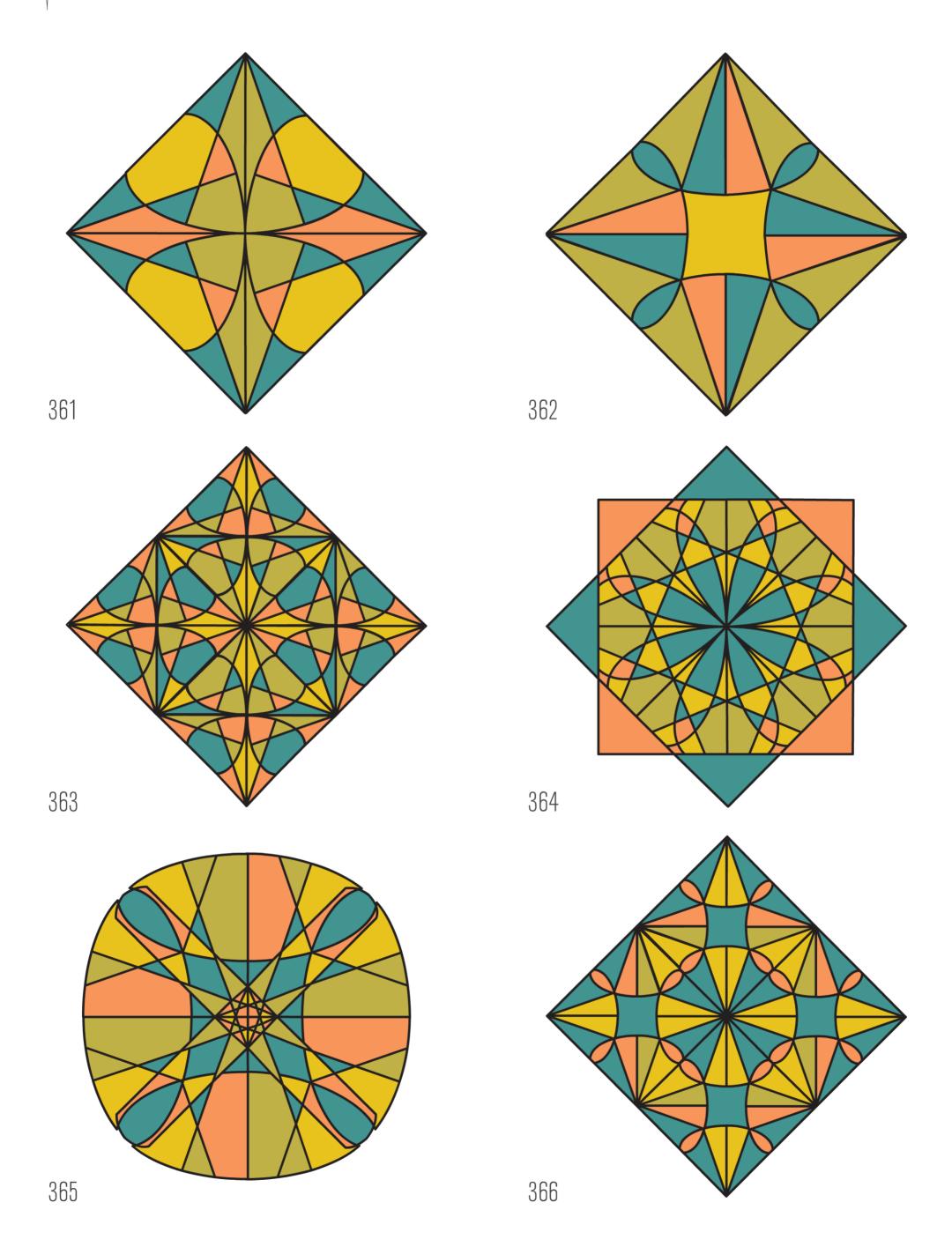
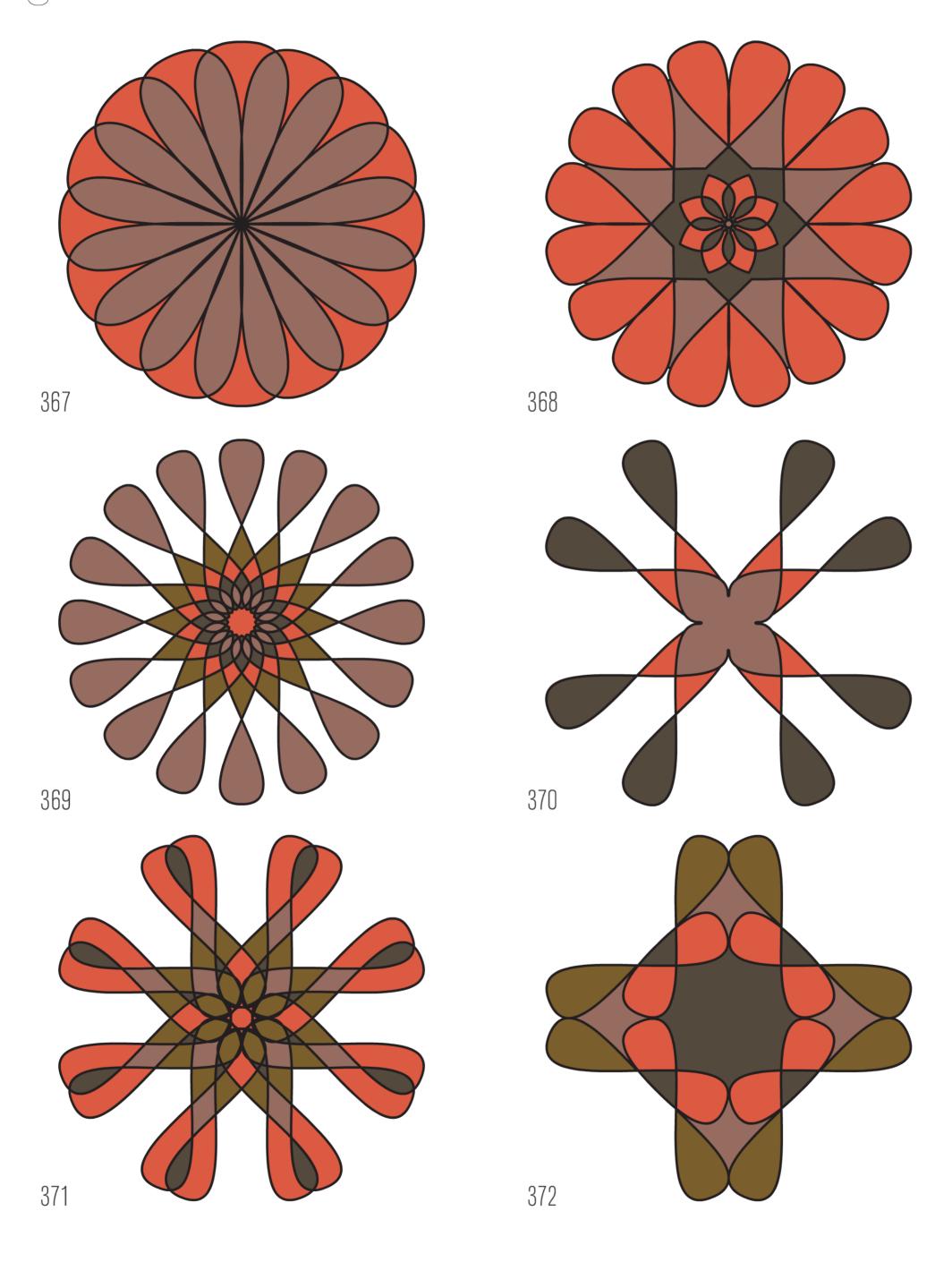
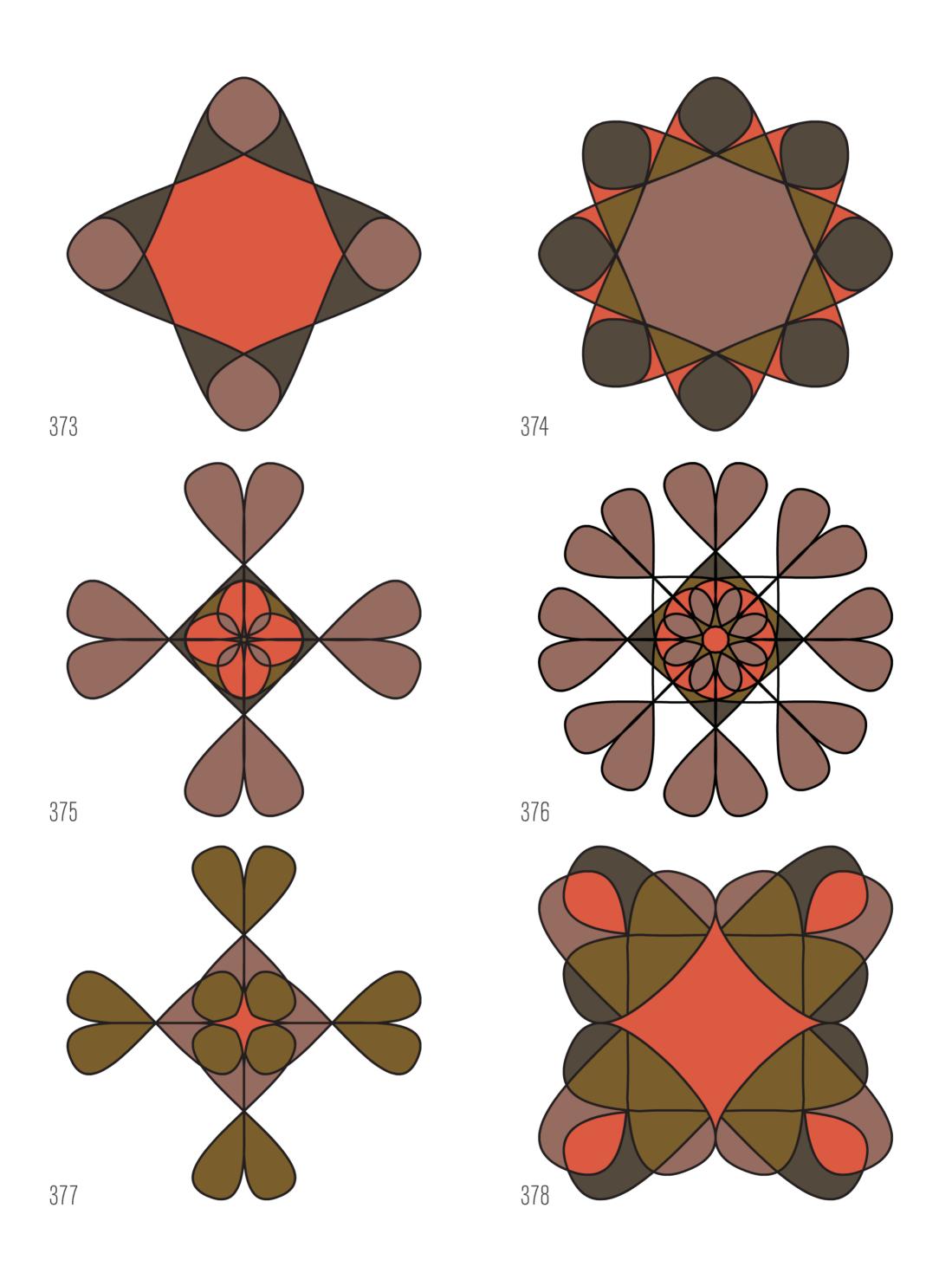
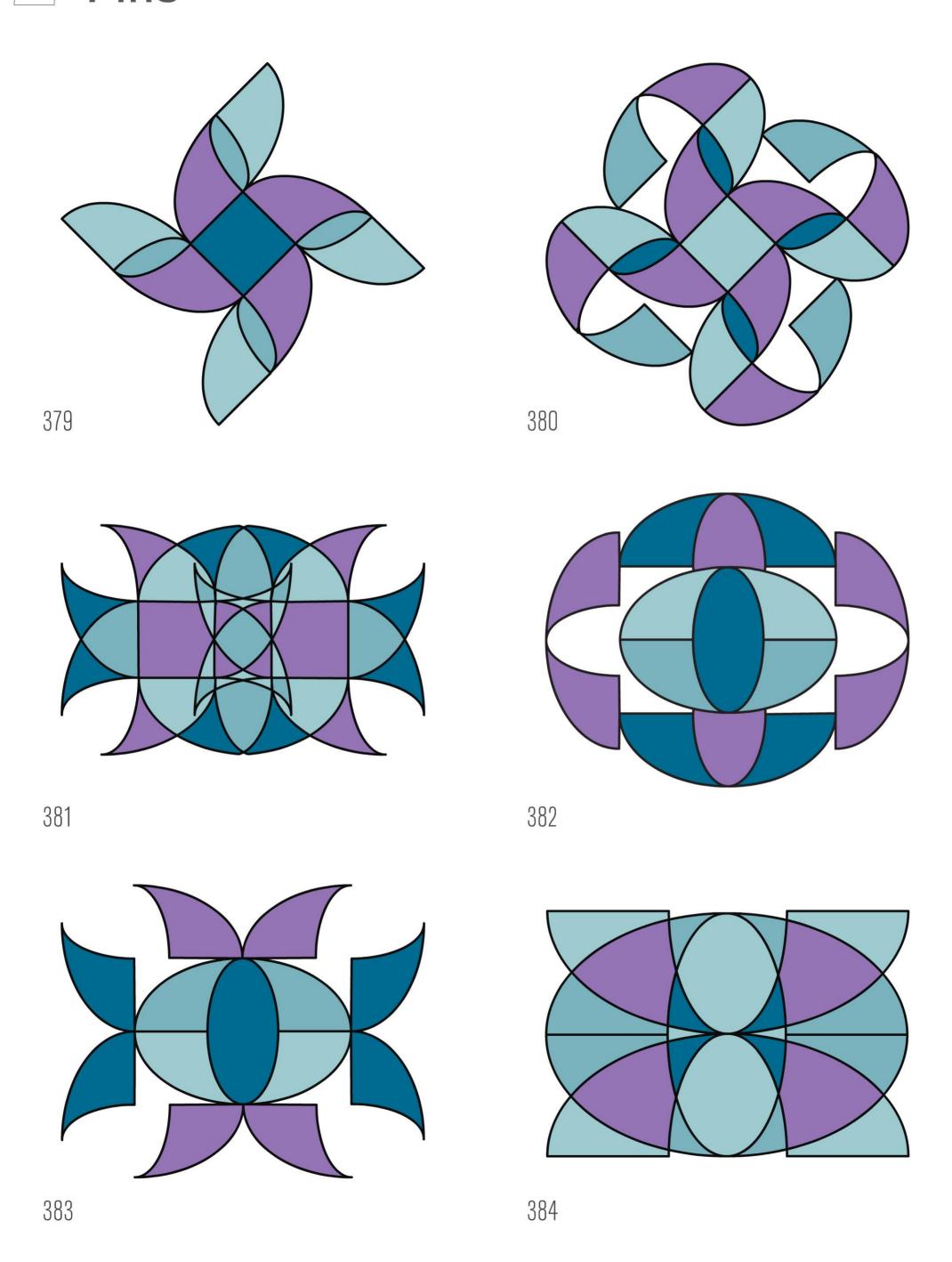


Figure 8

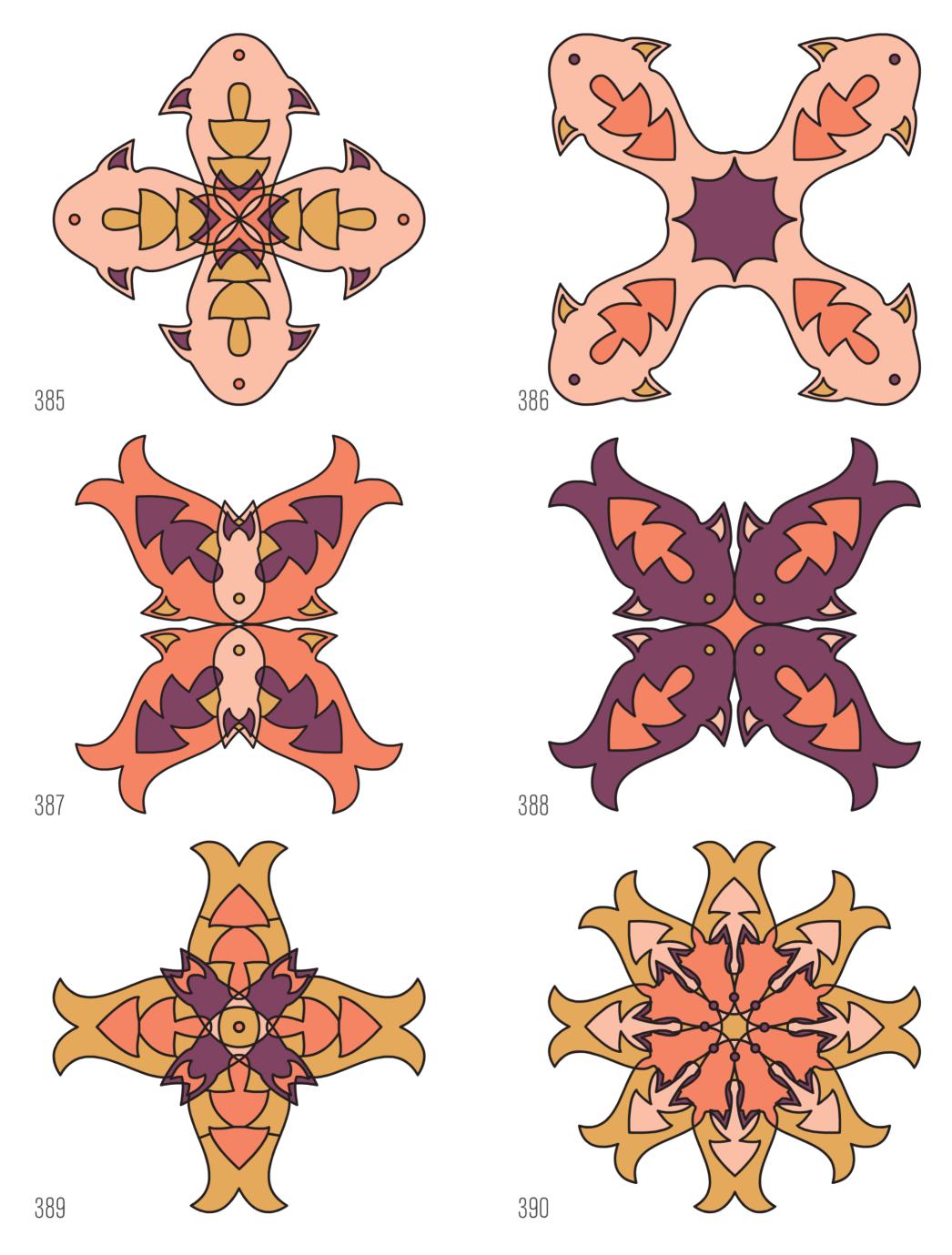




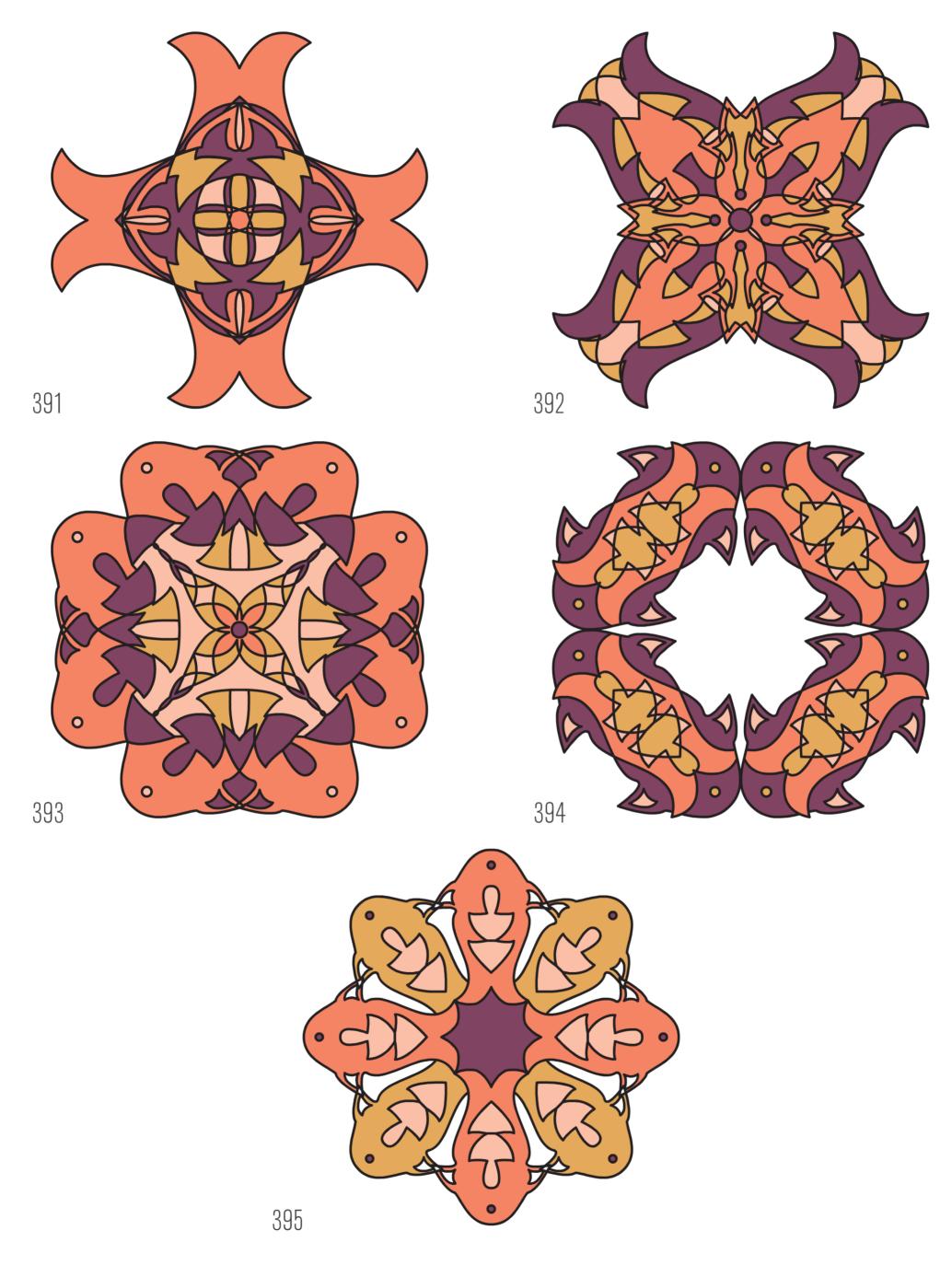
Fins

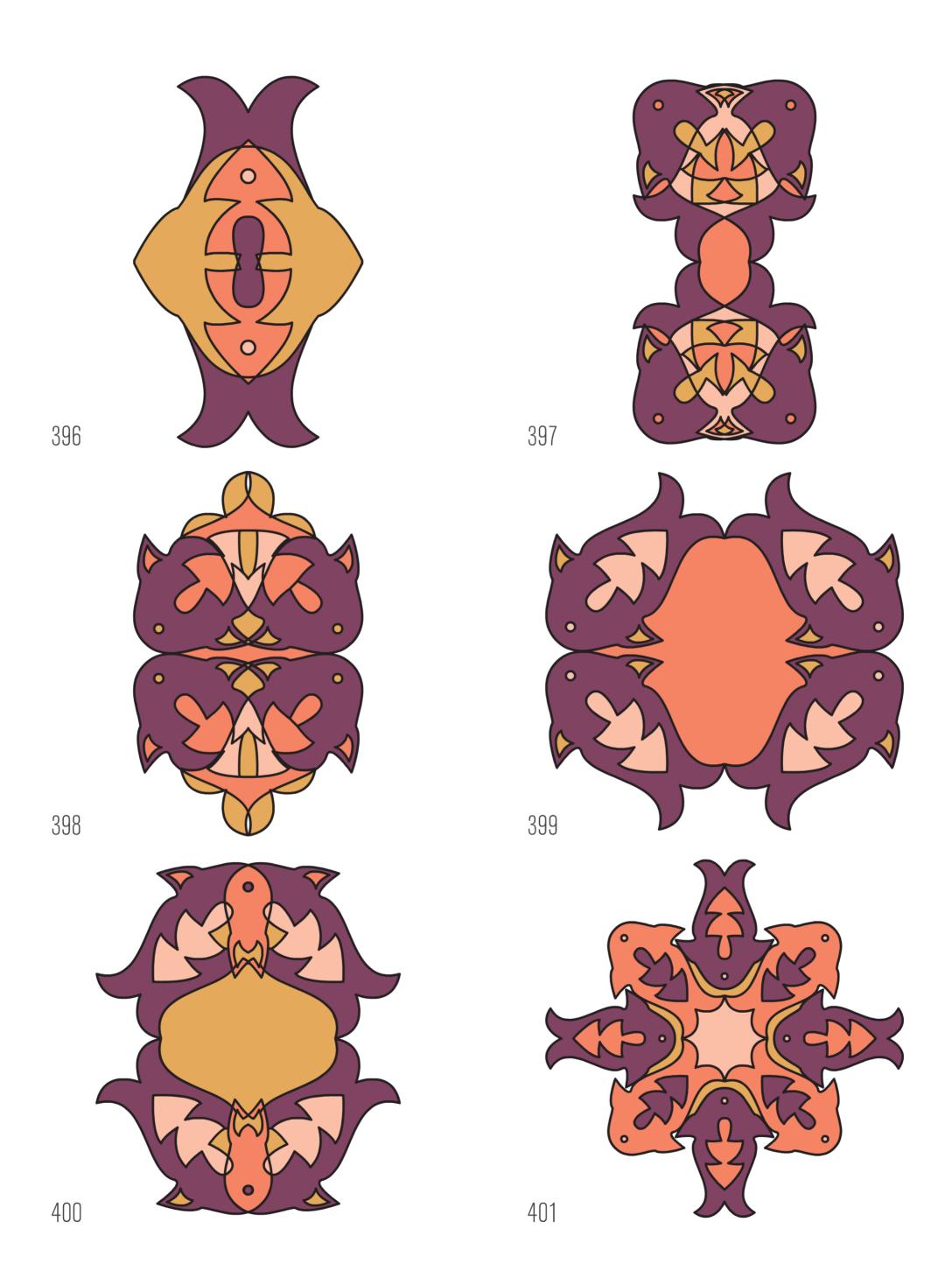




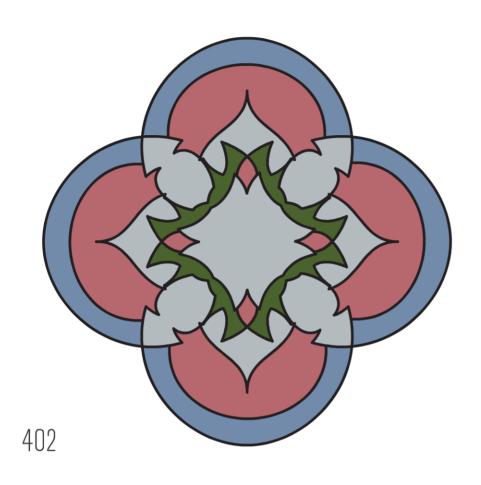


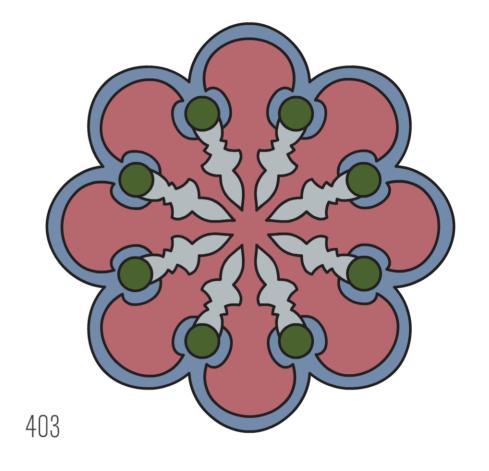


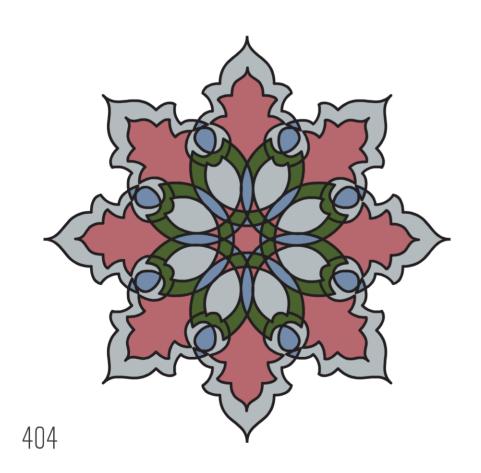


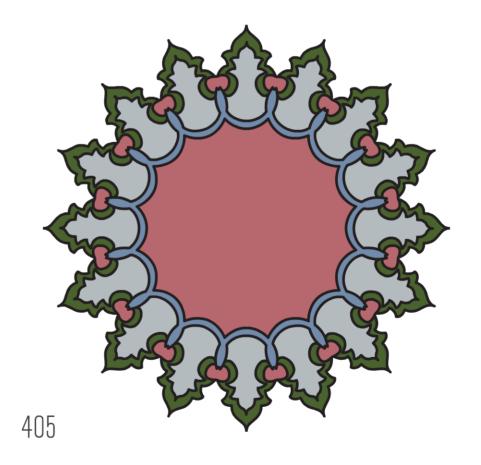


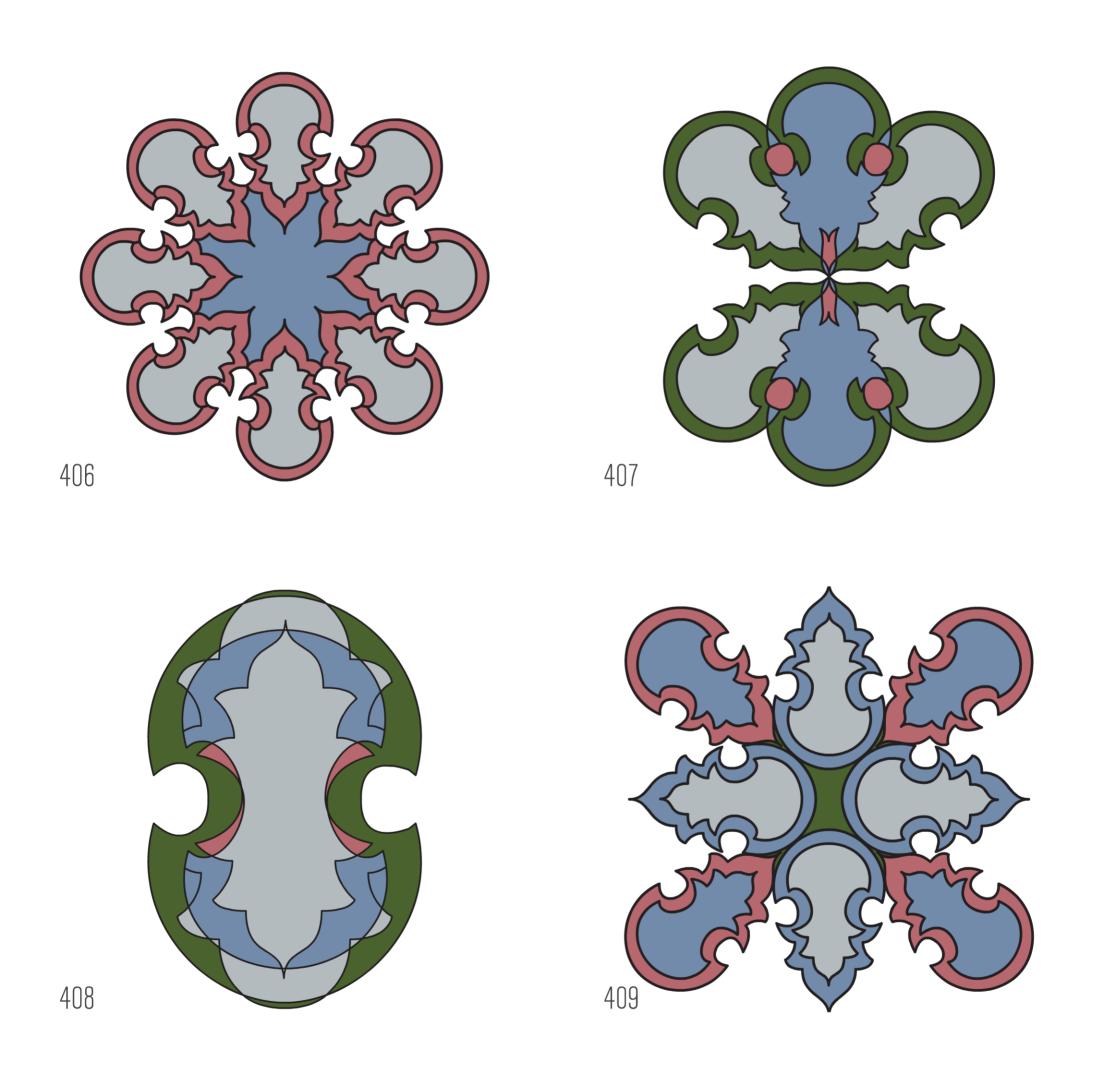
Fleur de lis



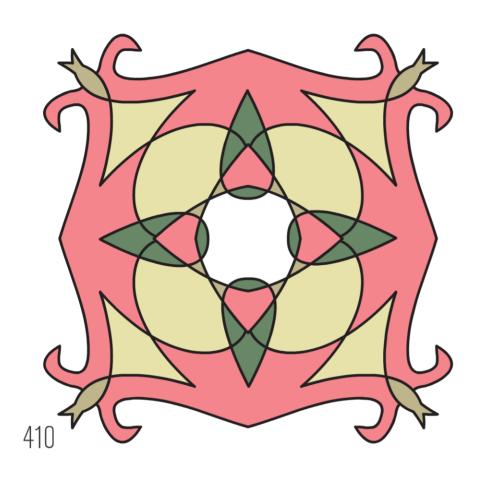


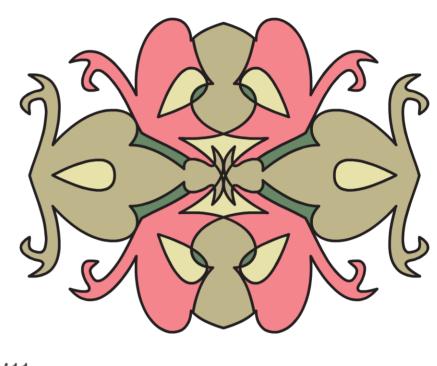




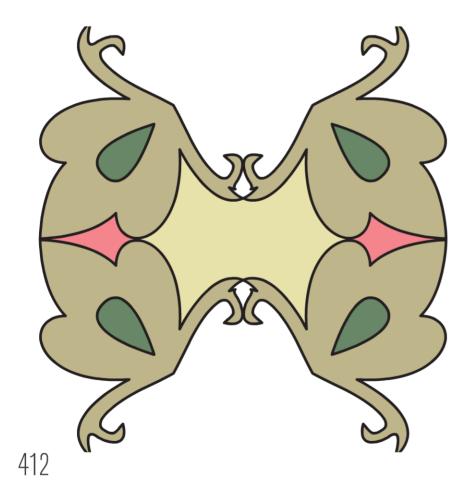


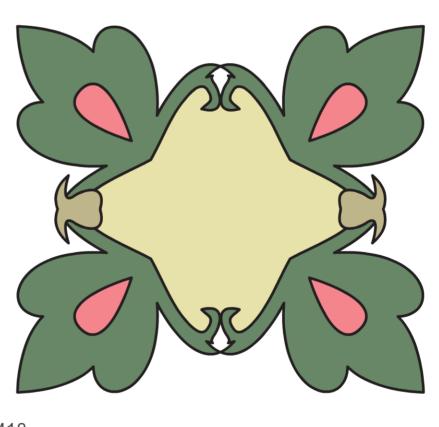
Fleur de lis 2



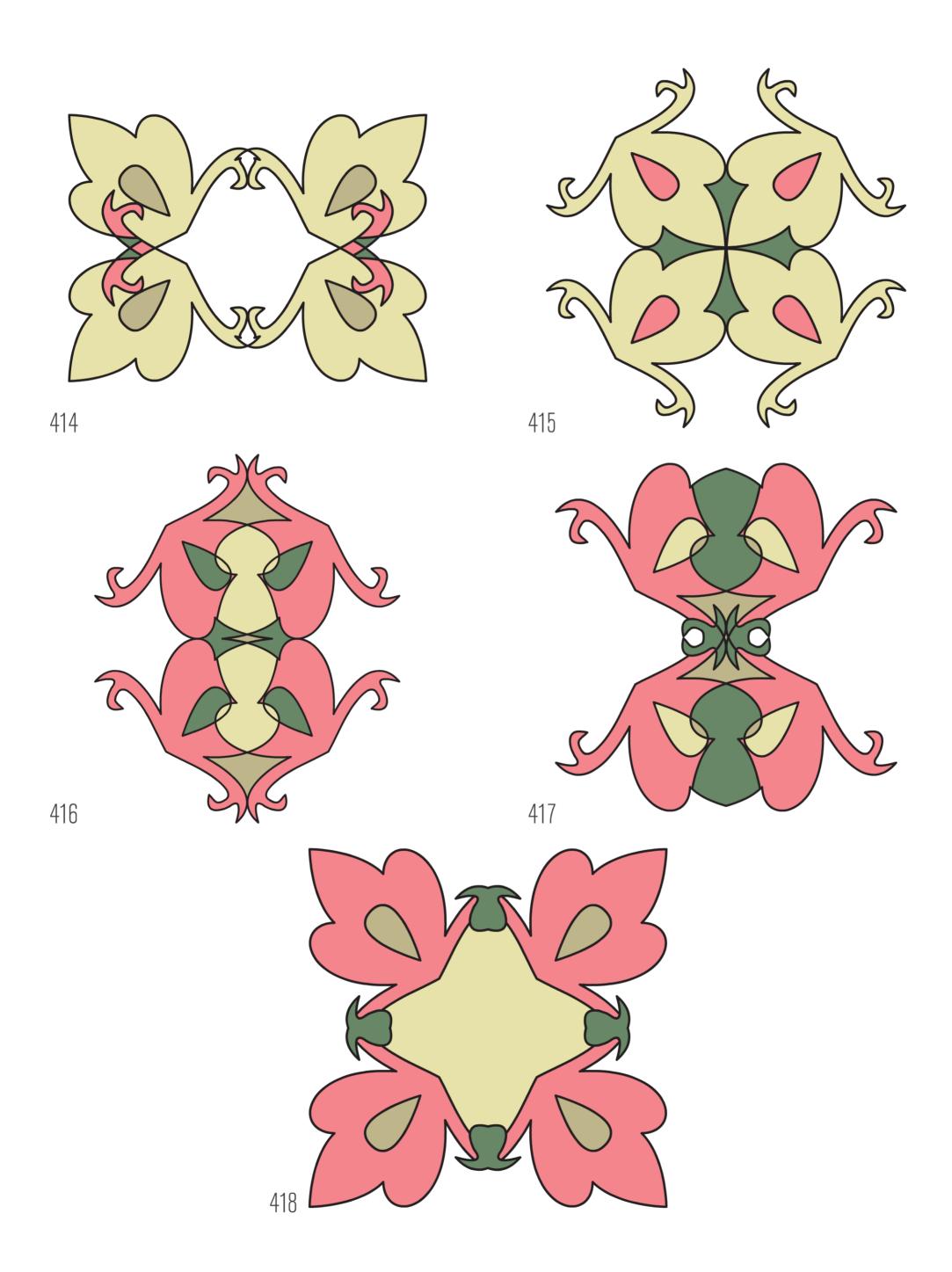


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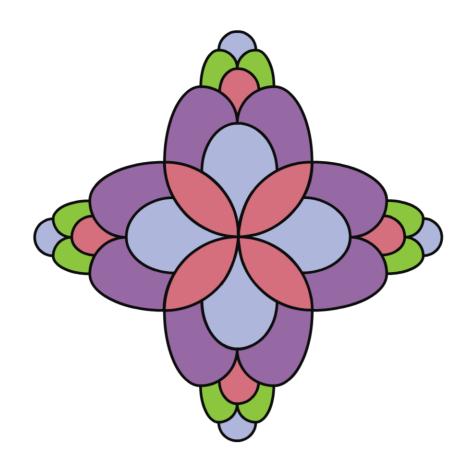


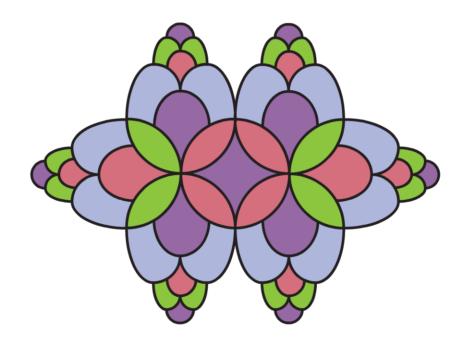


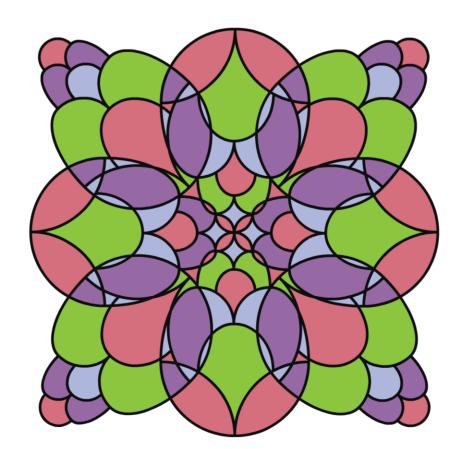
413

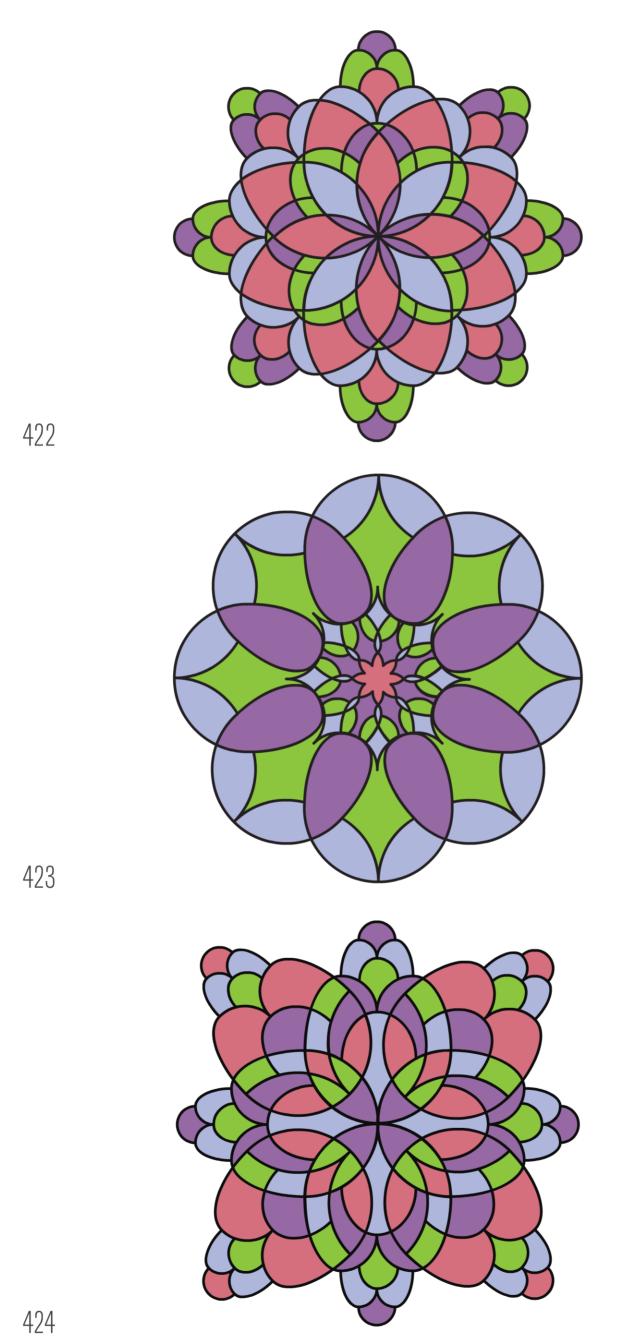




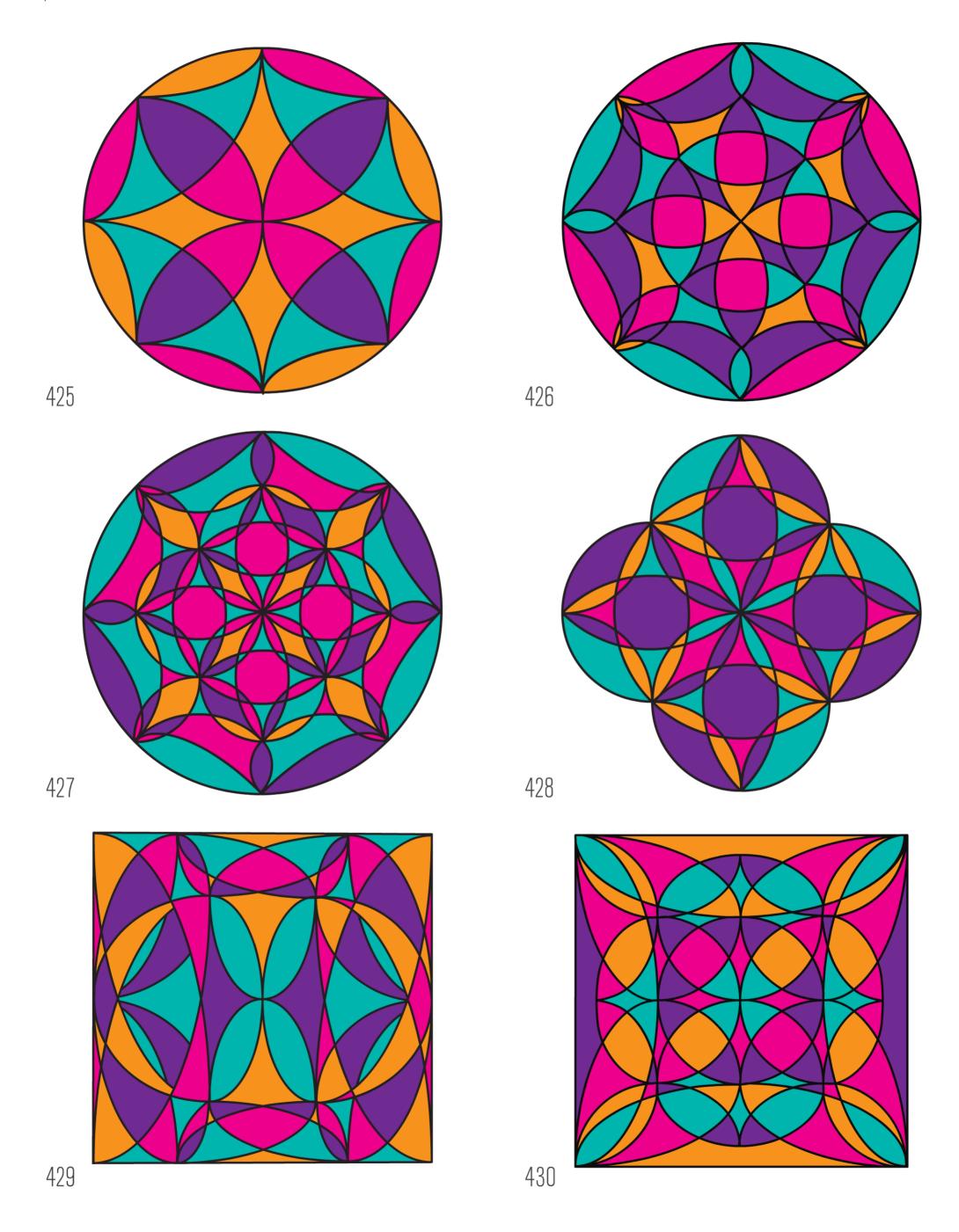




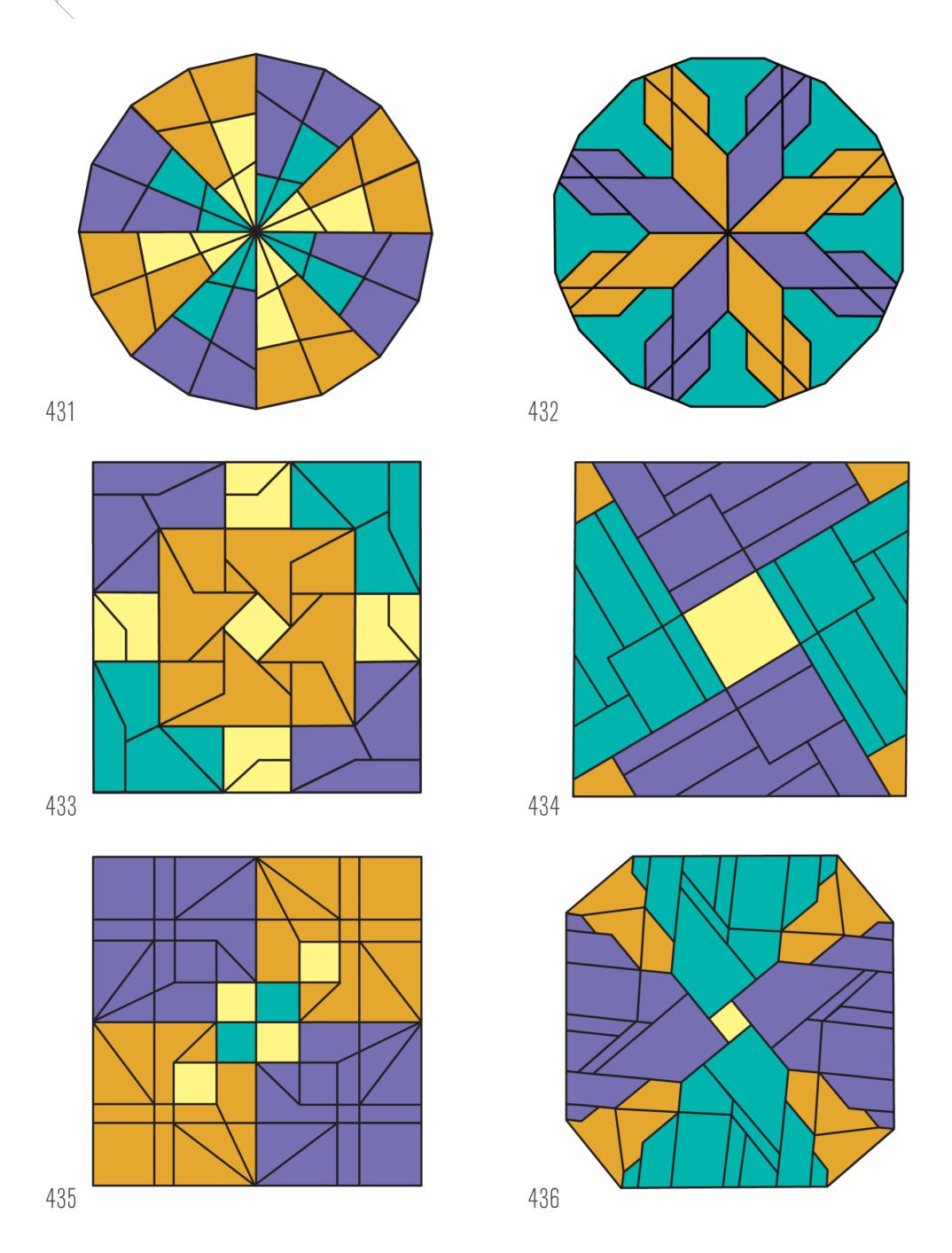


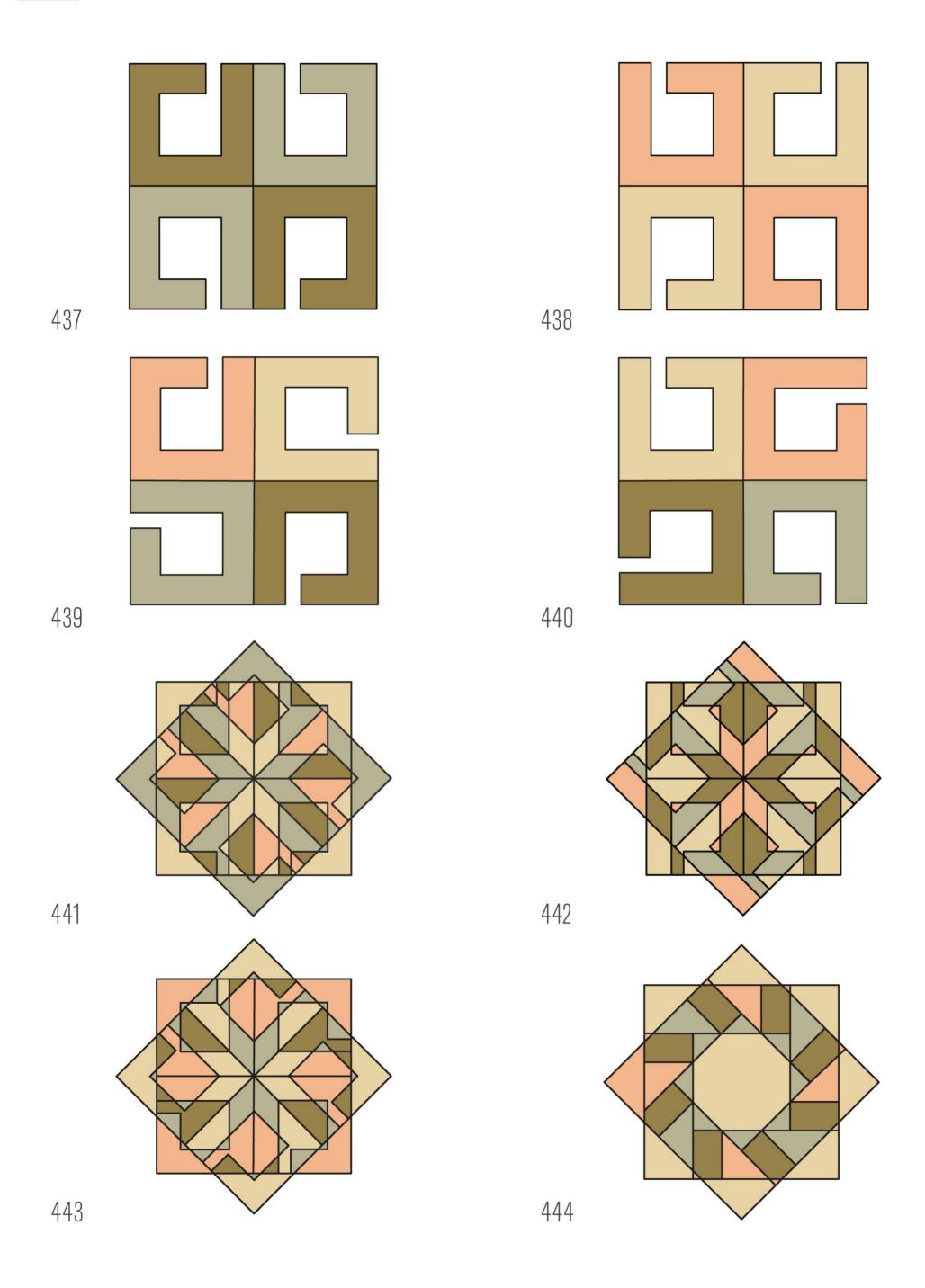


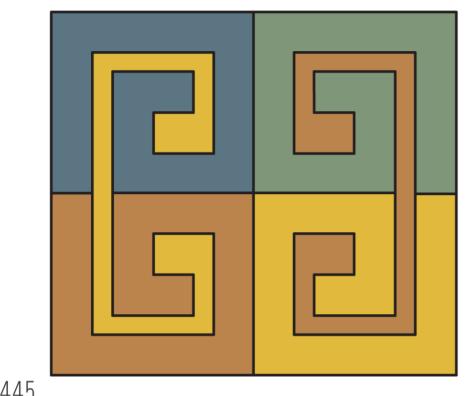
Filled Arcs

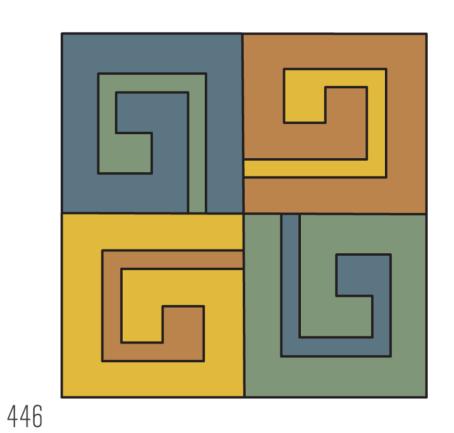


Fractures

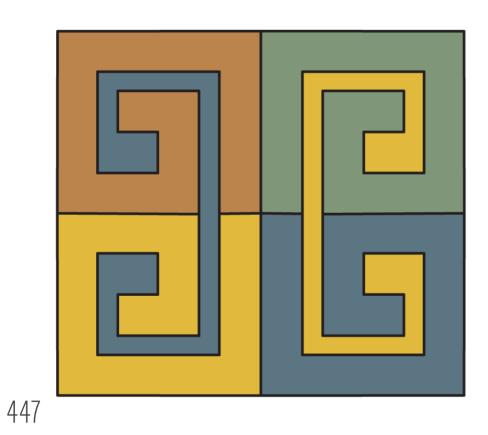


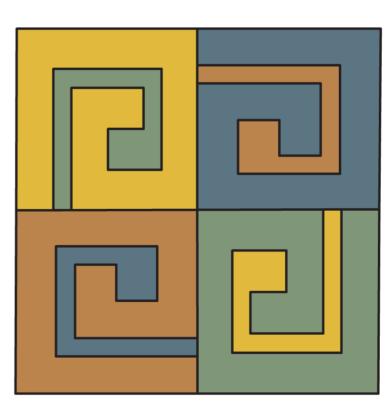






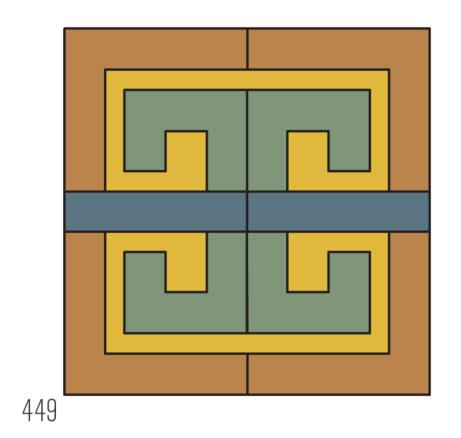
445

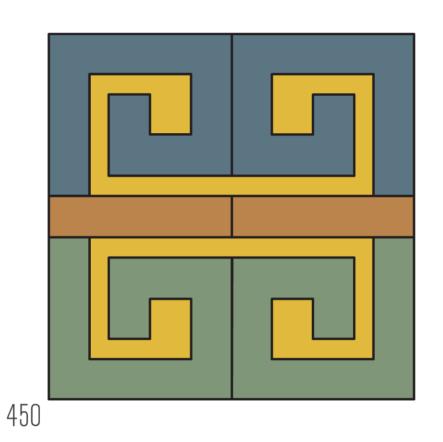


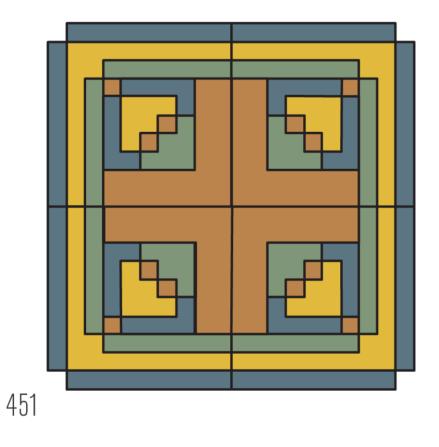


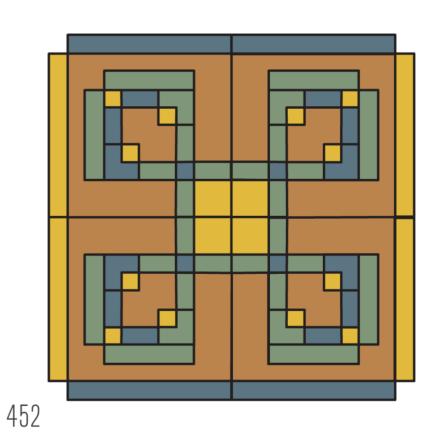
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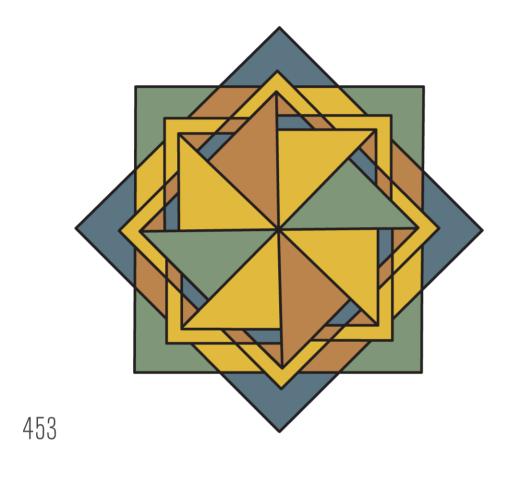
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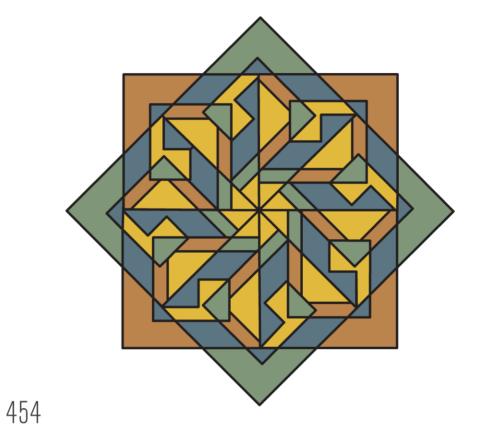


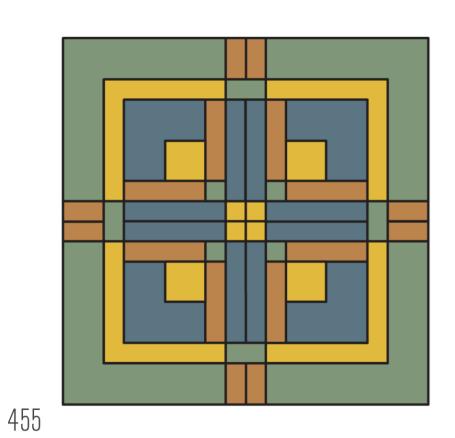


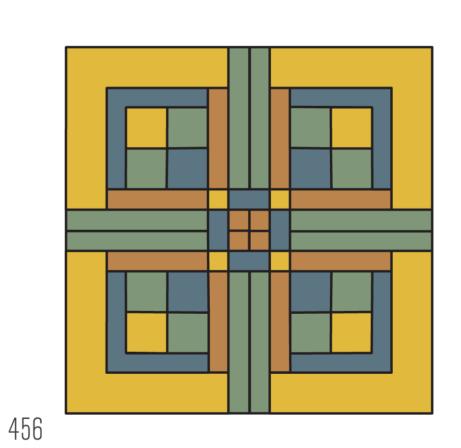




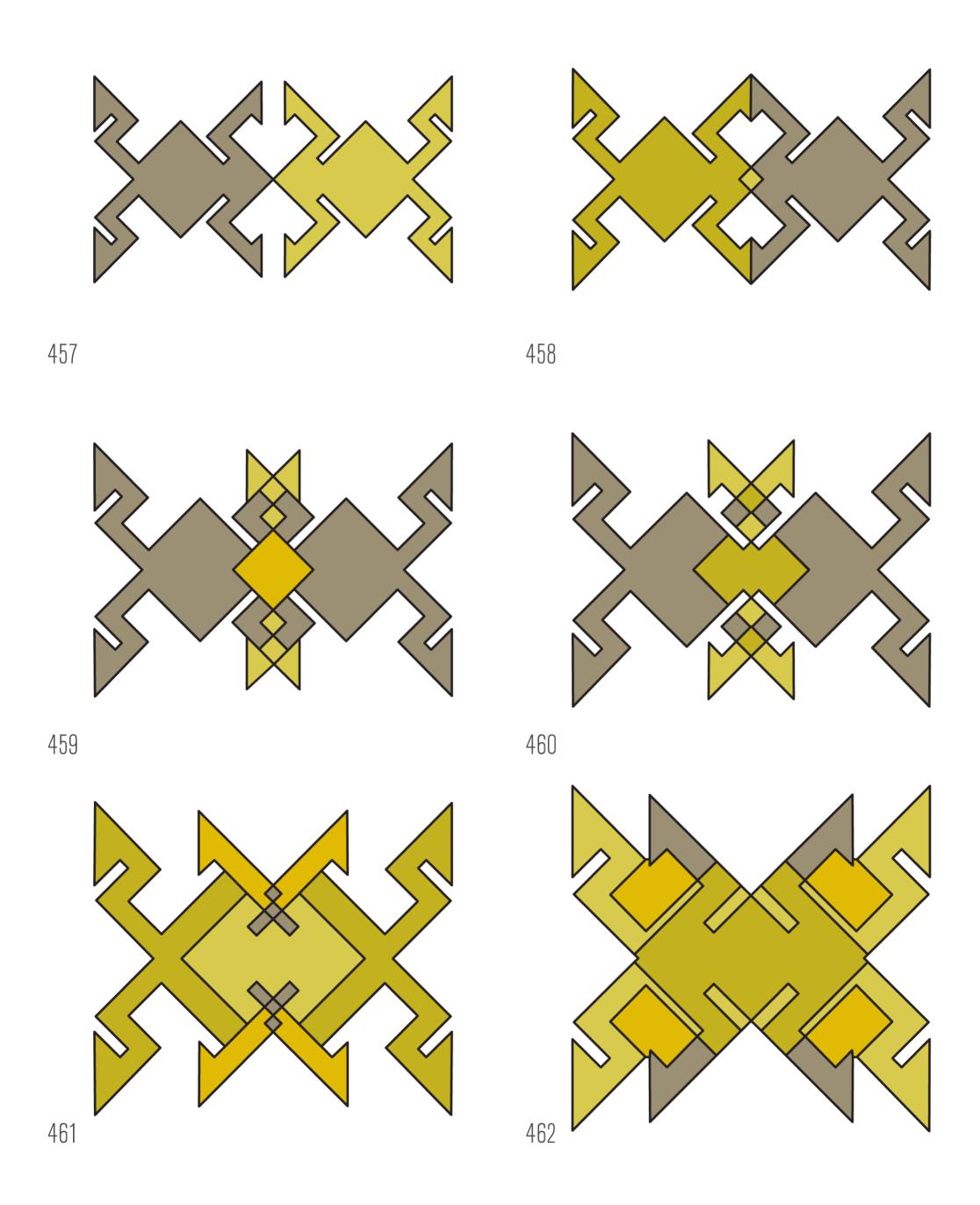


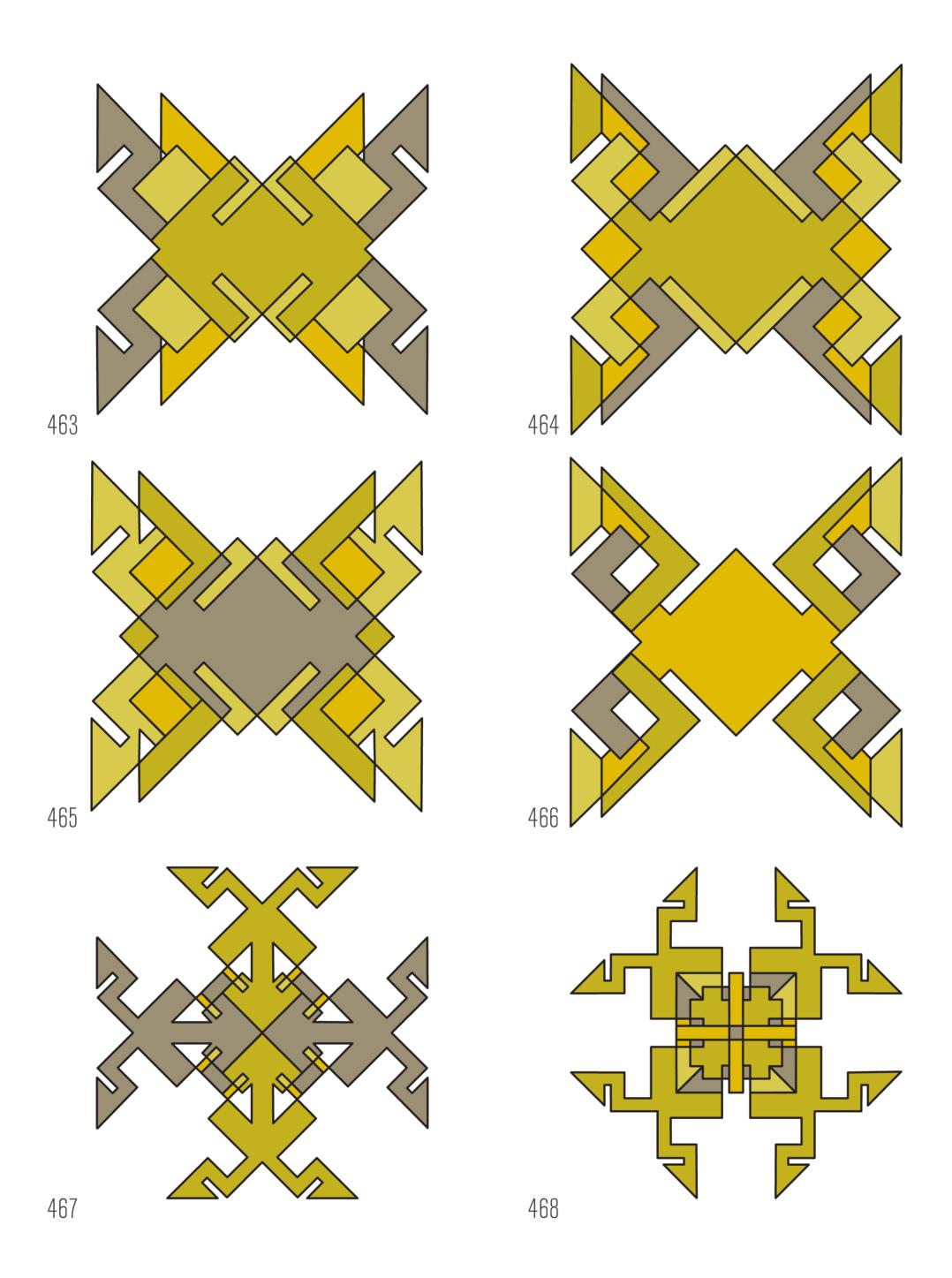


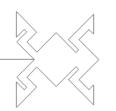




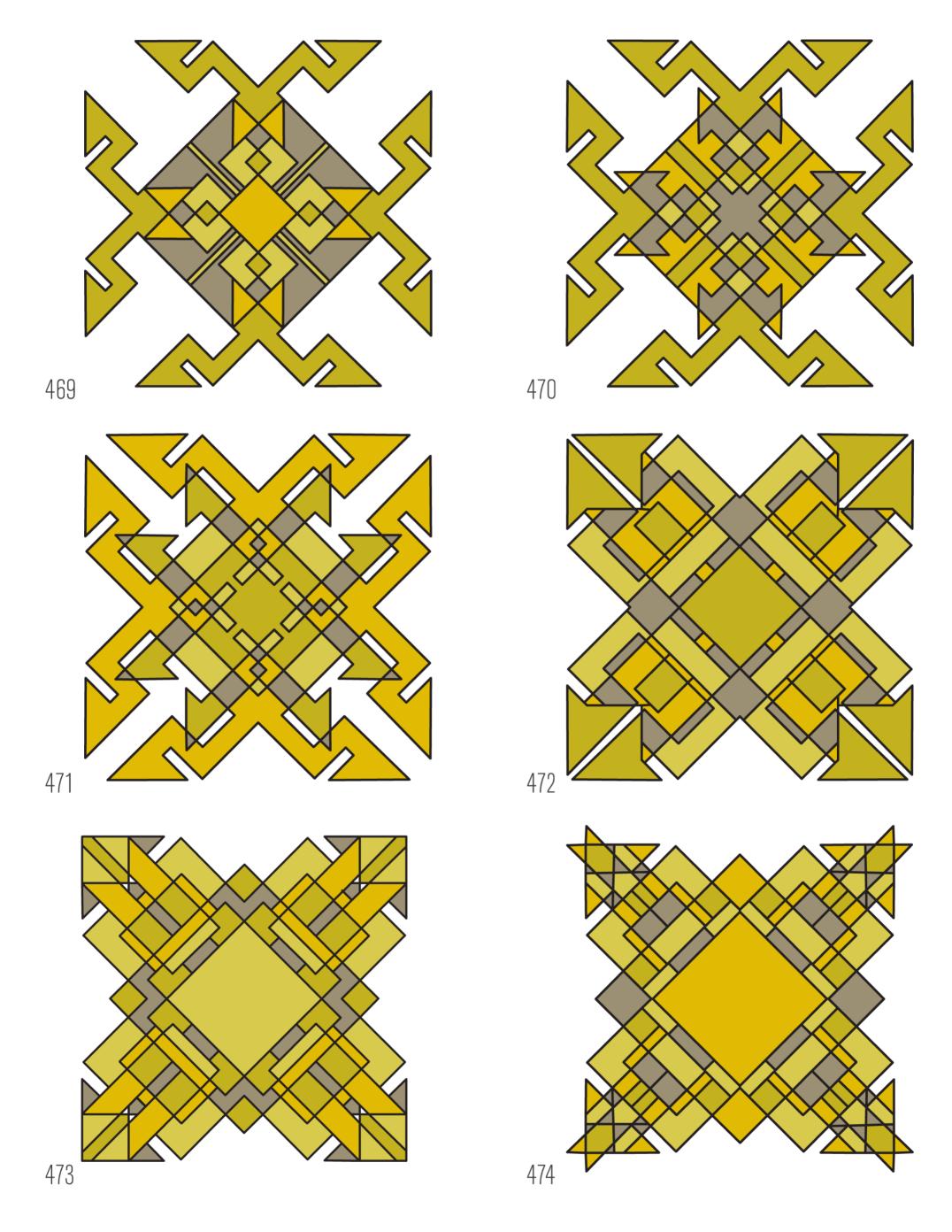




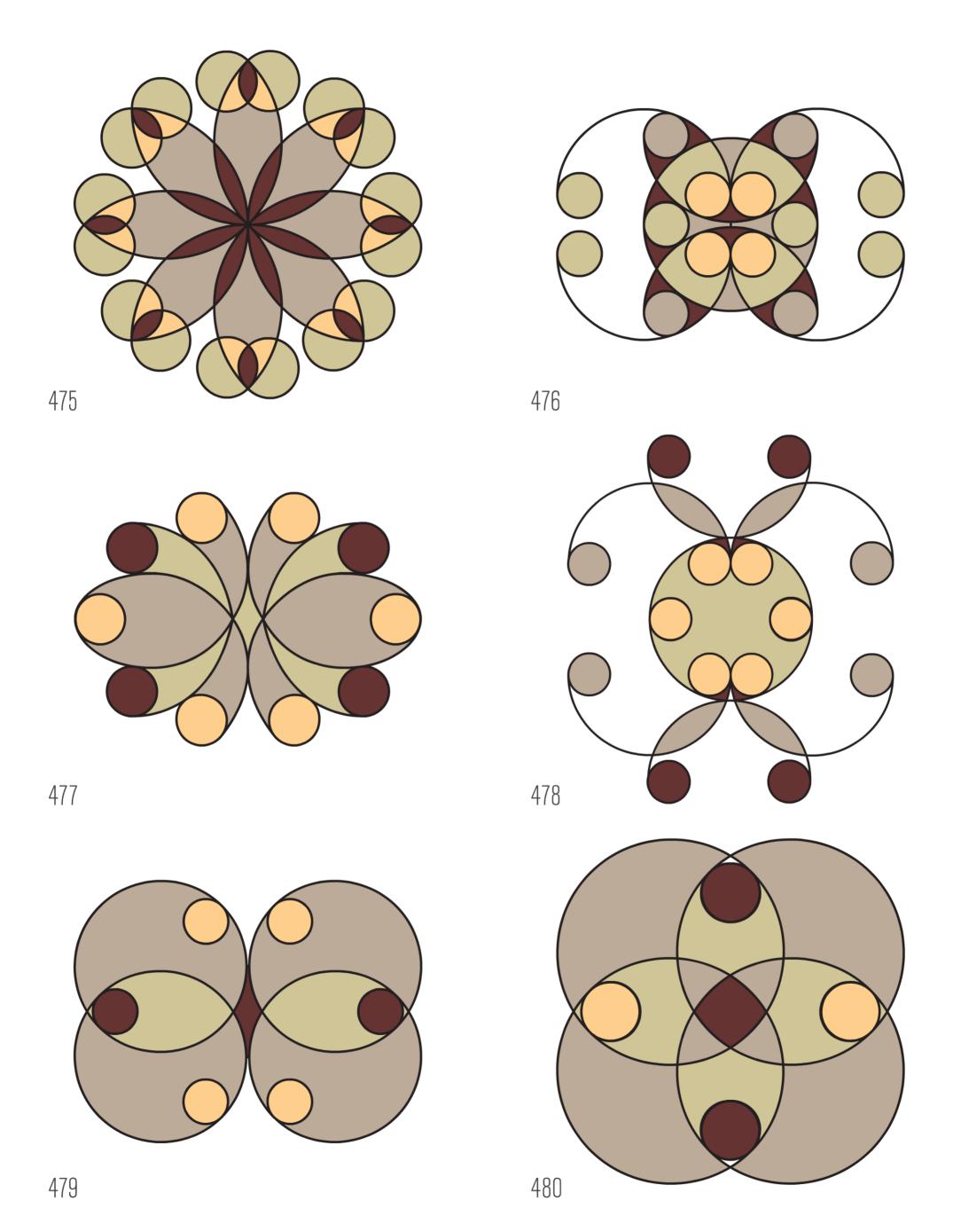




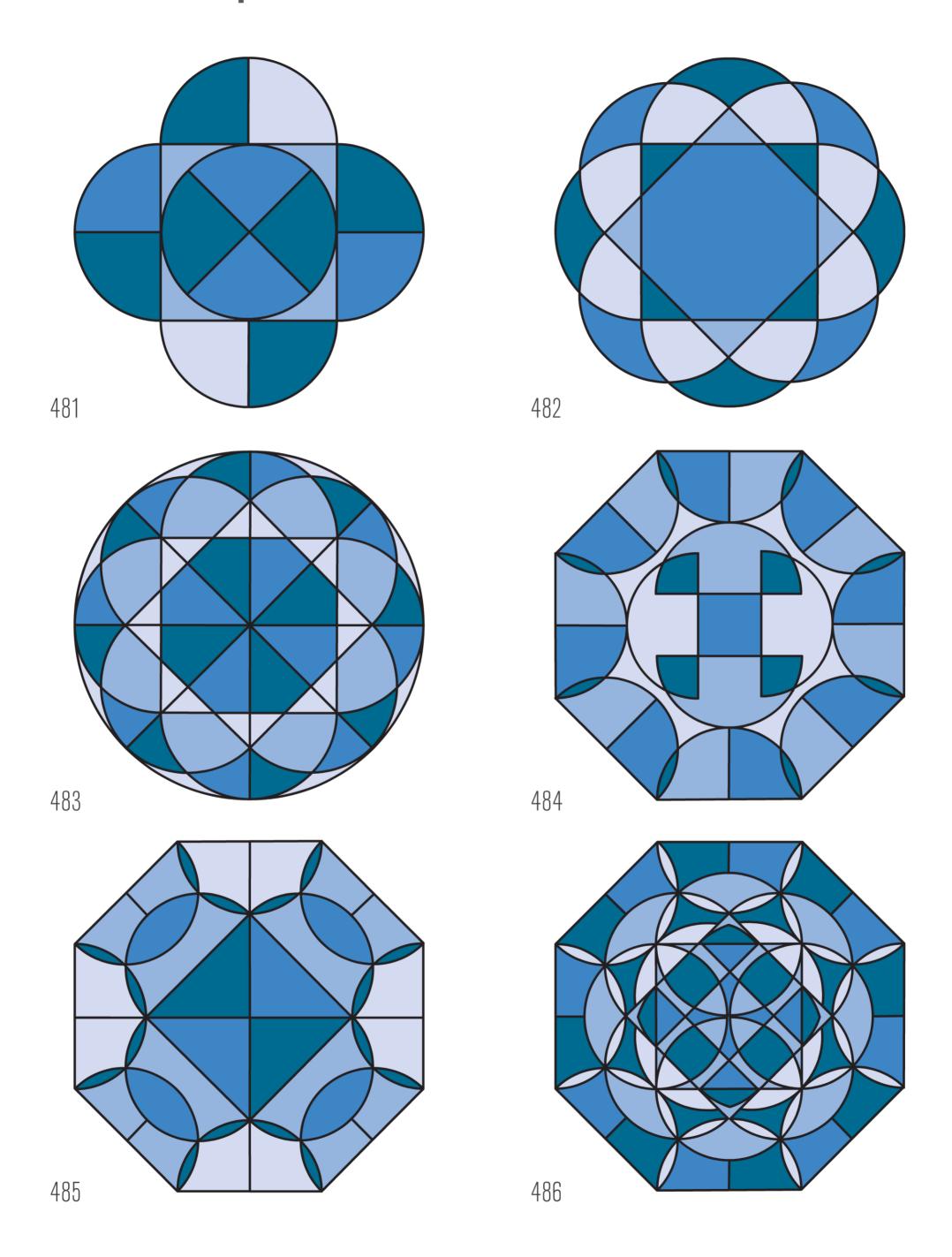
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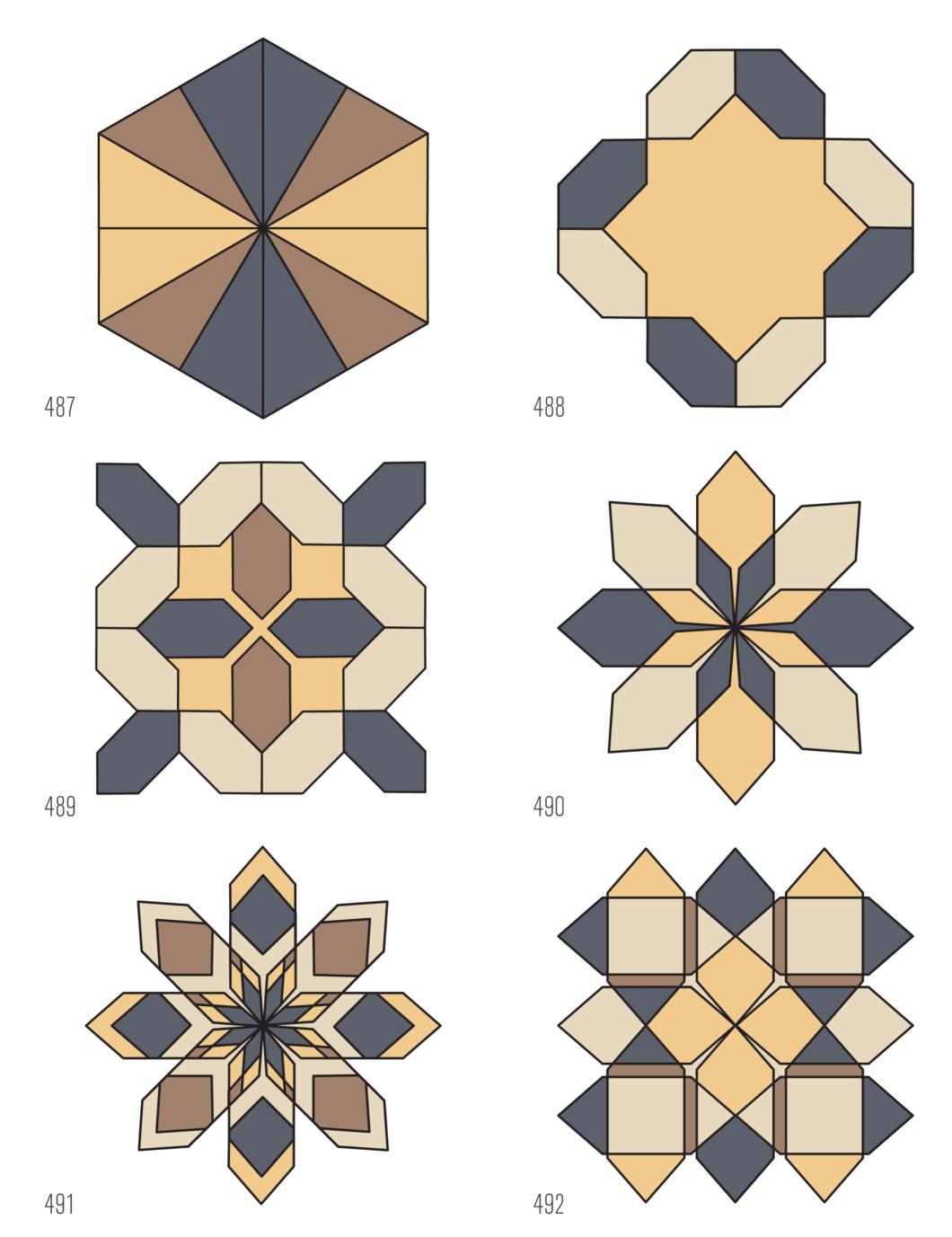
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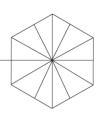


Hemispheres

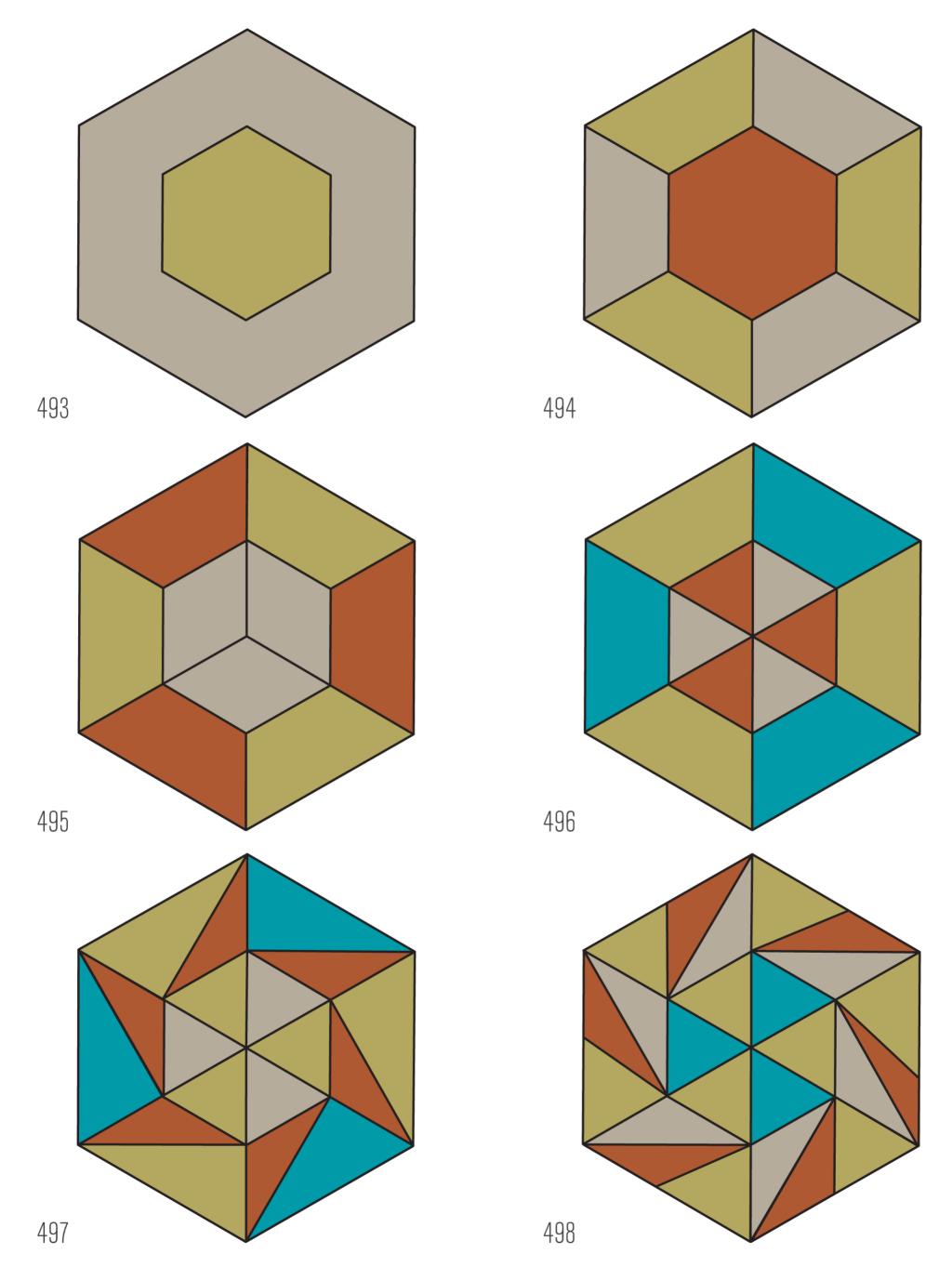


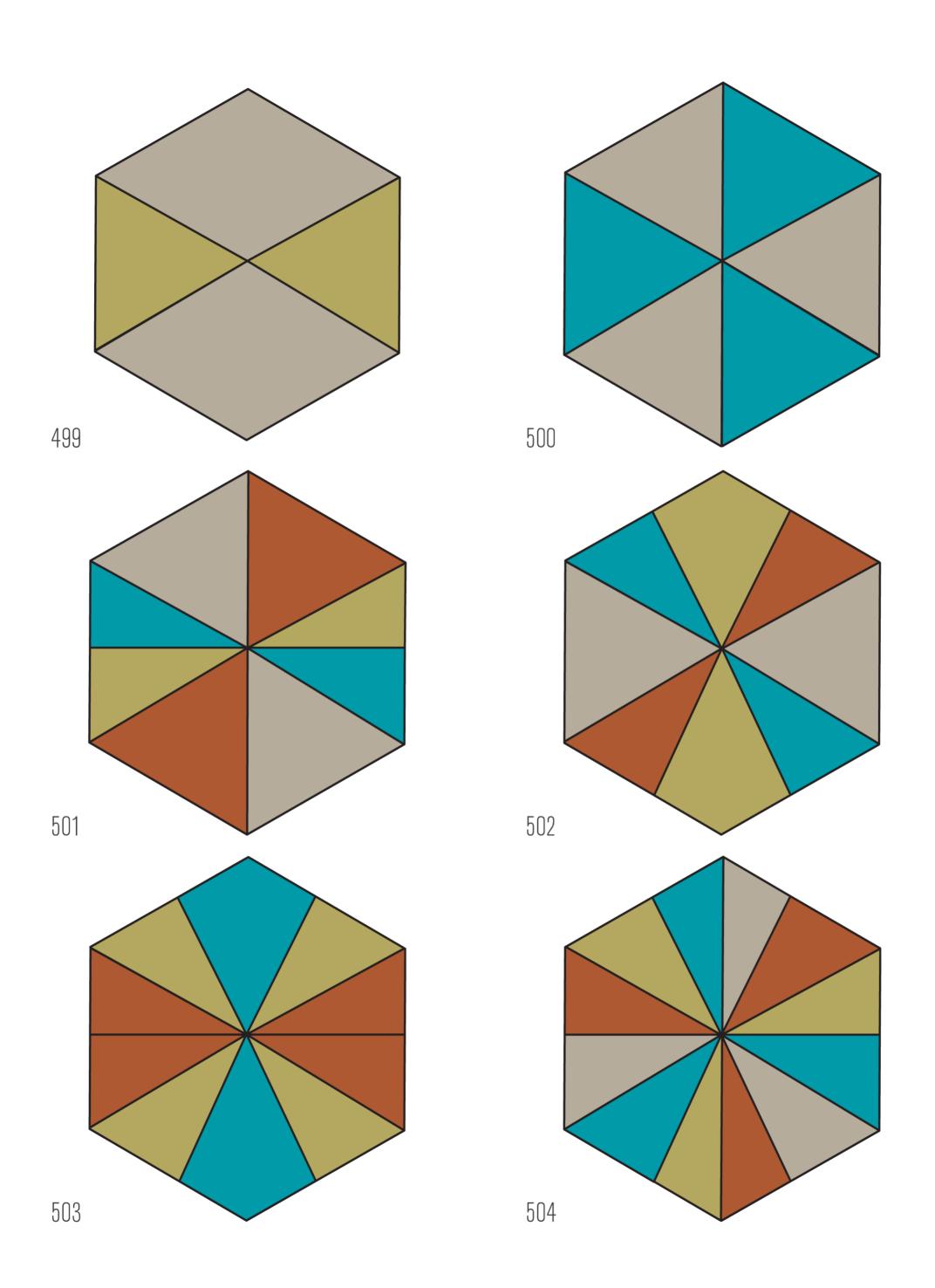
Hexagons



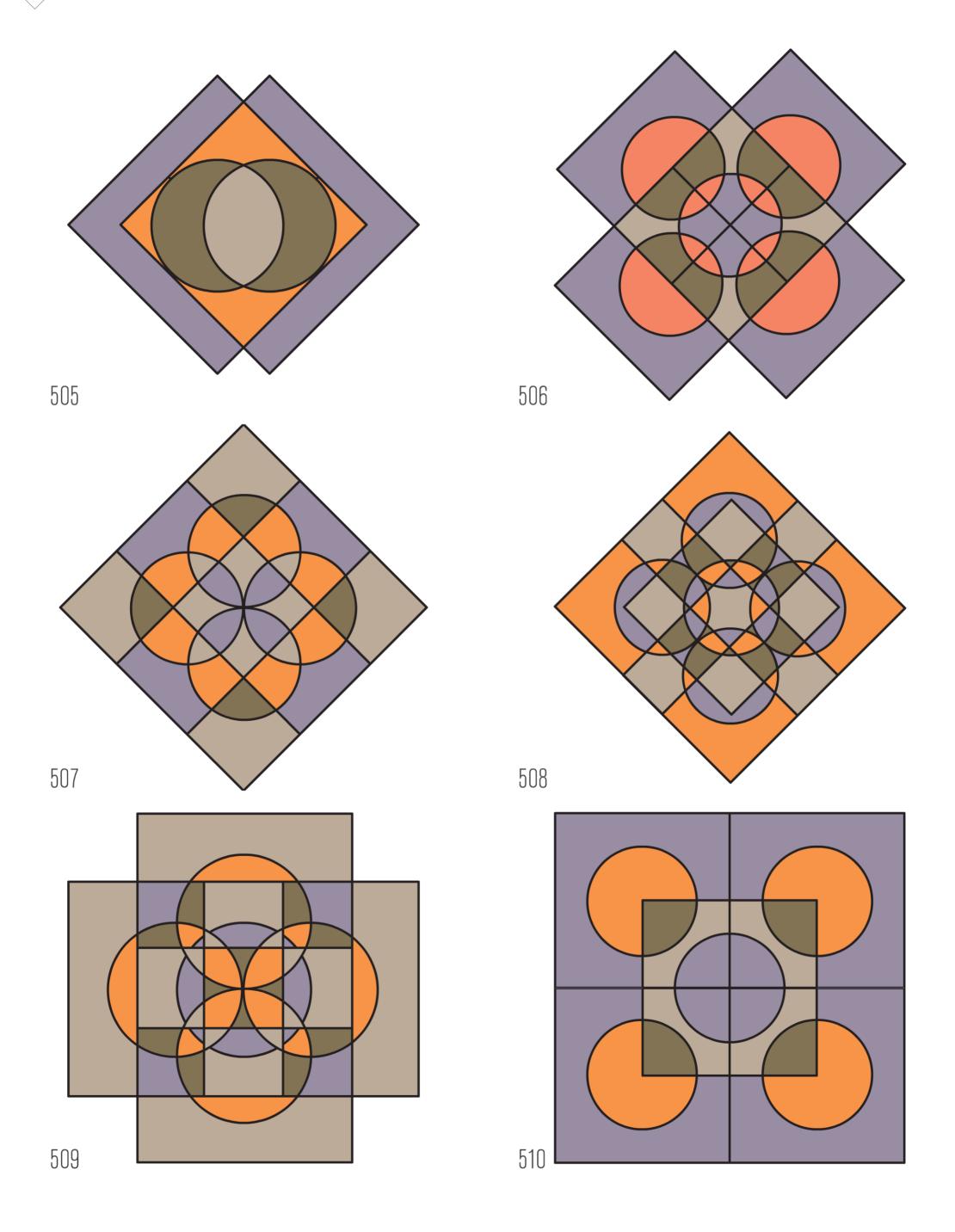


Hexagons Divided

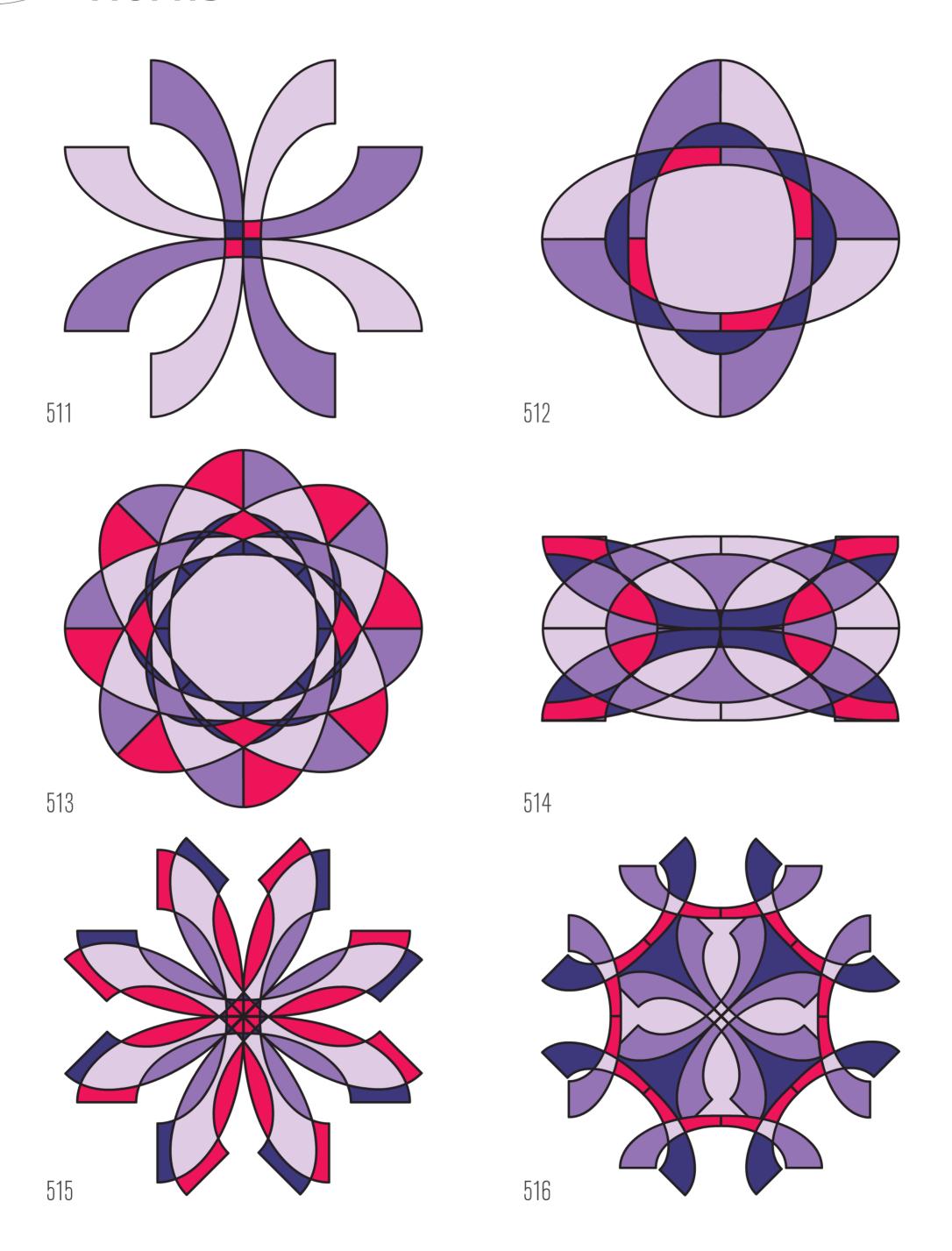




Holes

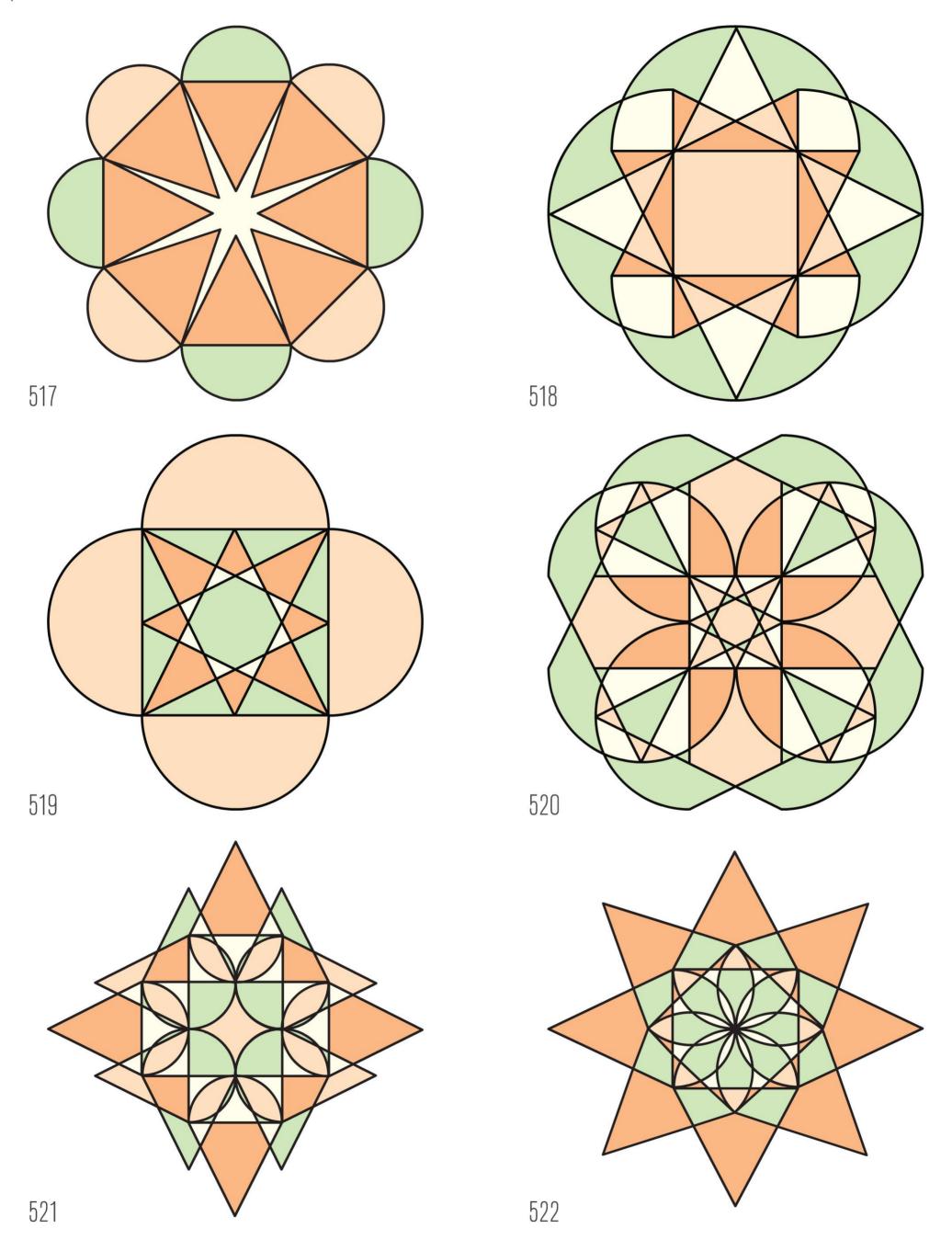


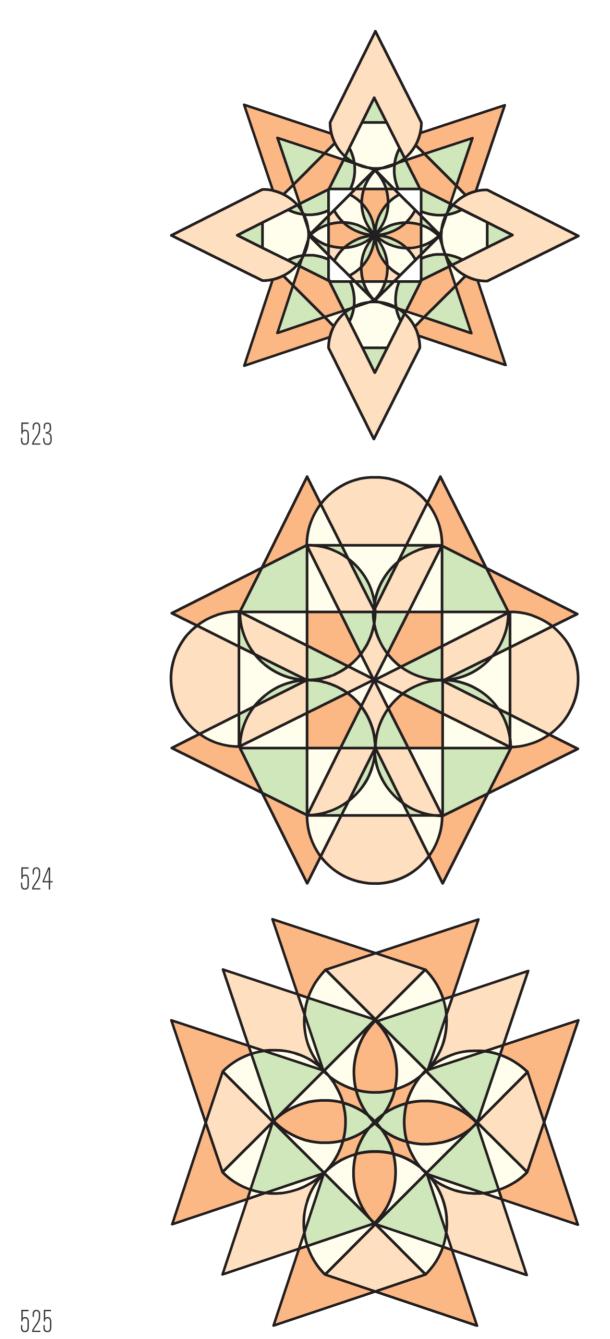
Horns





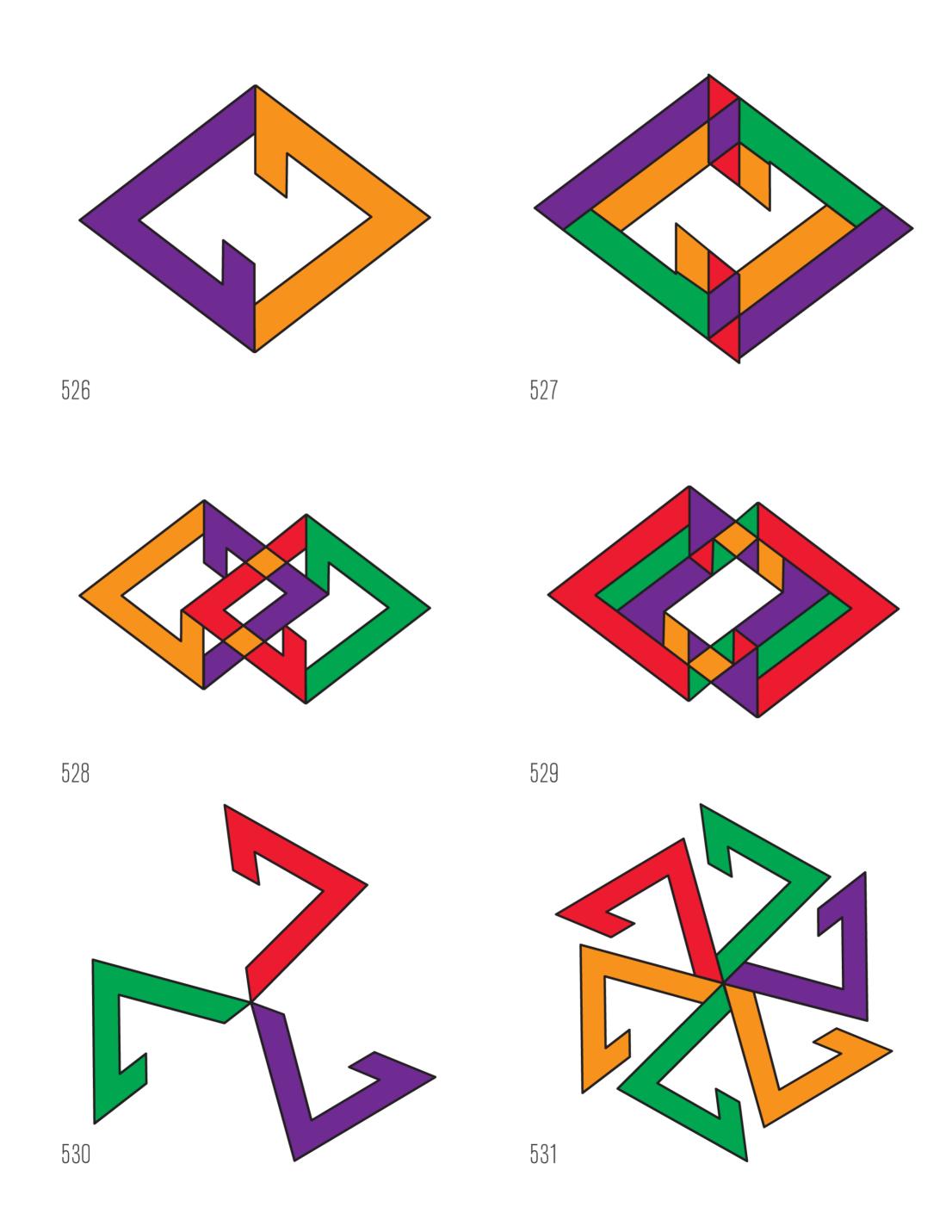
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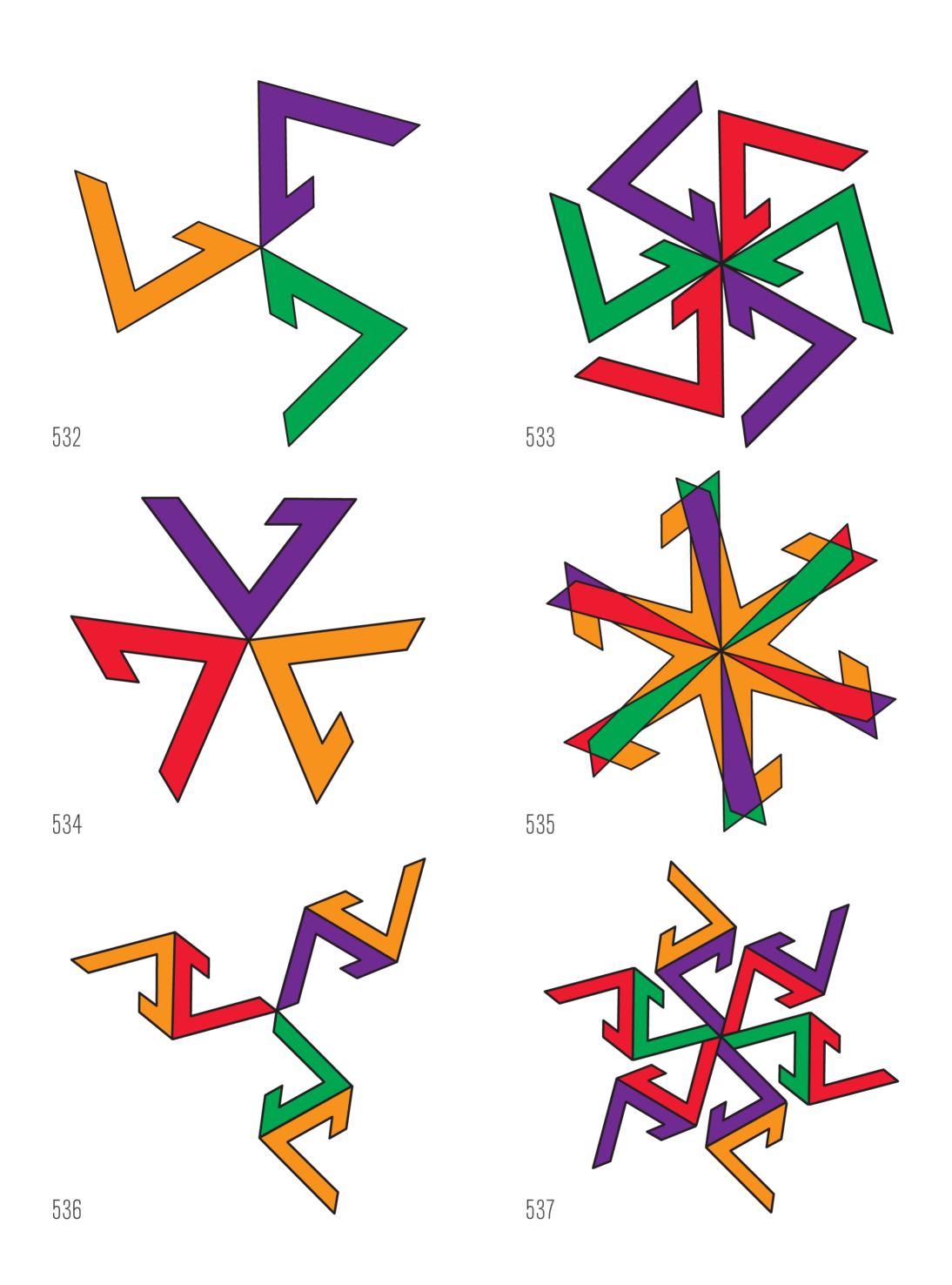




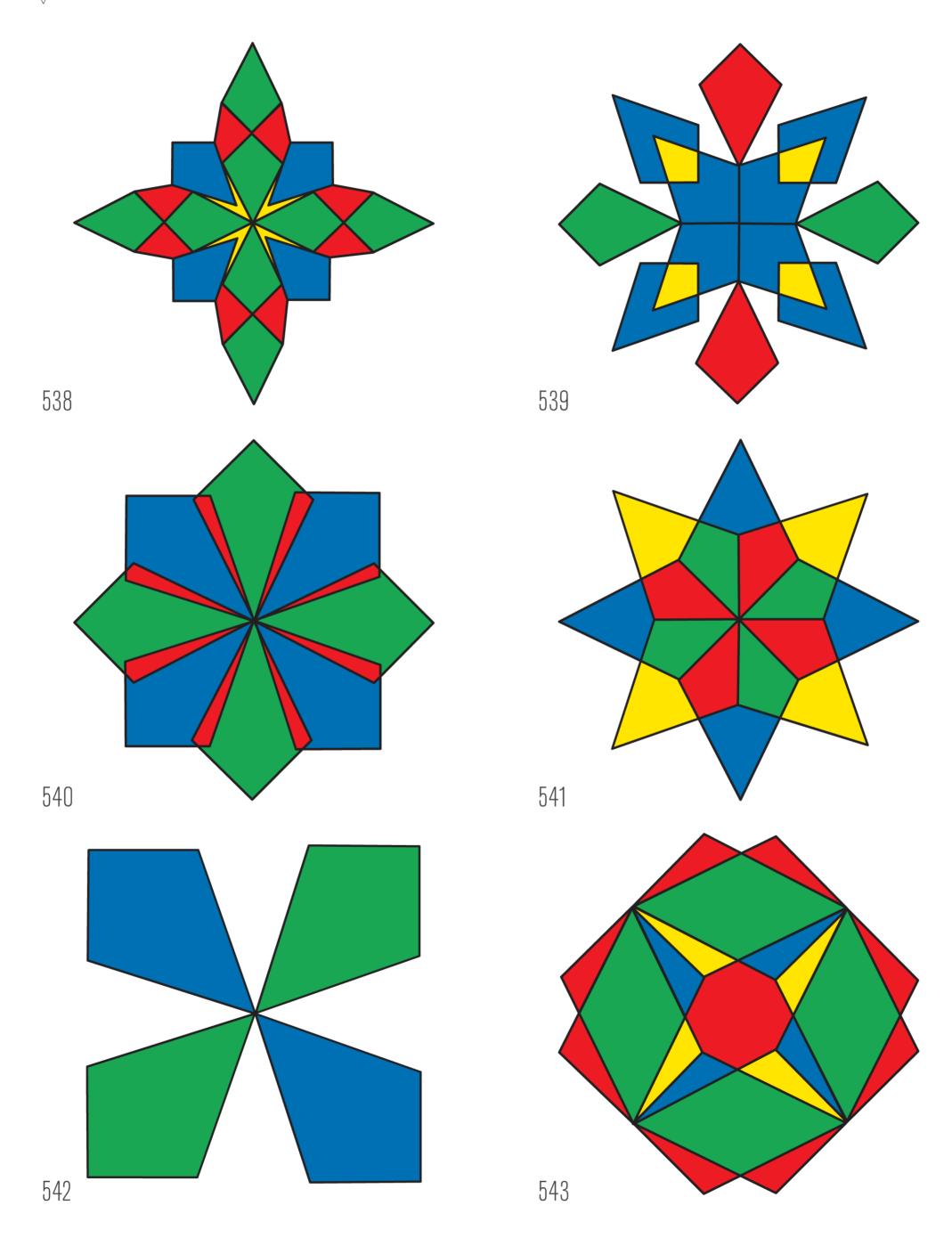


Kinked Chevrons

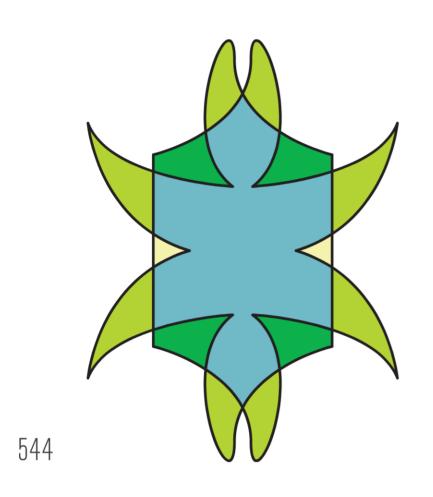


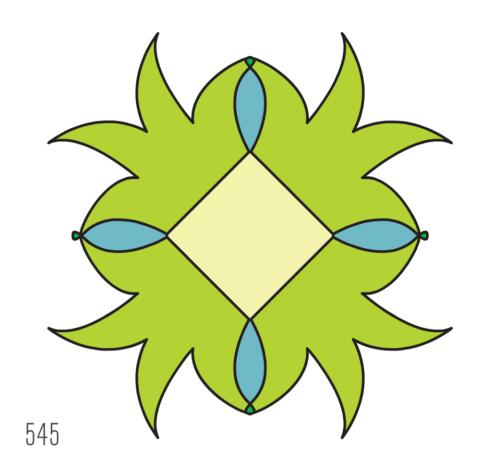


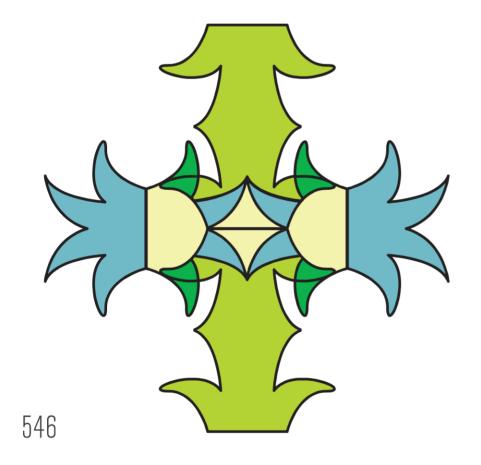
Kites

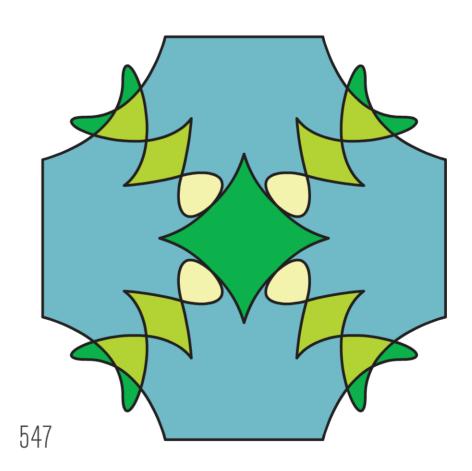






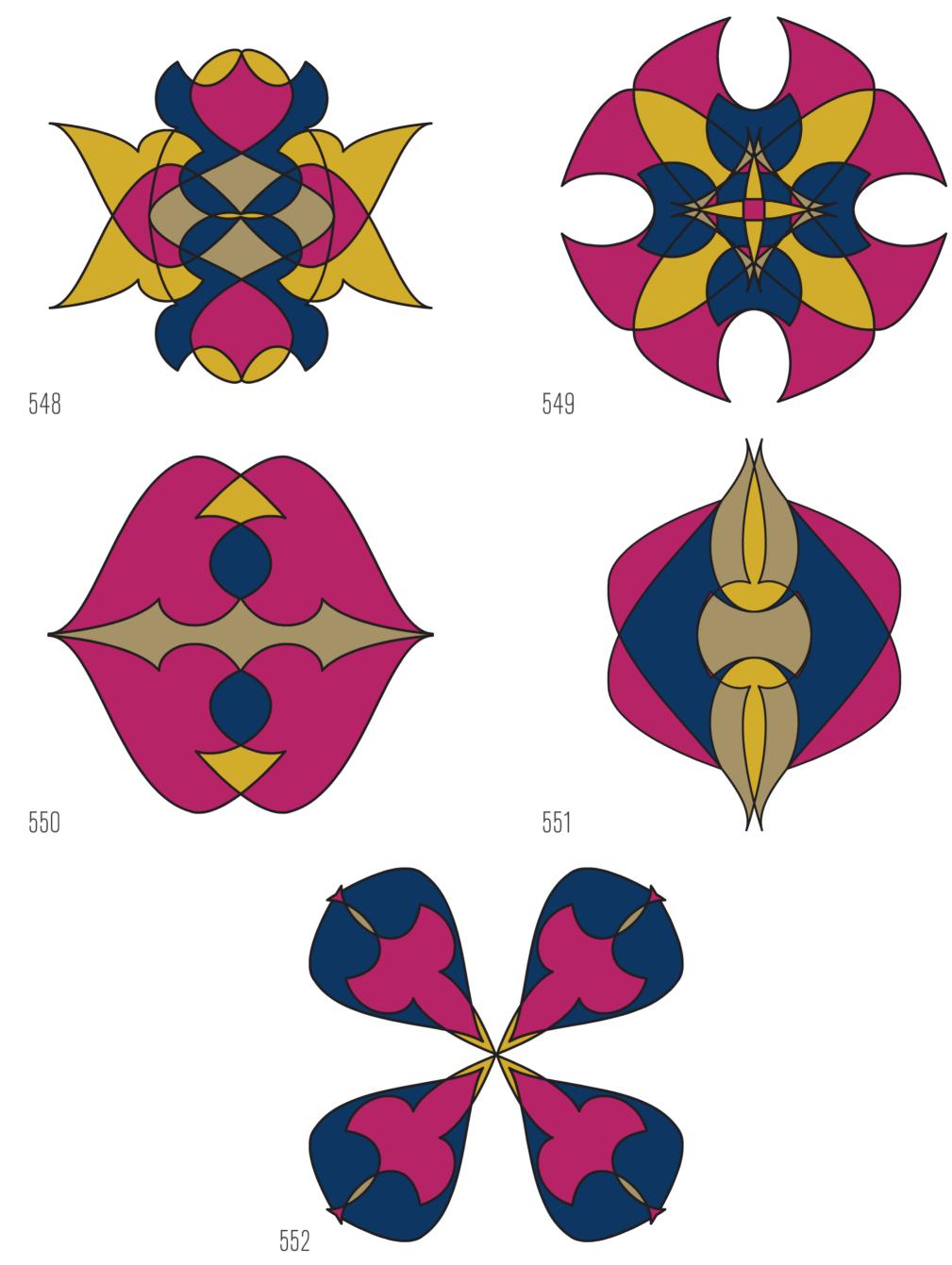


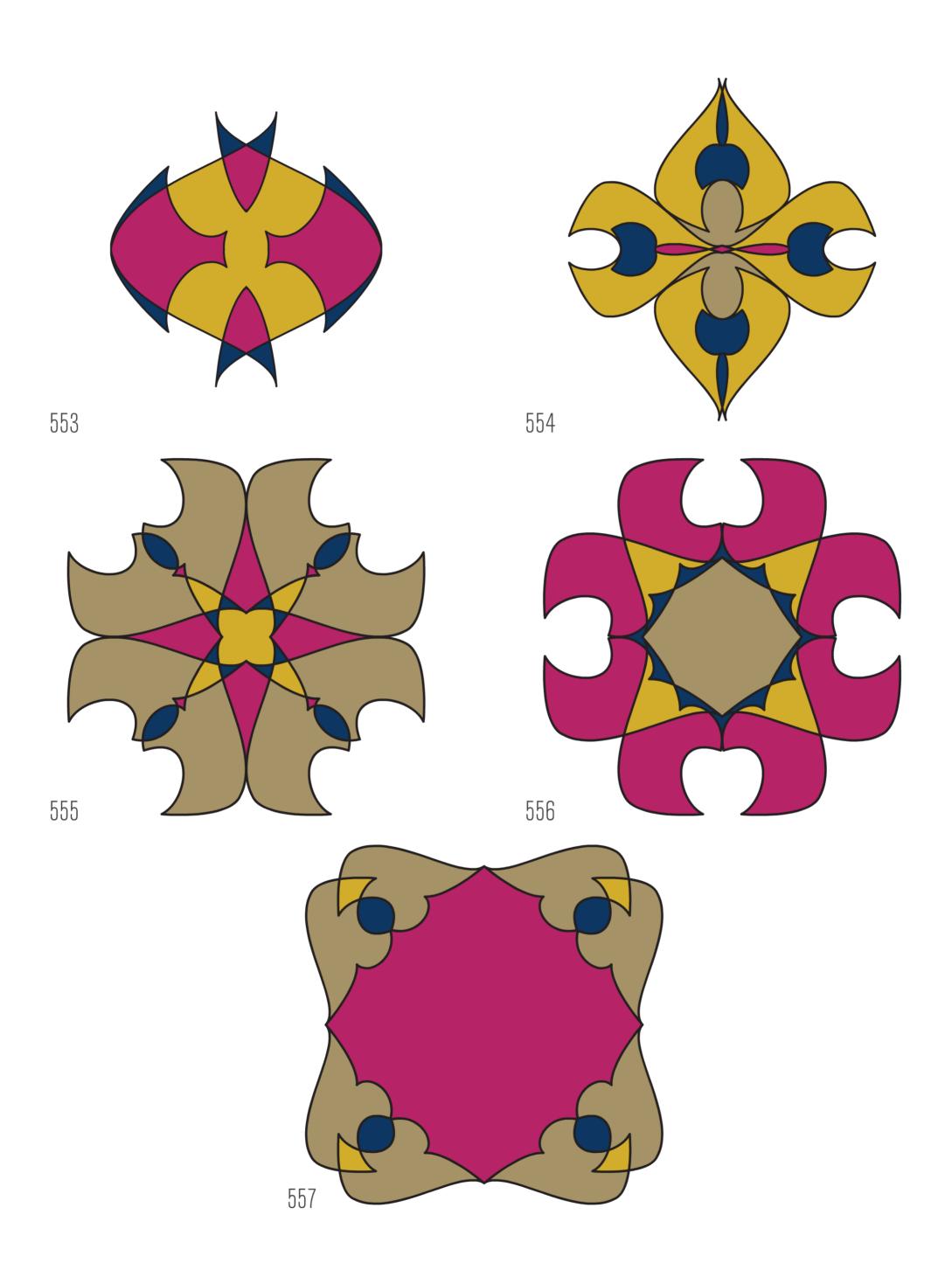




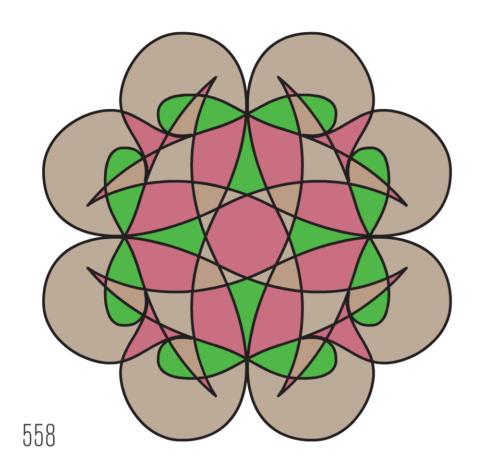


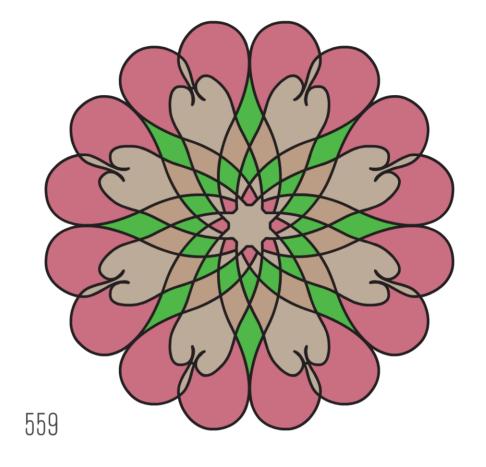
Leaf Petal 2

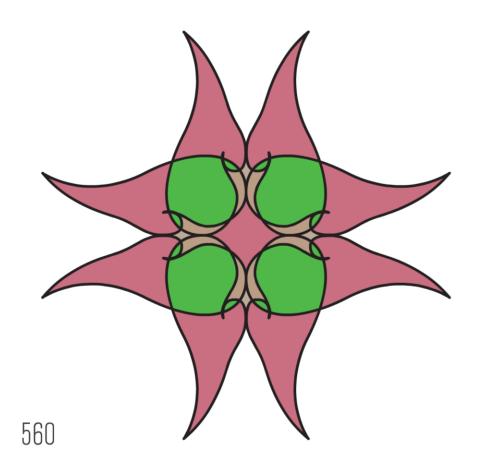


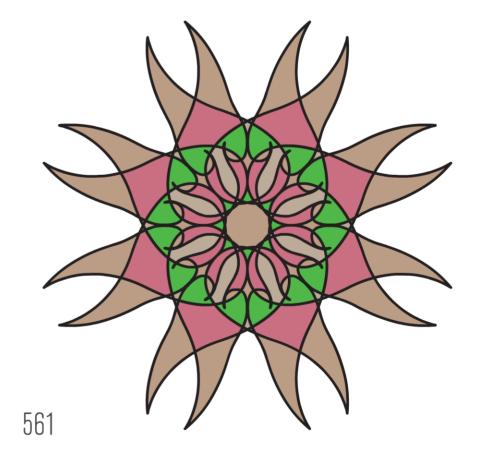


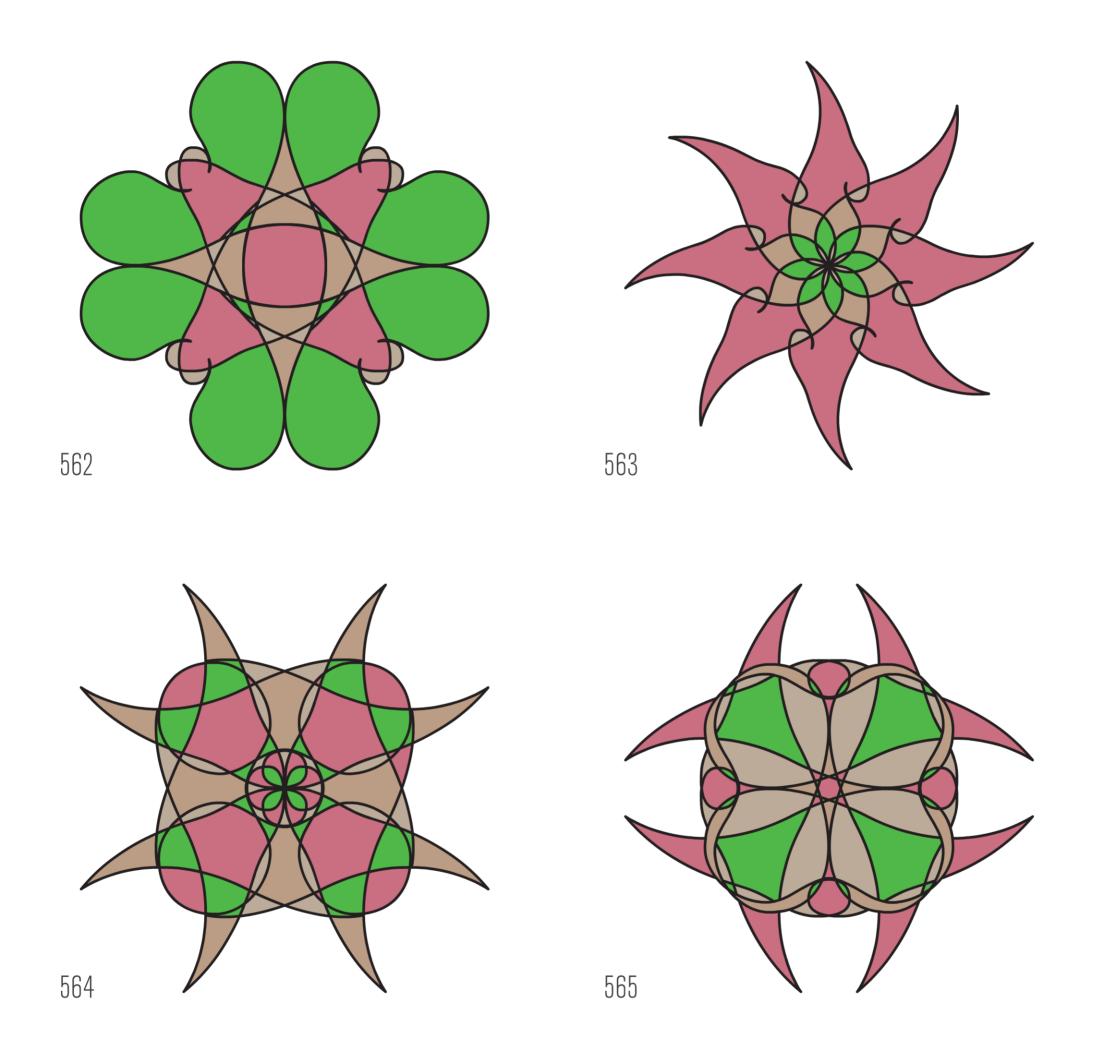
Leaf Petal 3



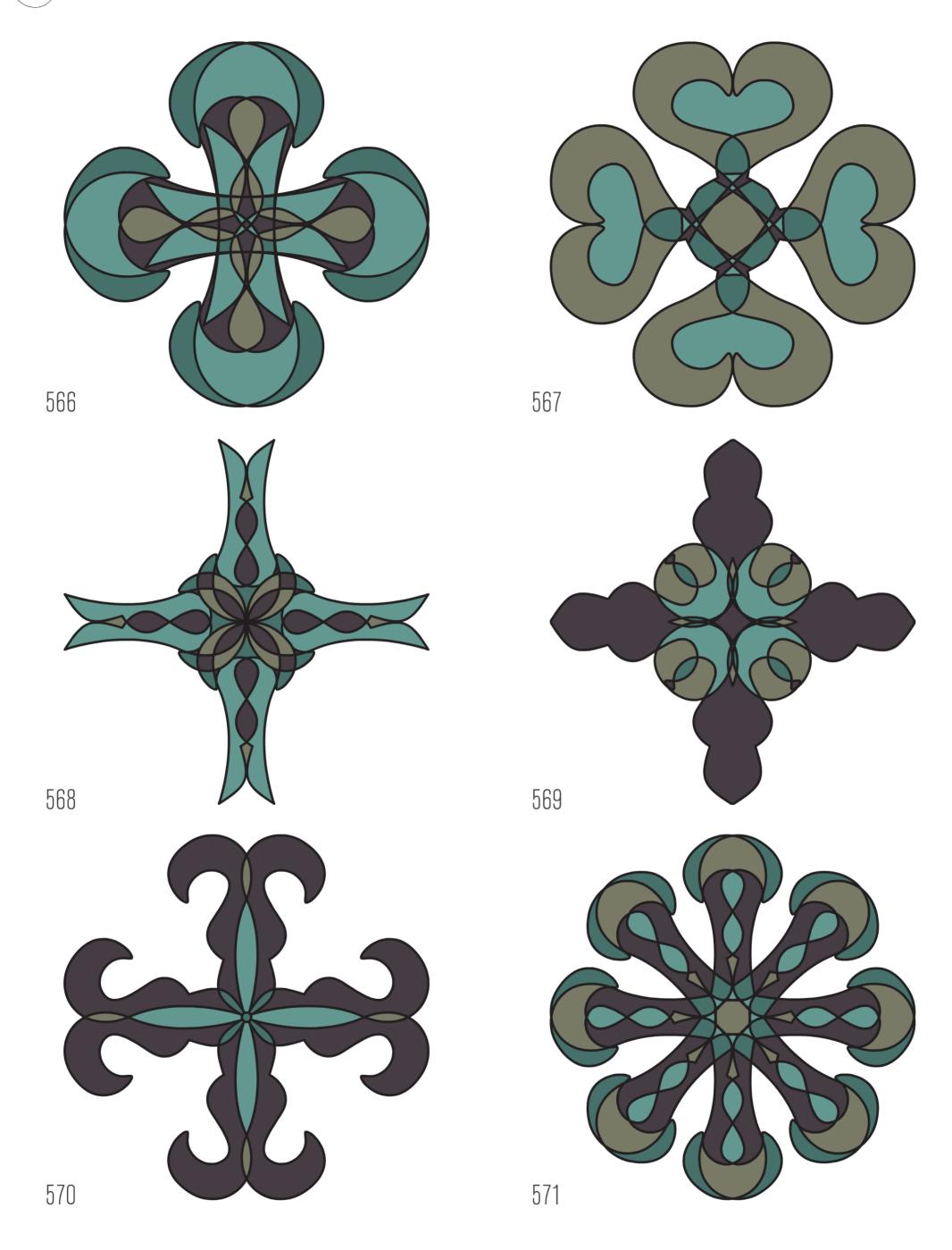


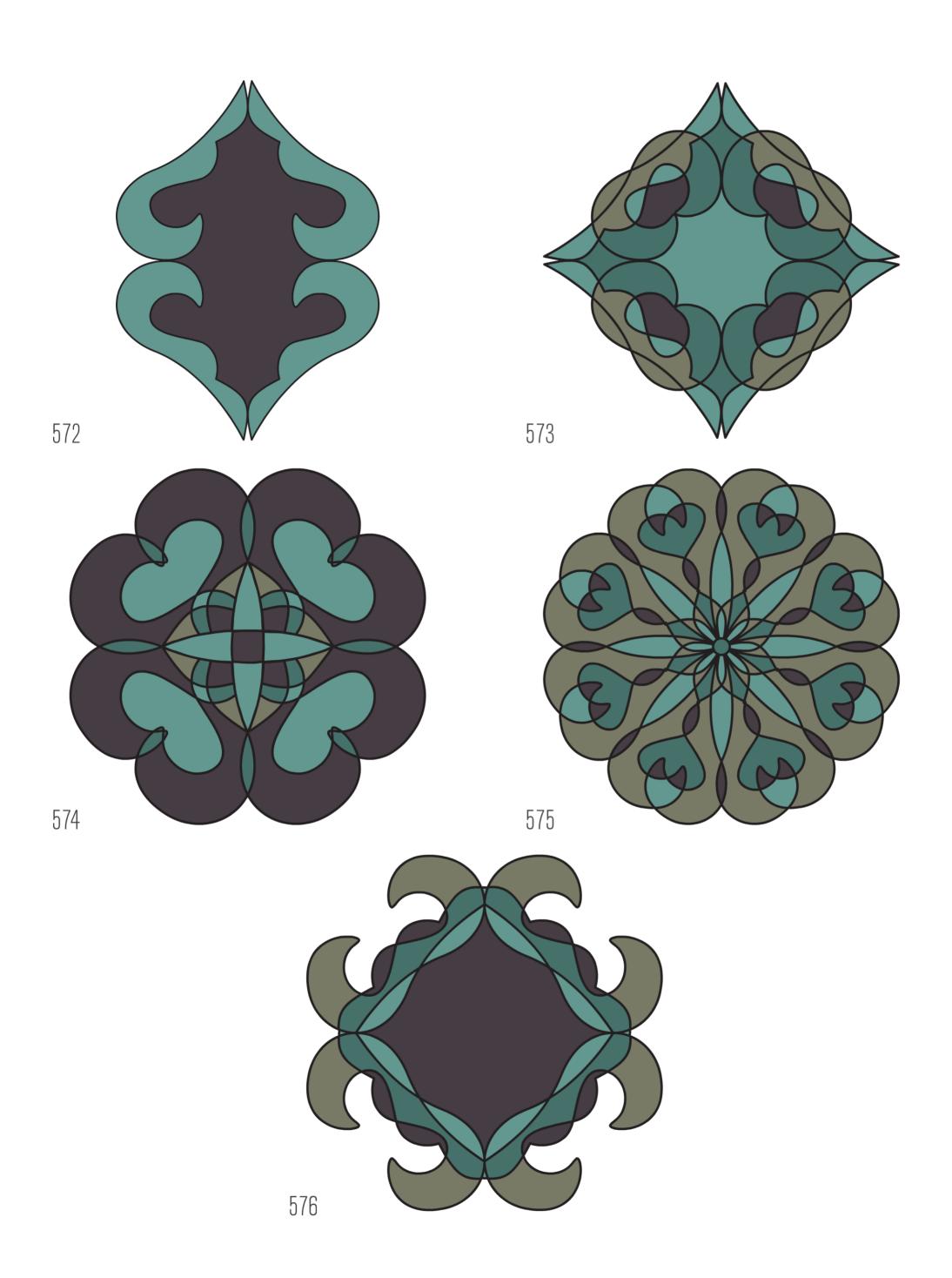




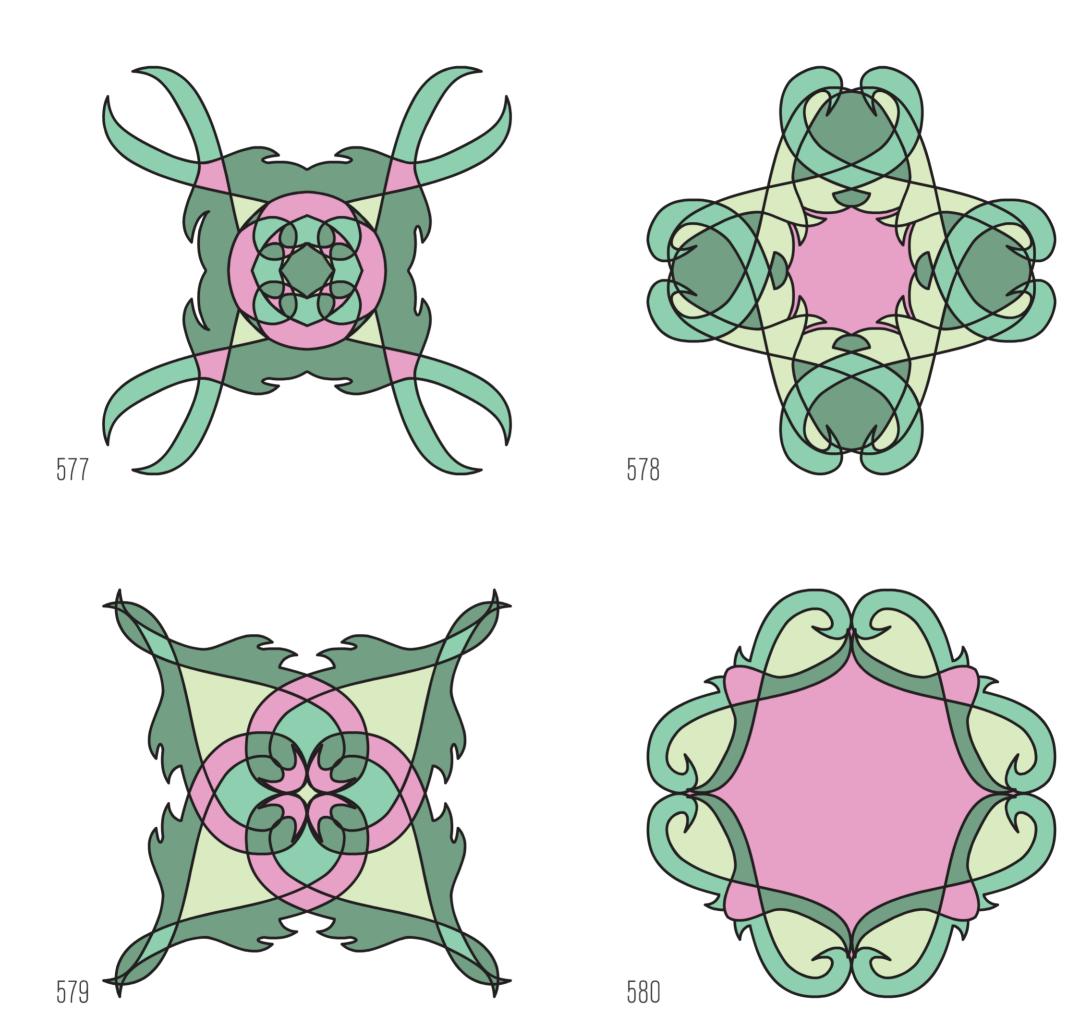


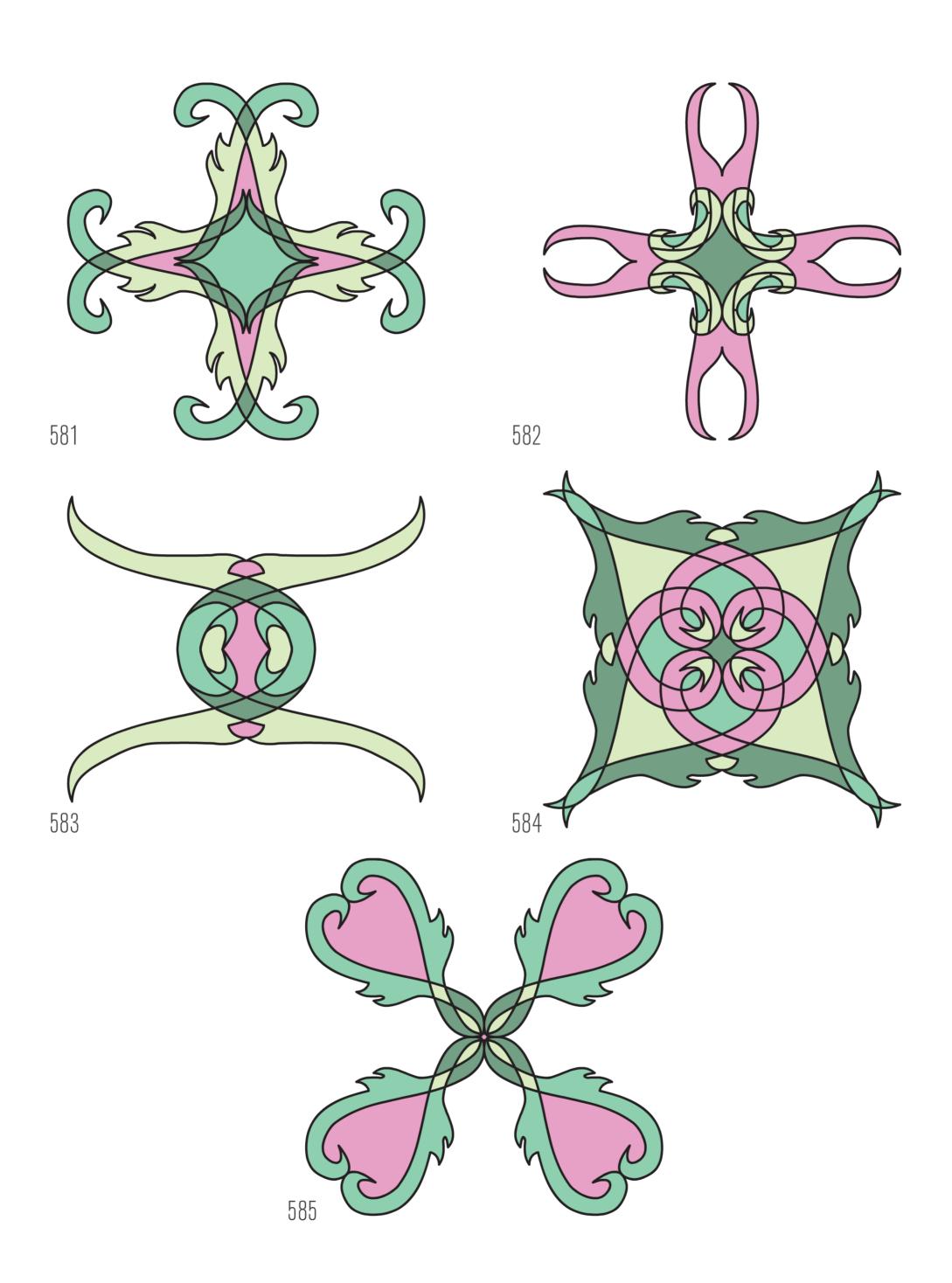
Leaf Petal 4



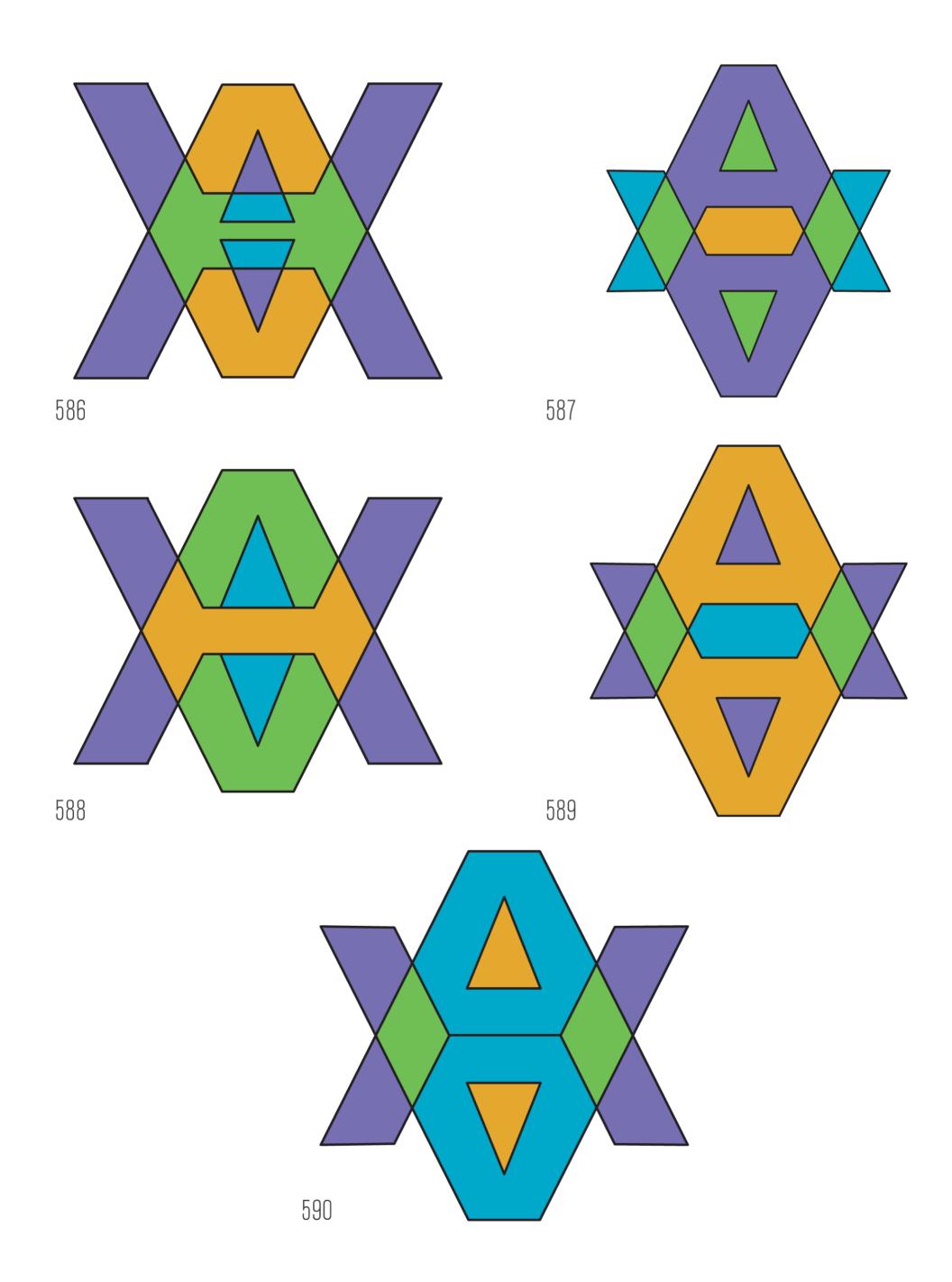


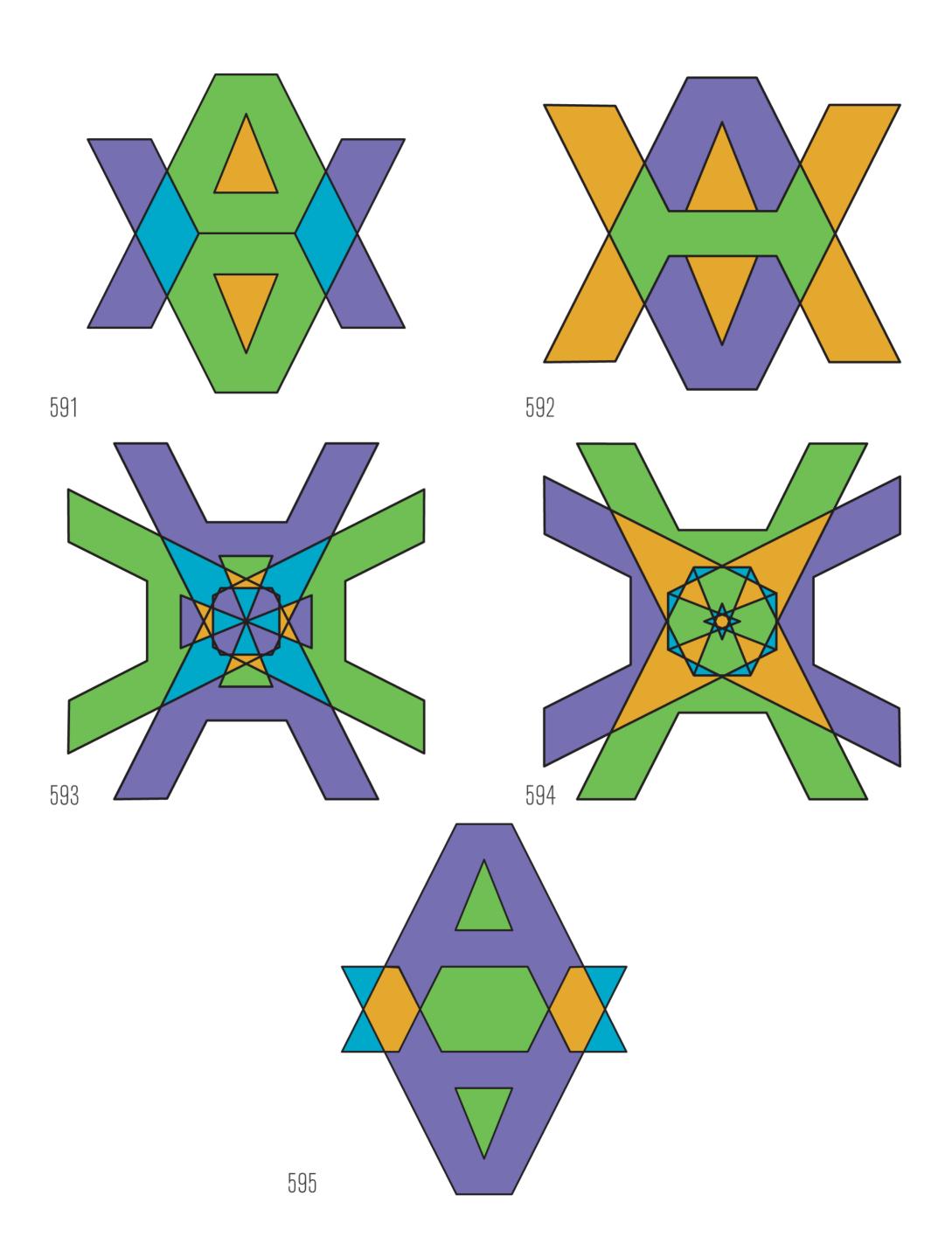
Leaf Vine



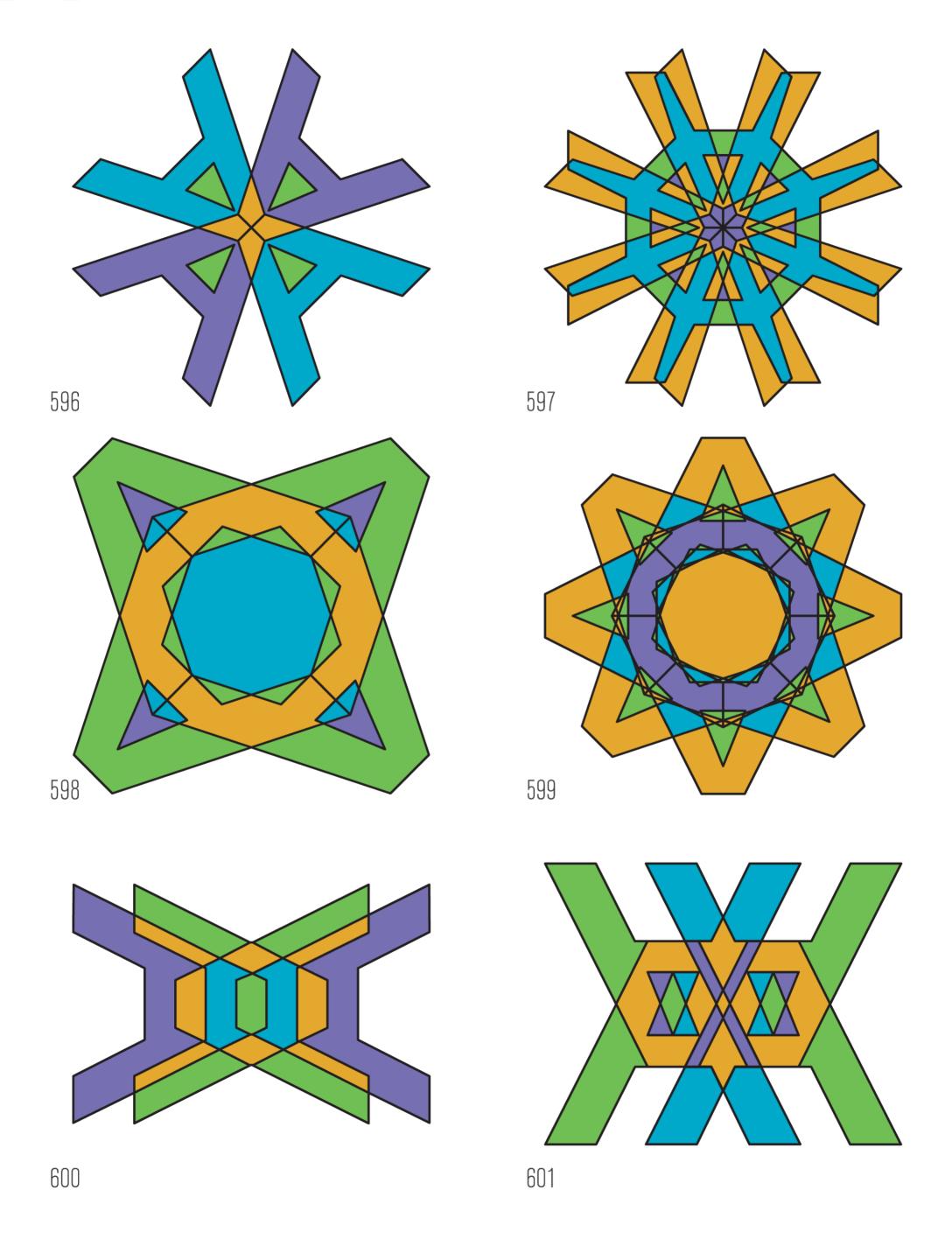


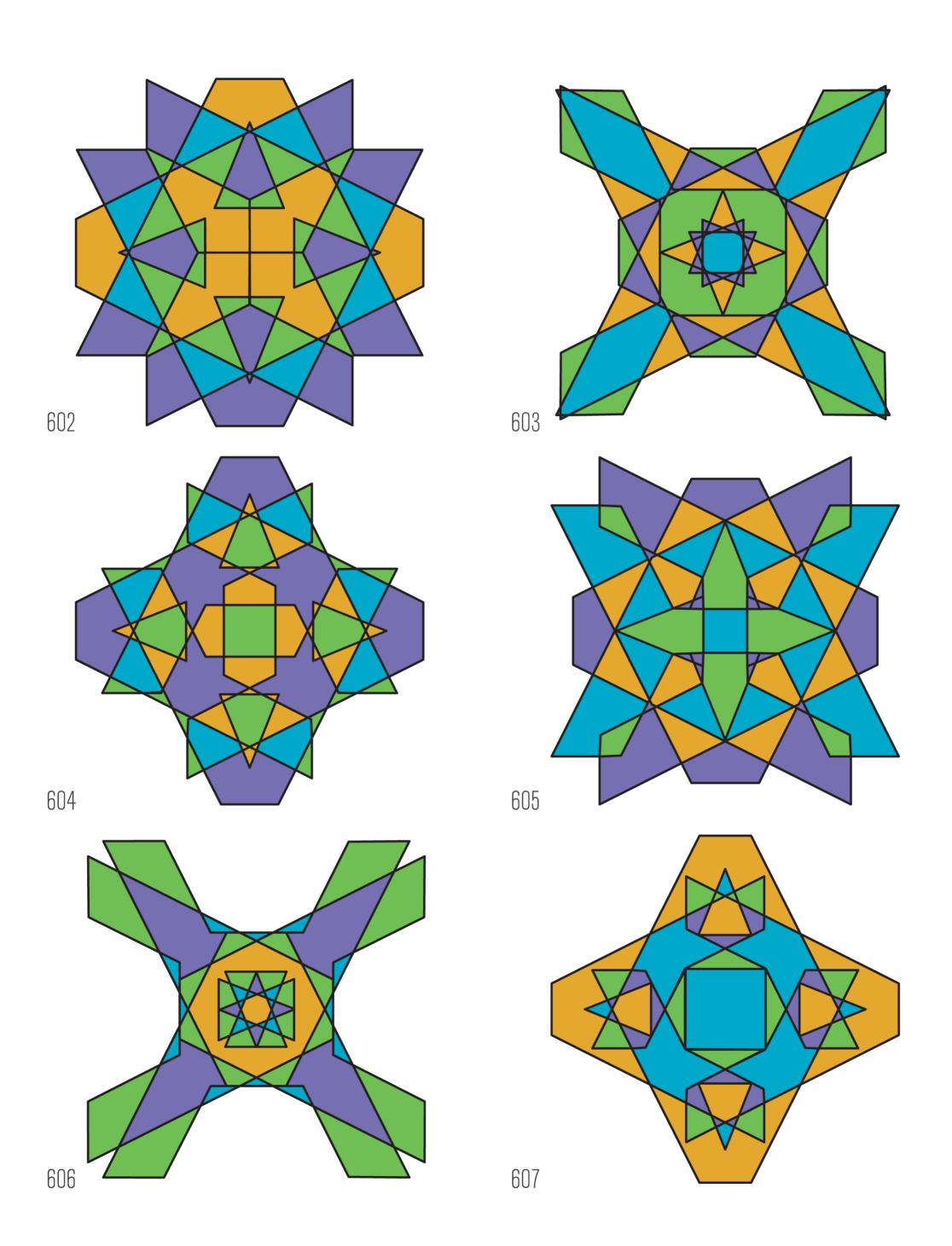




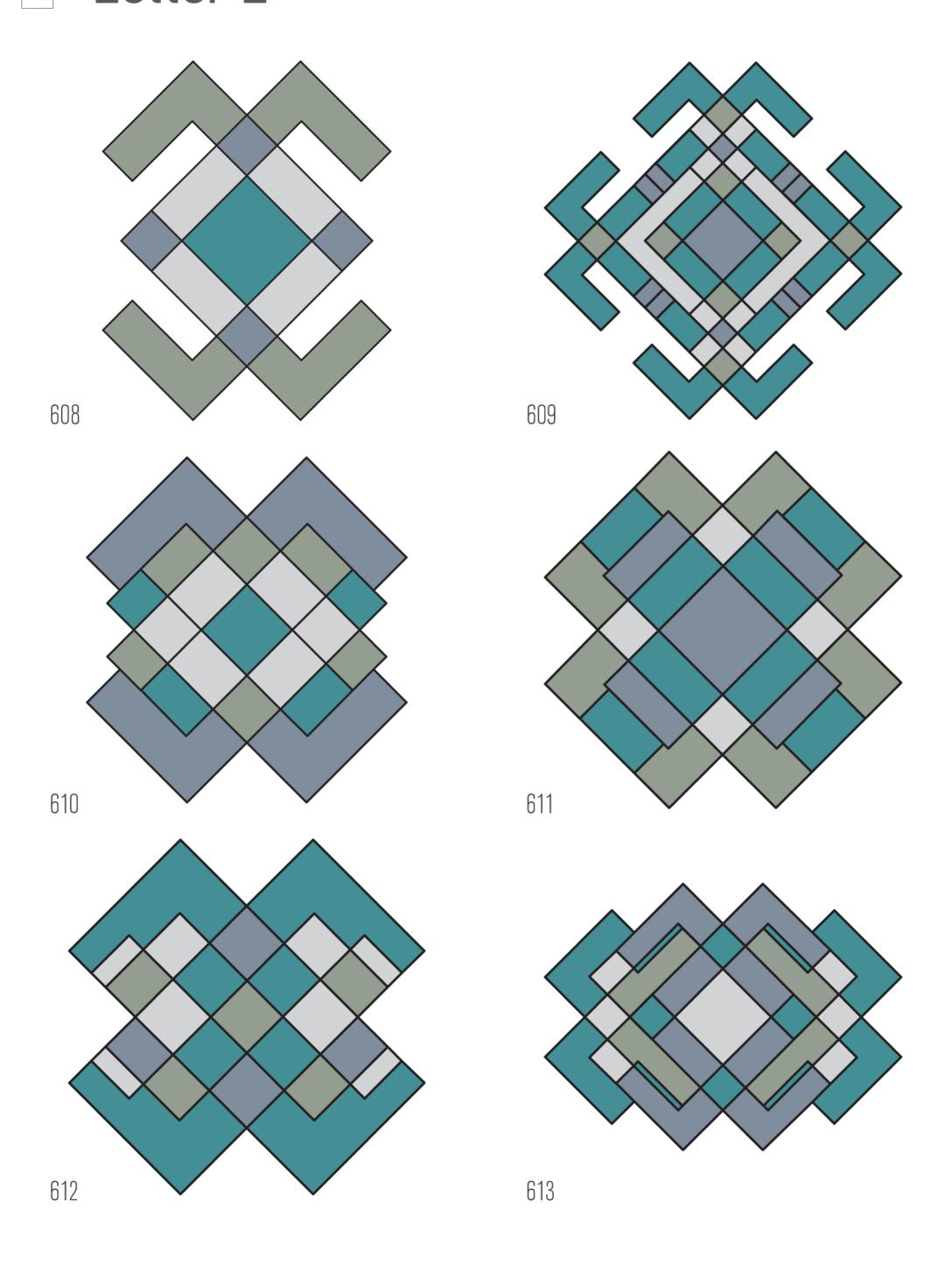


Letter A

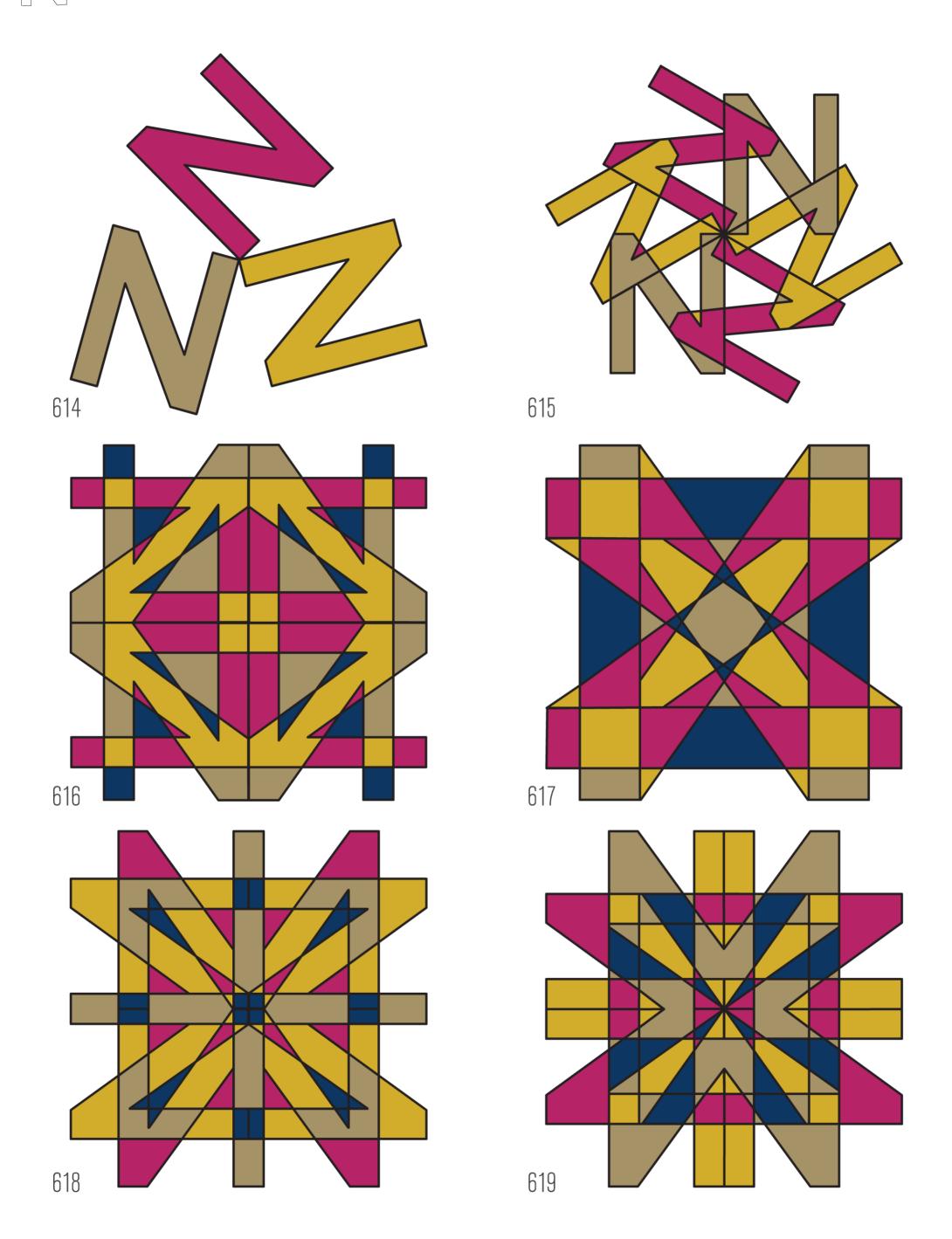




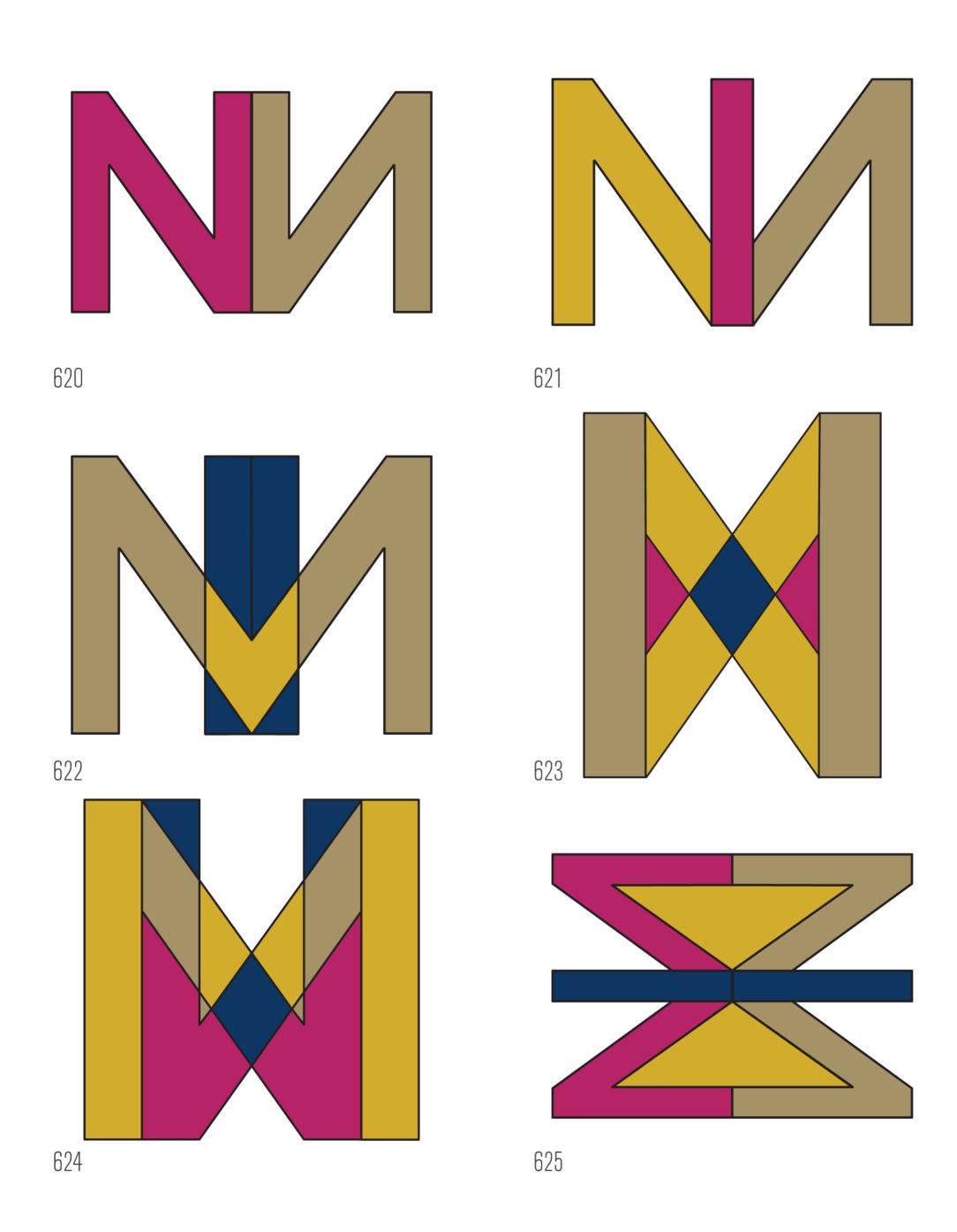
Letter L



Letter N

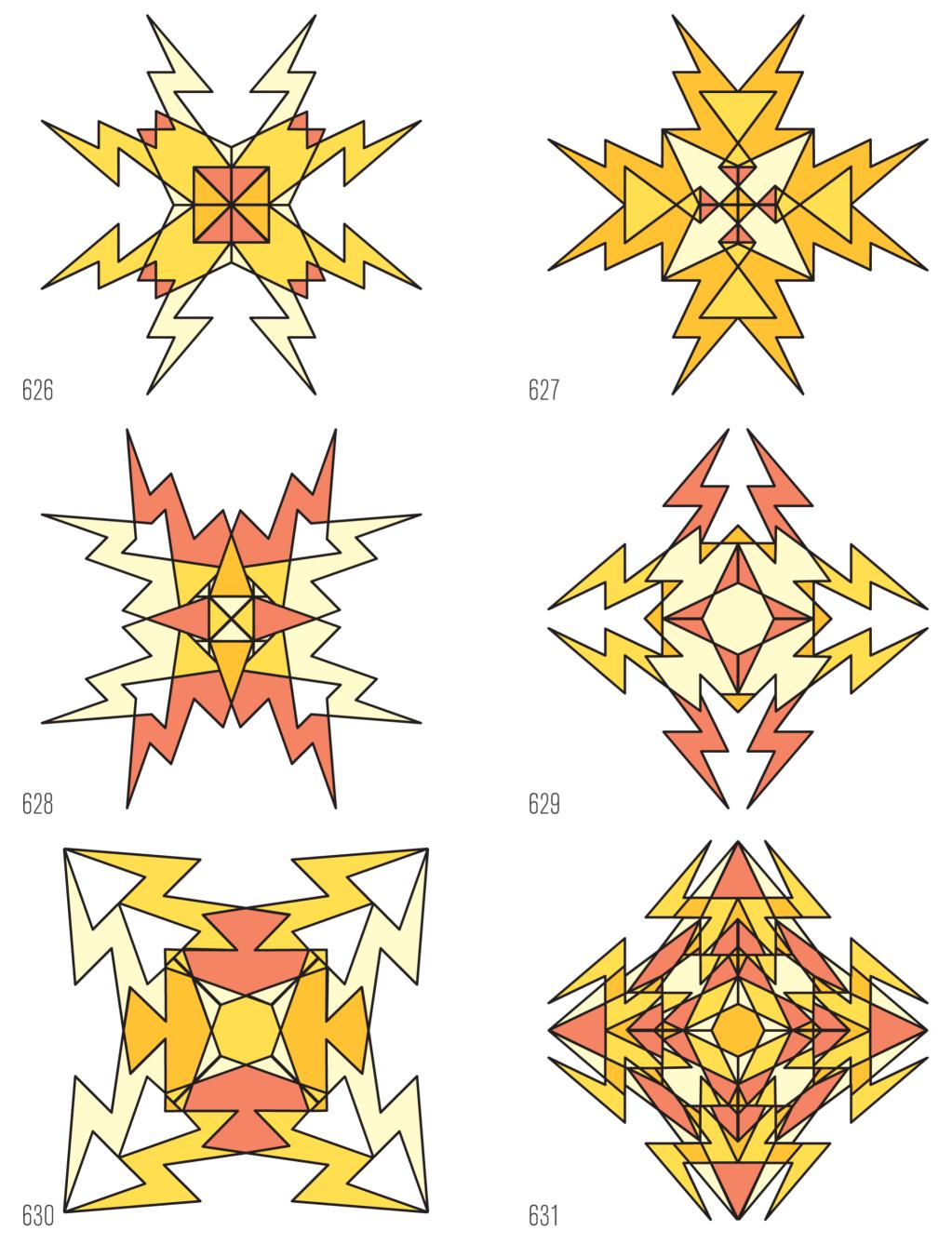


Letter N

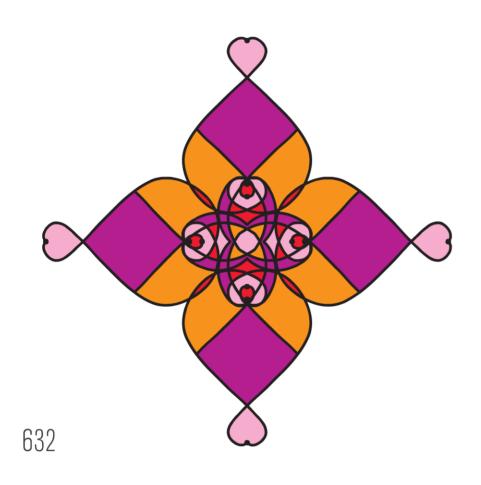


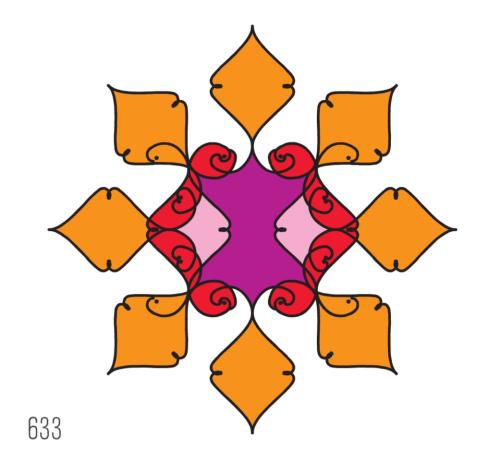


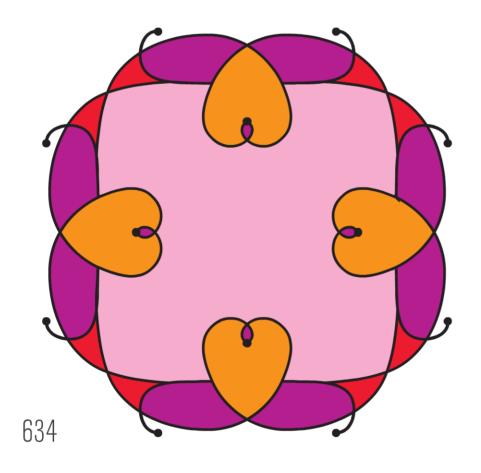
Lightning Bolt

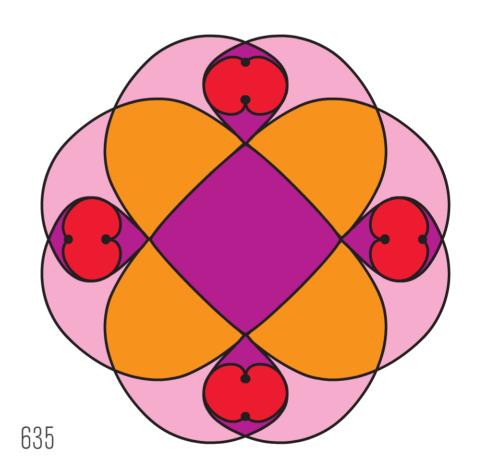


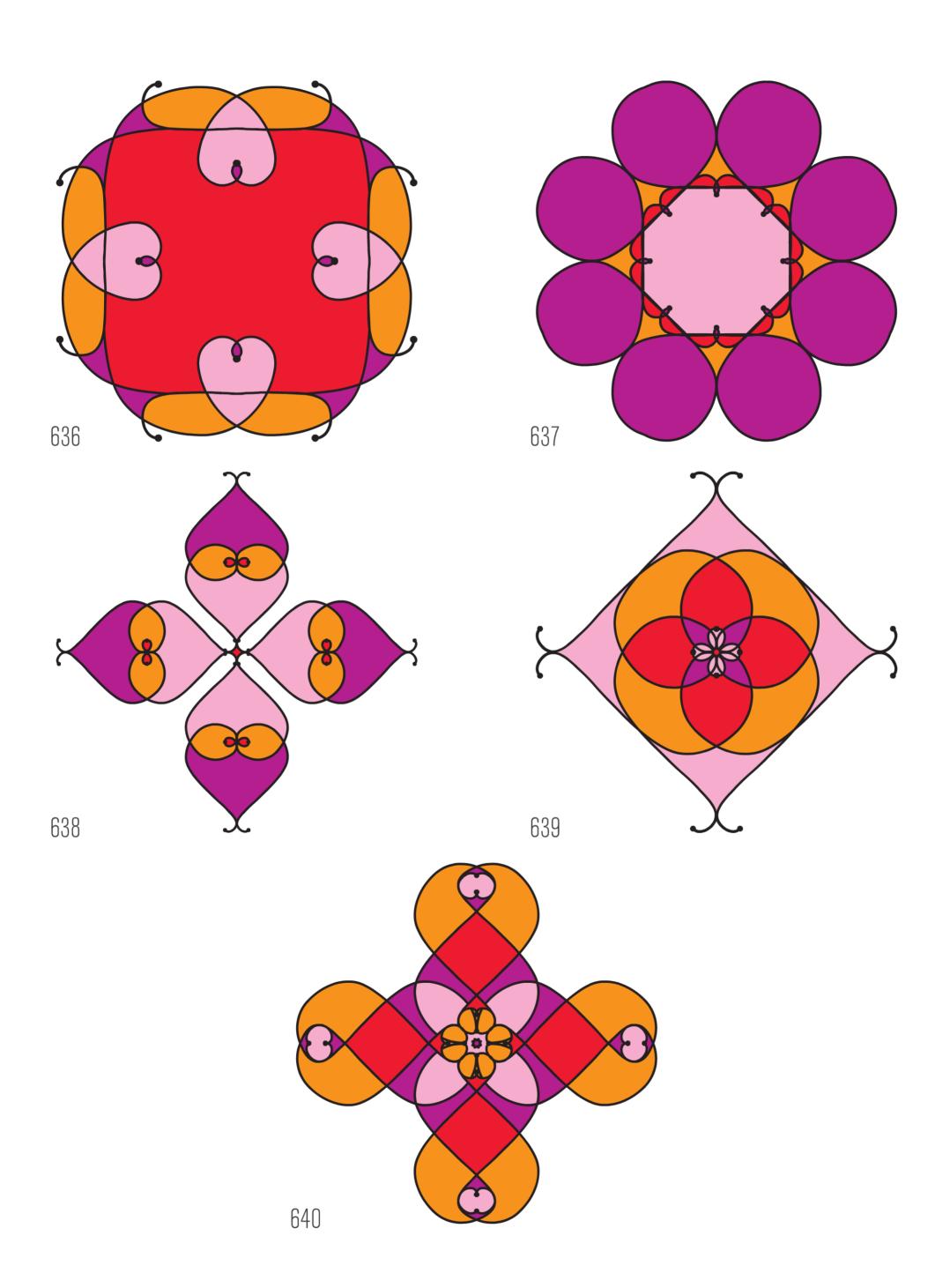




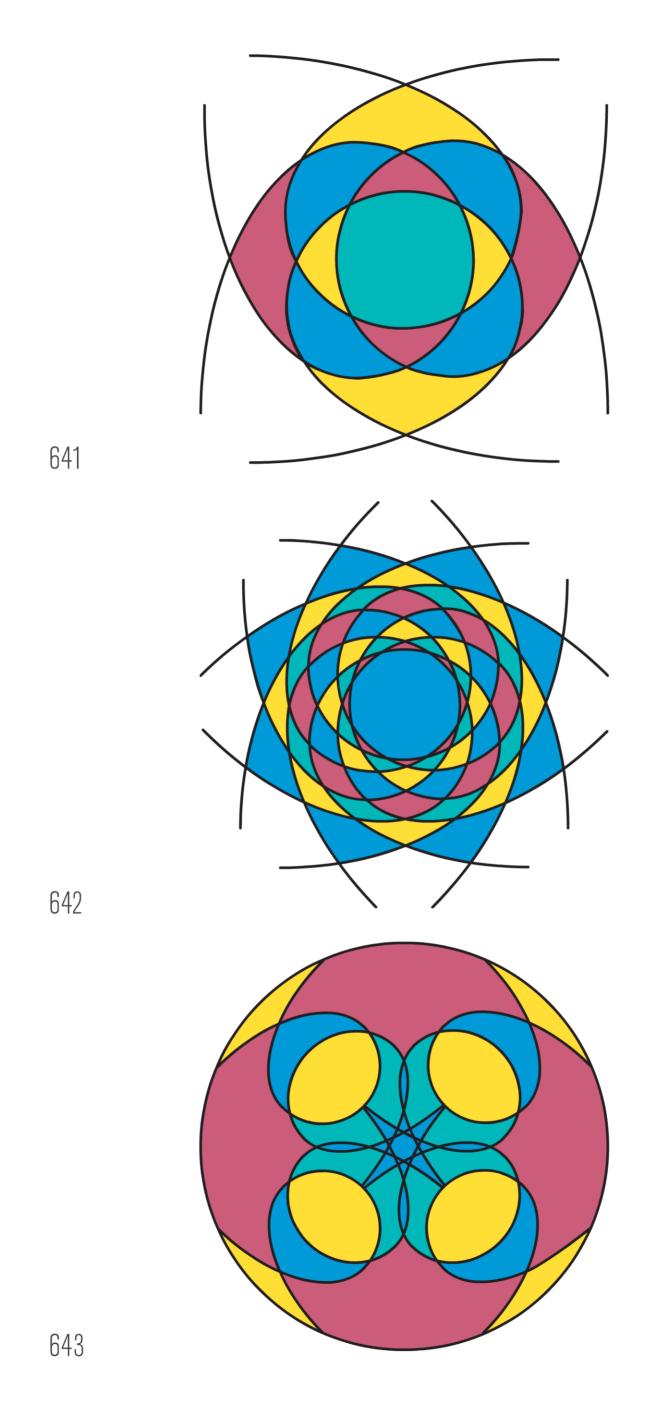


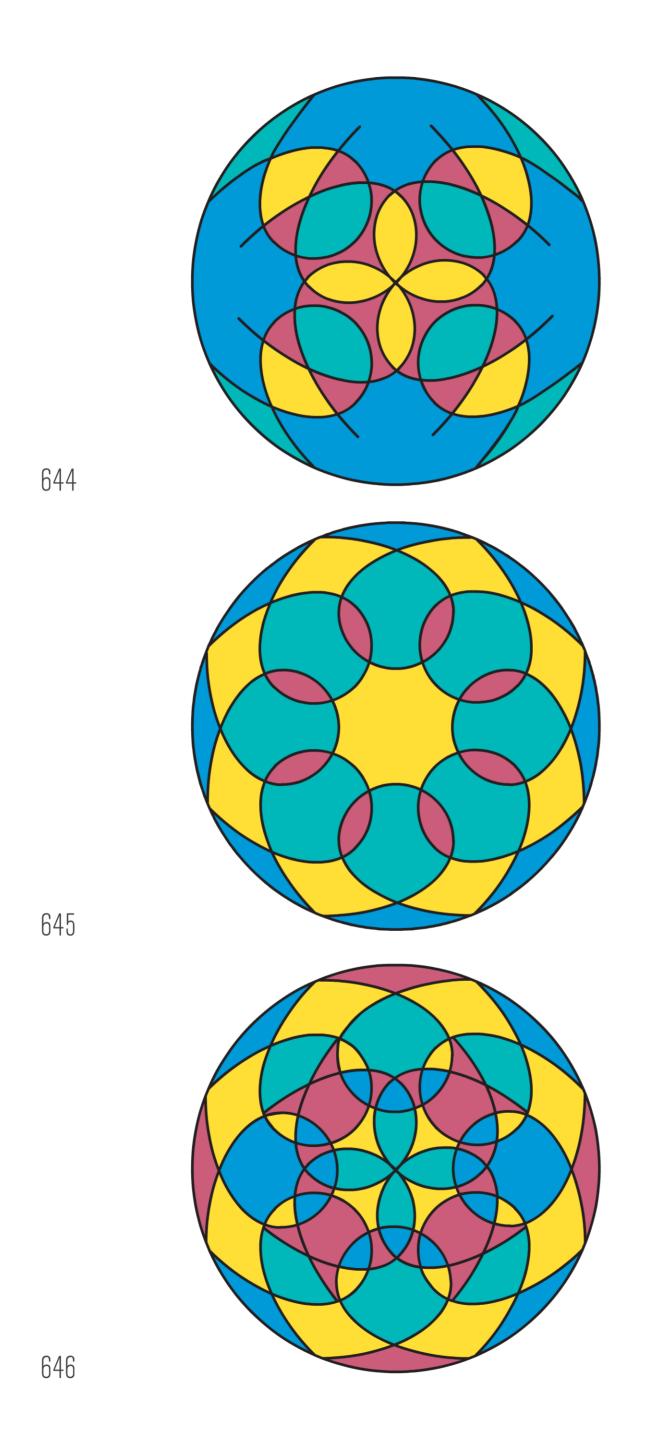




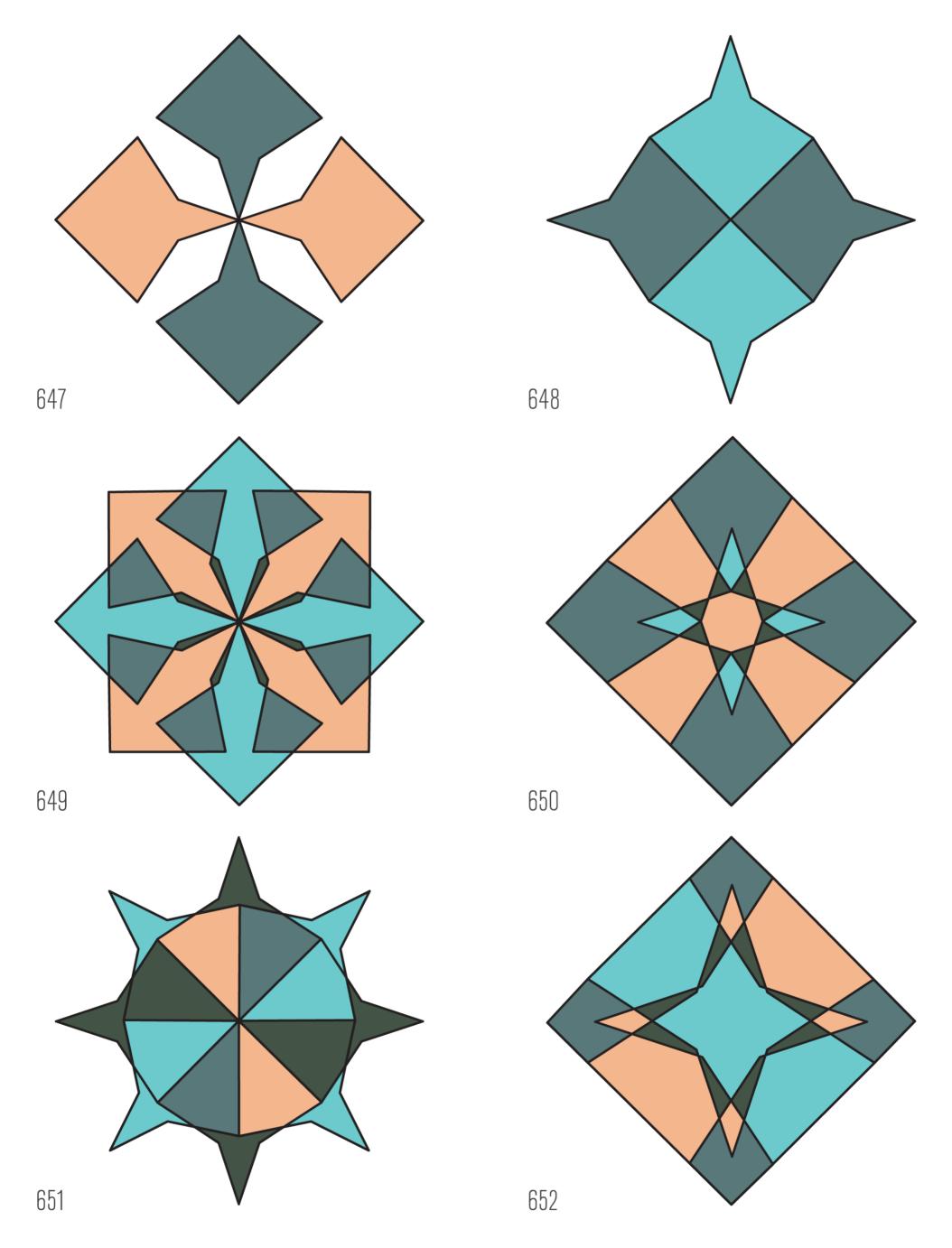


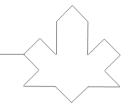
Loops



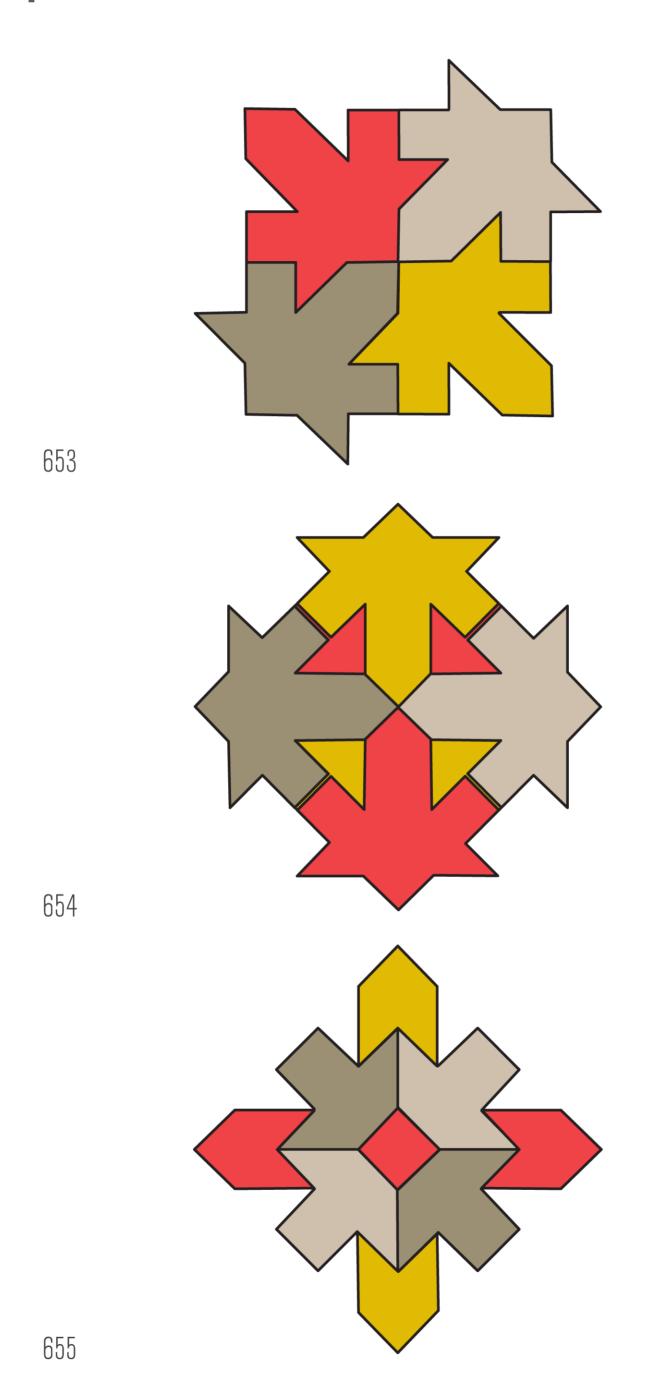


Manta Rays





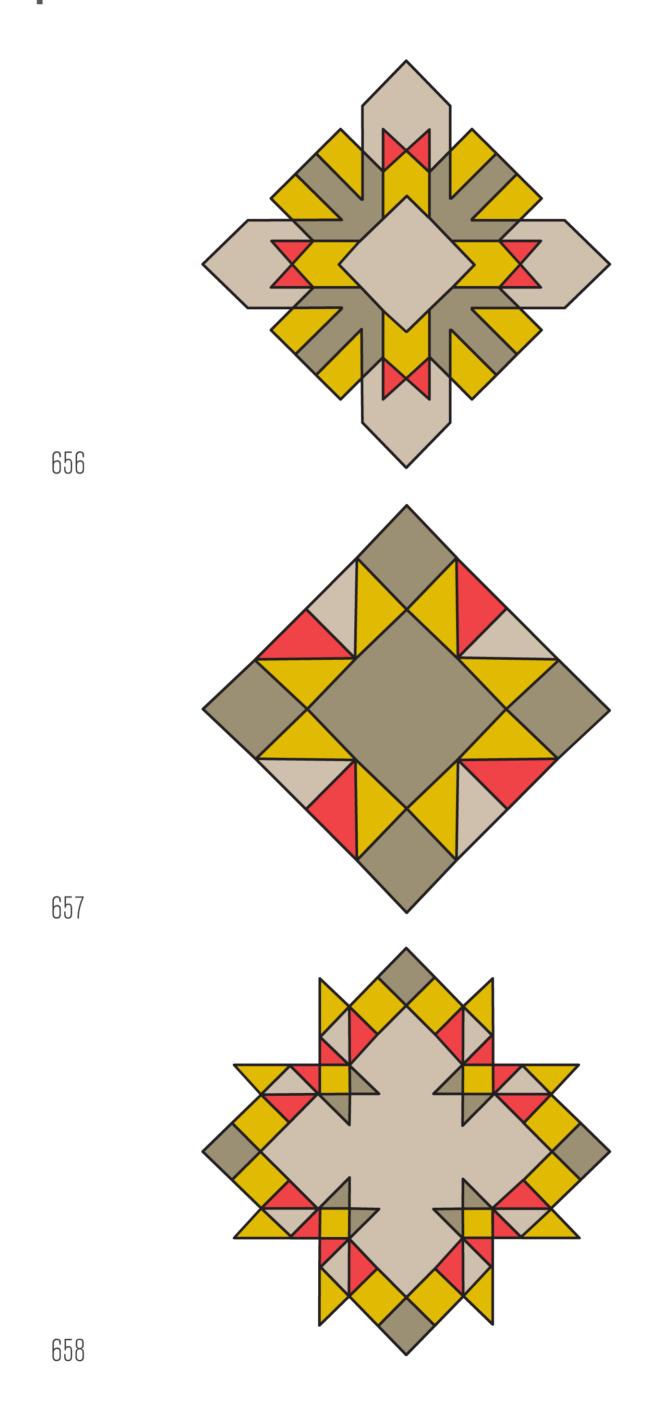
Maple Leaf

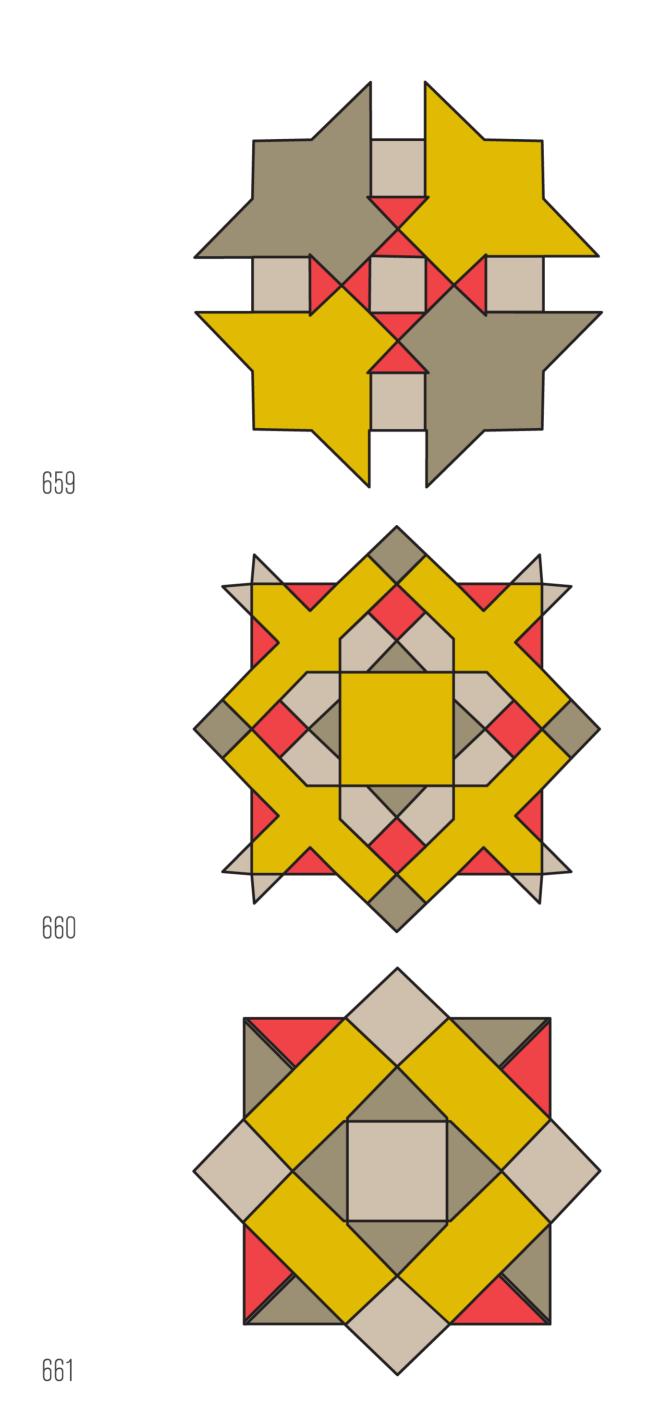


Maple Leaf

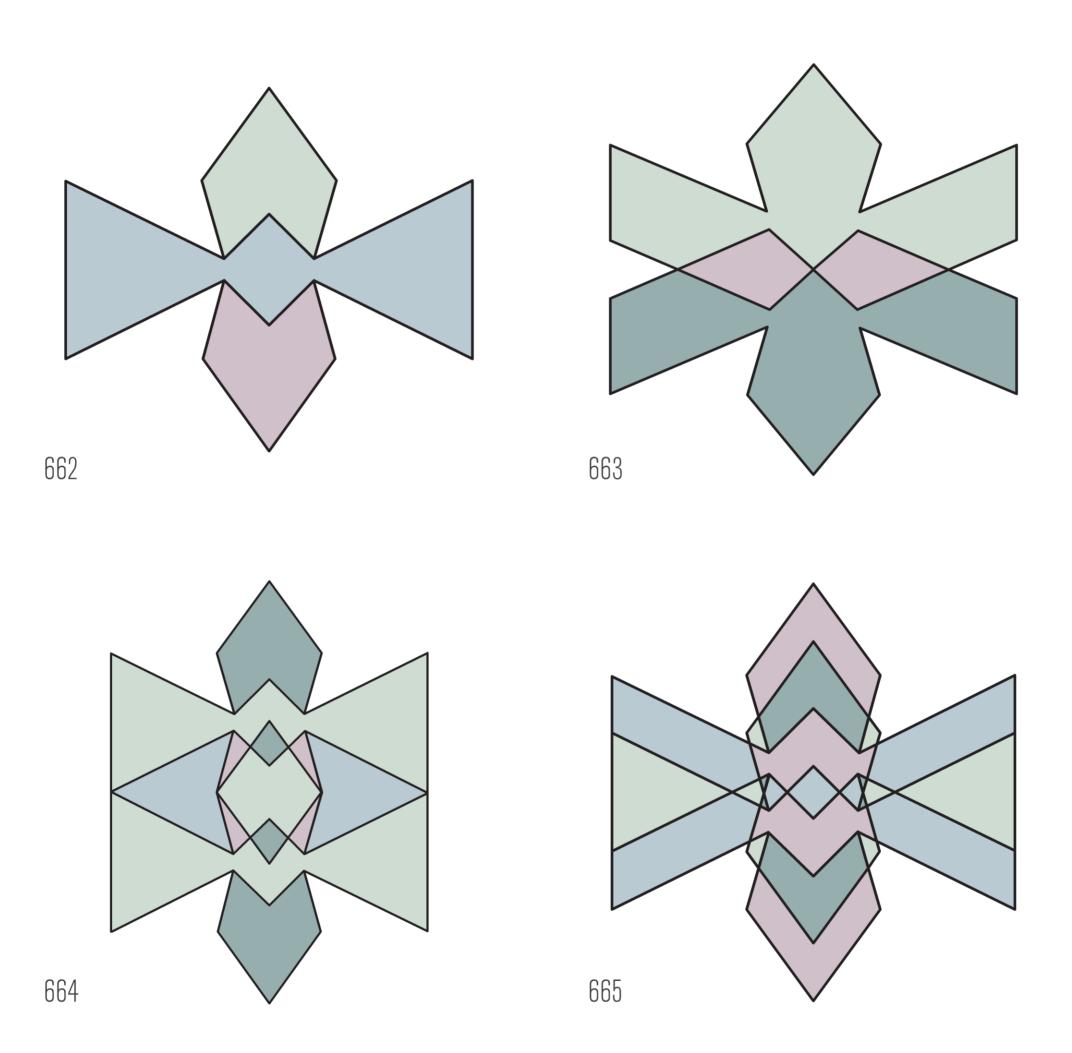


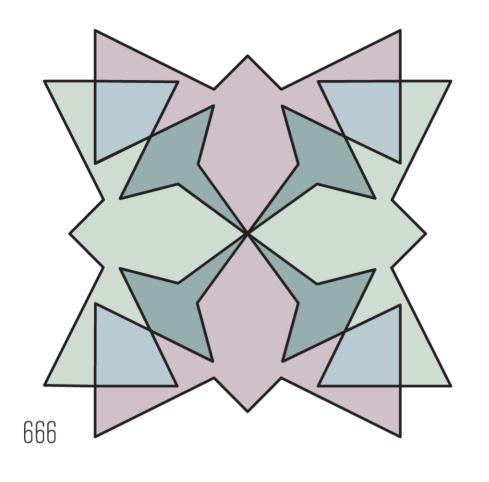
Maple Leaf

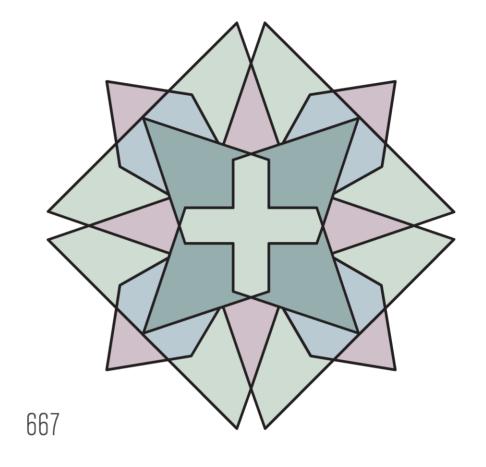


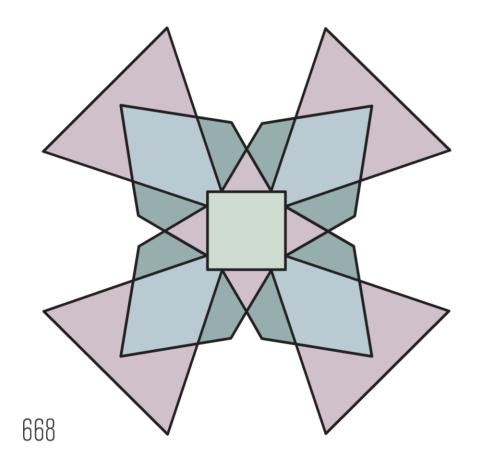


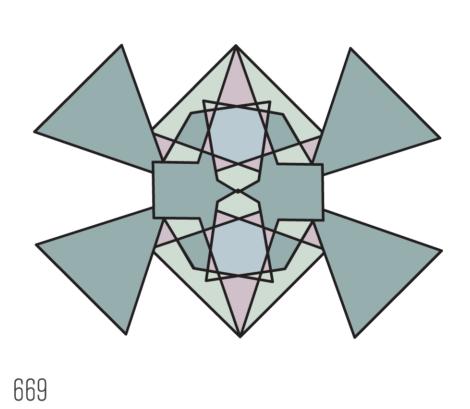
Moths



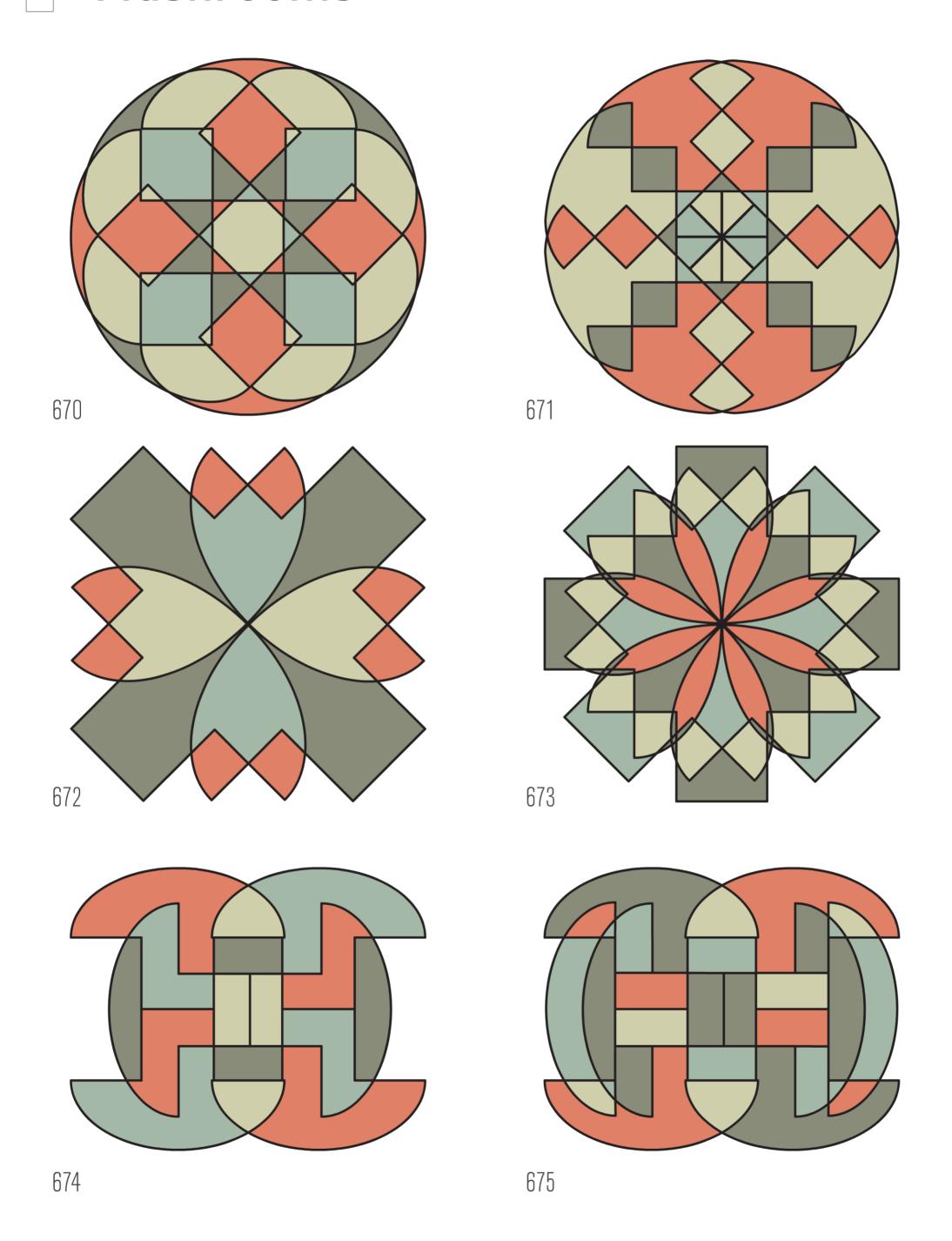




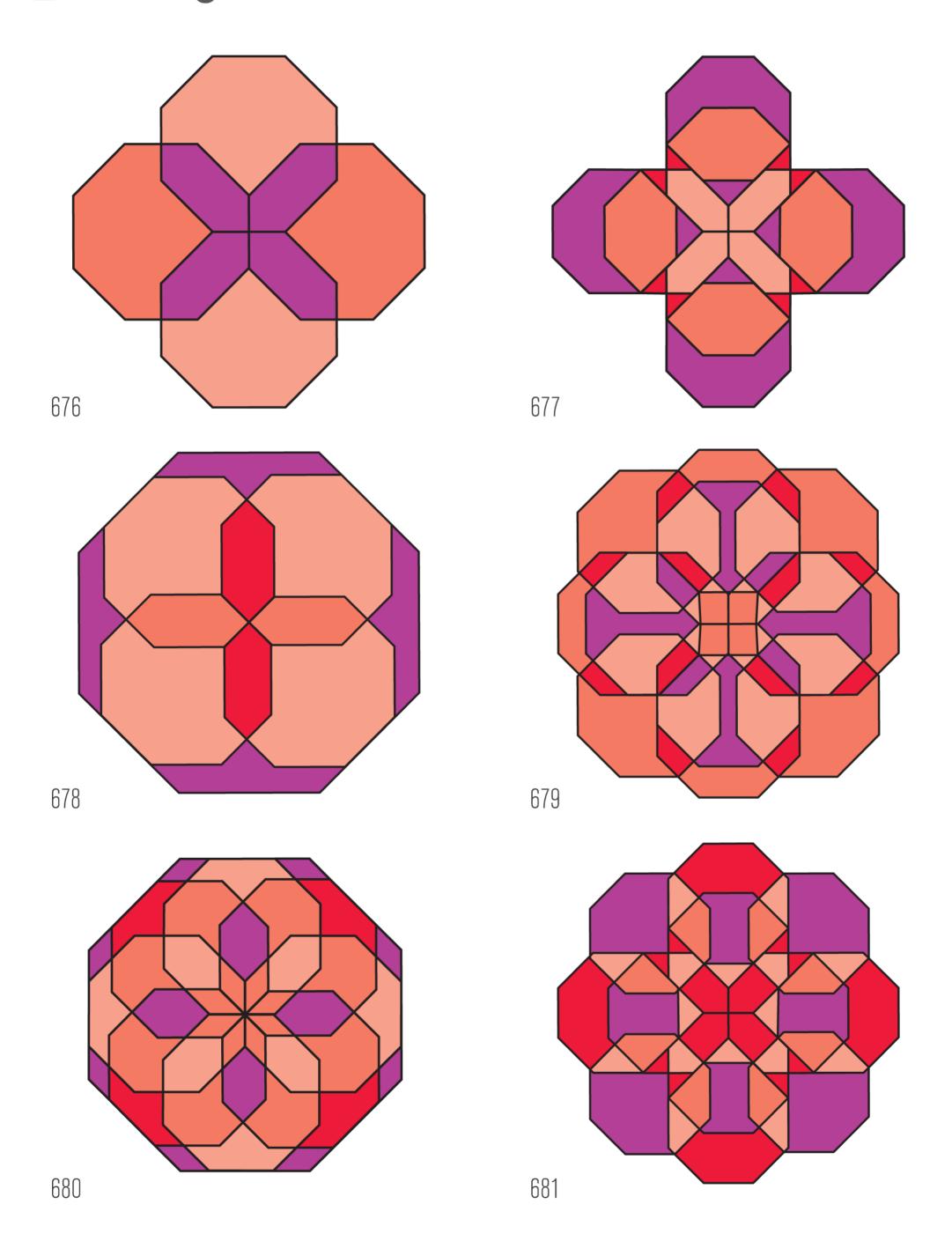




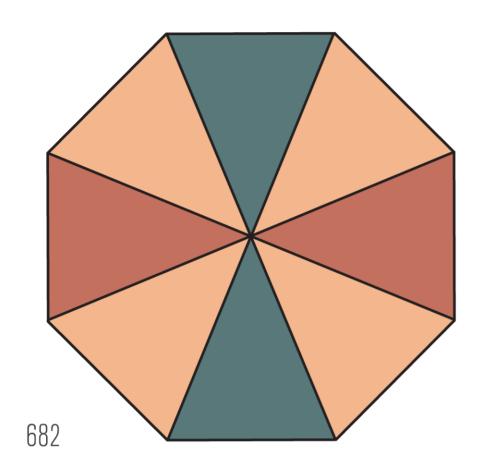
Mushrooms

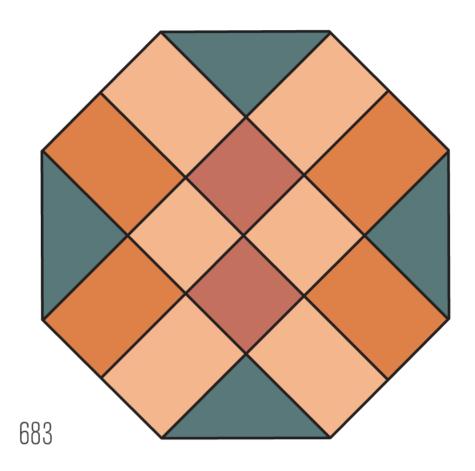


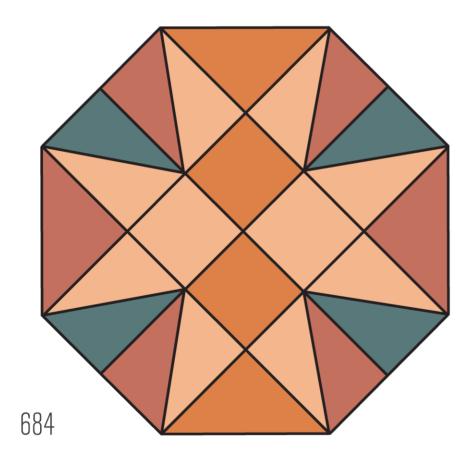
Octagons

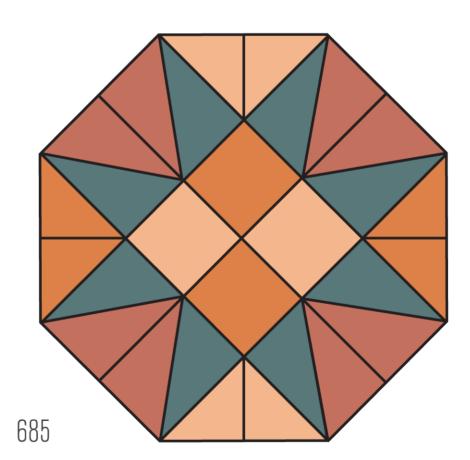


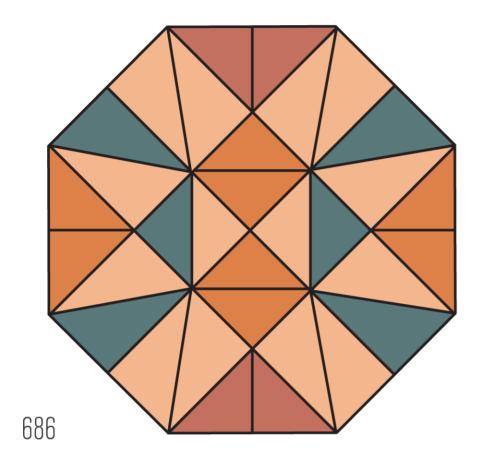
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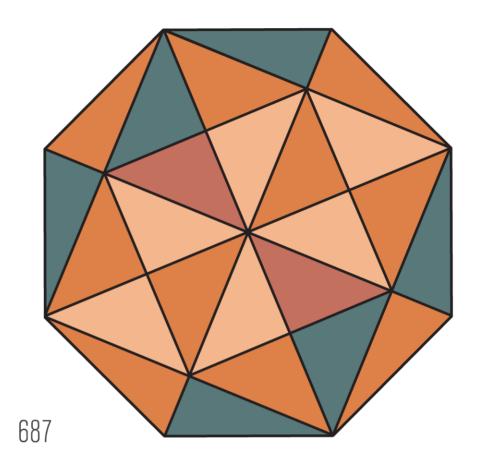


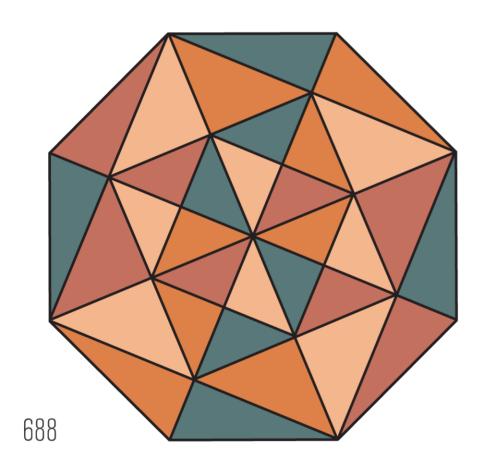


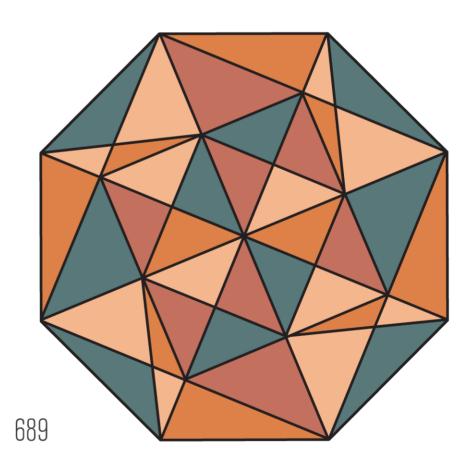




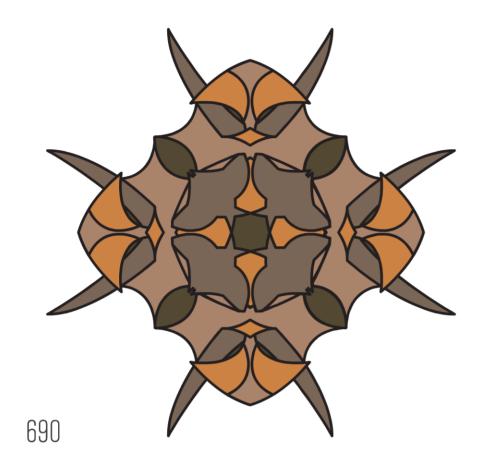


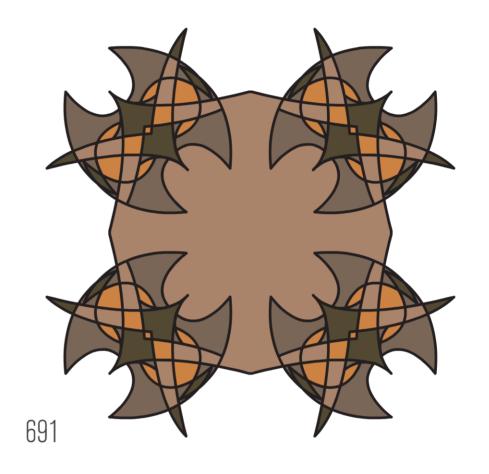


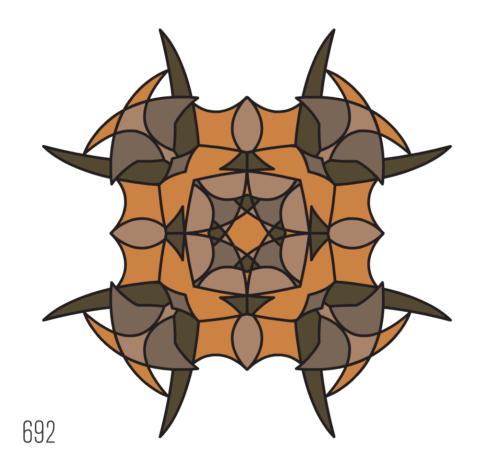


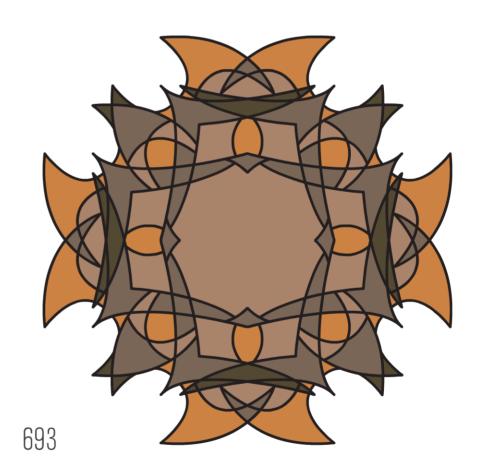


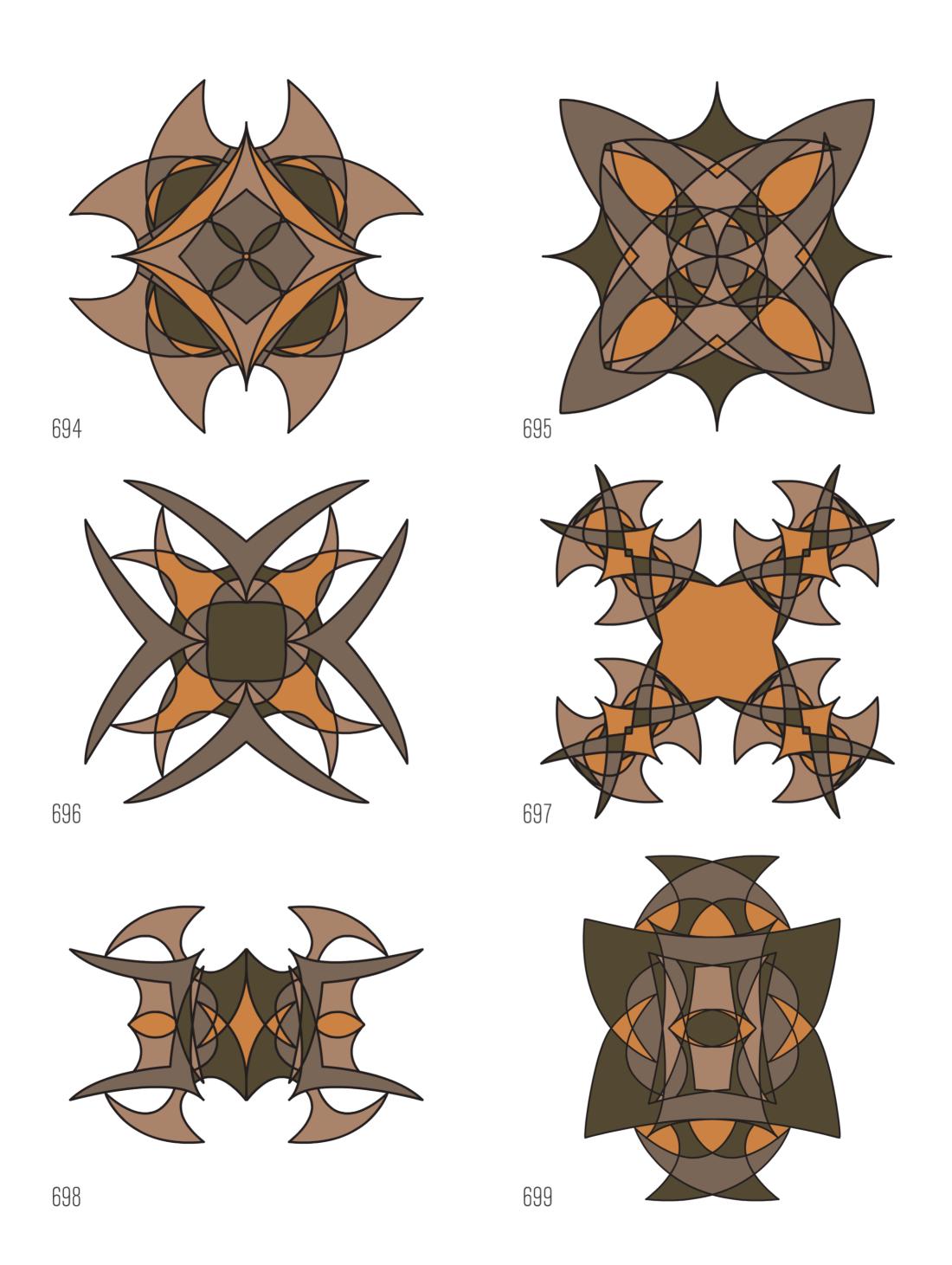
Owl Face



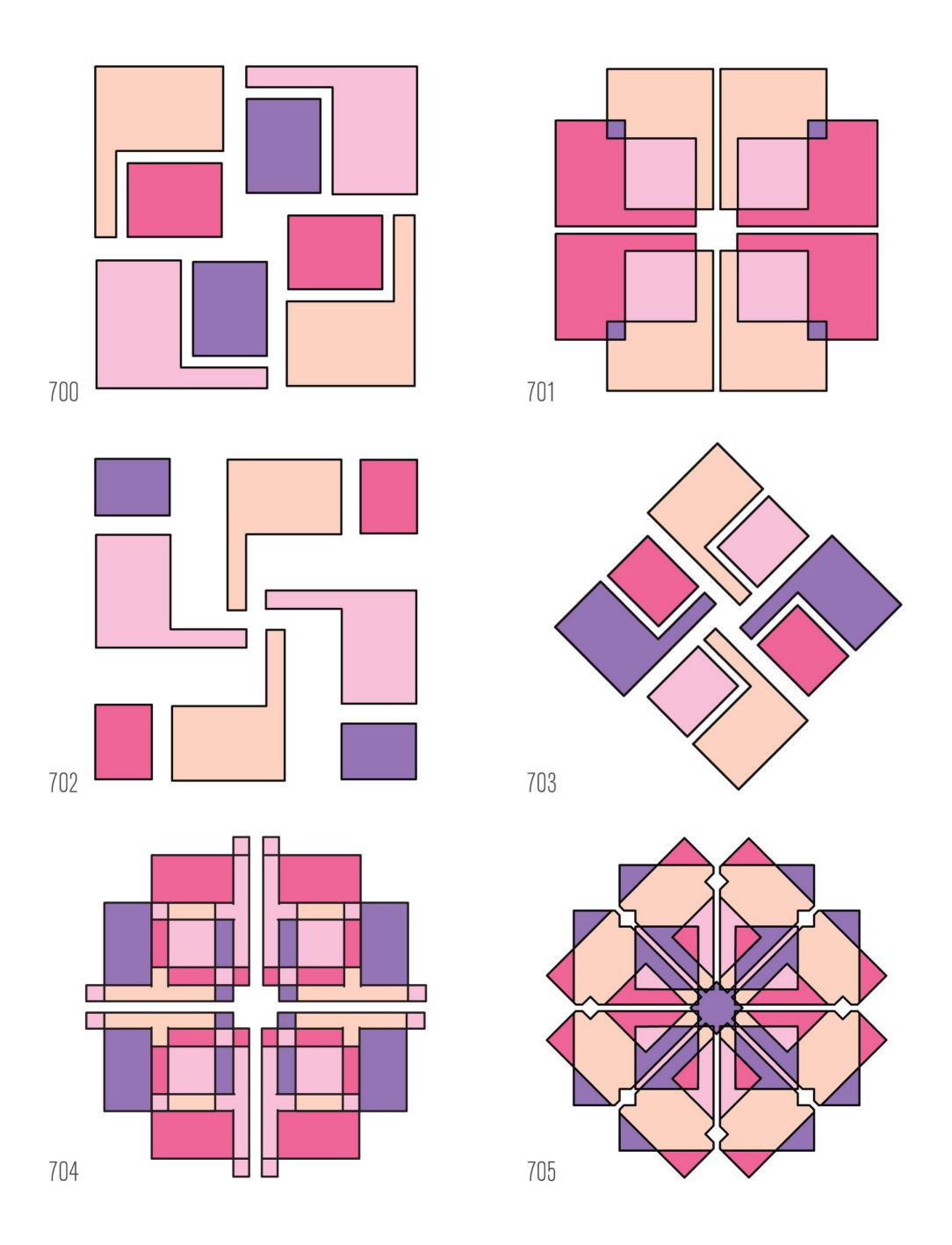


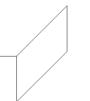




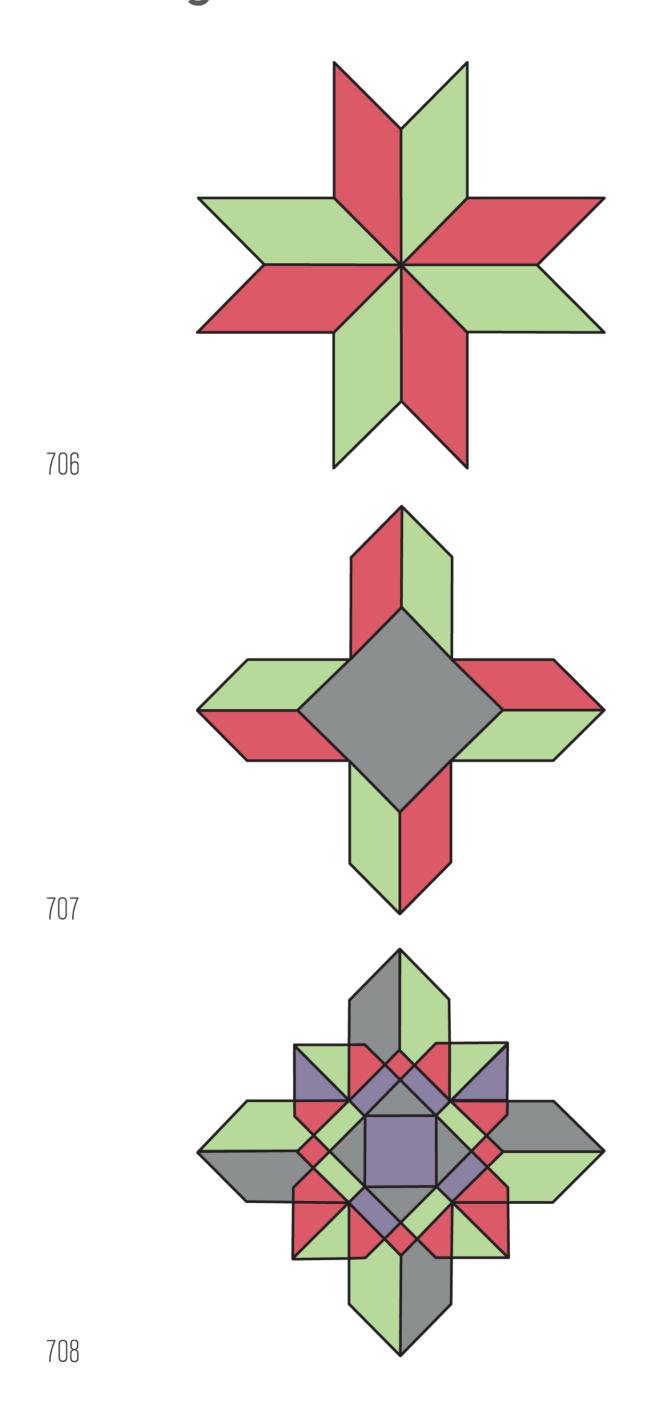


Paddles



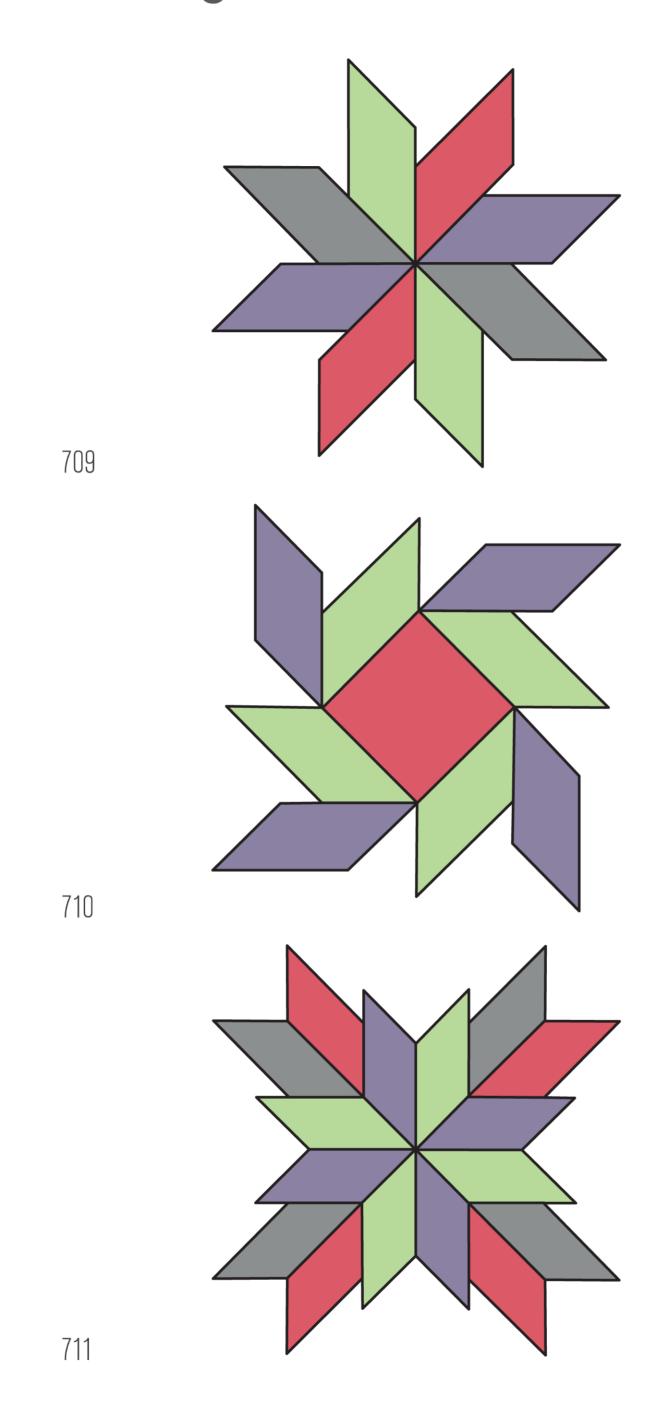


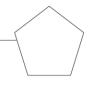
Parallelograms



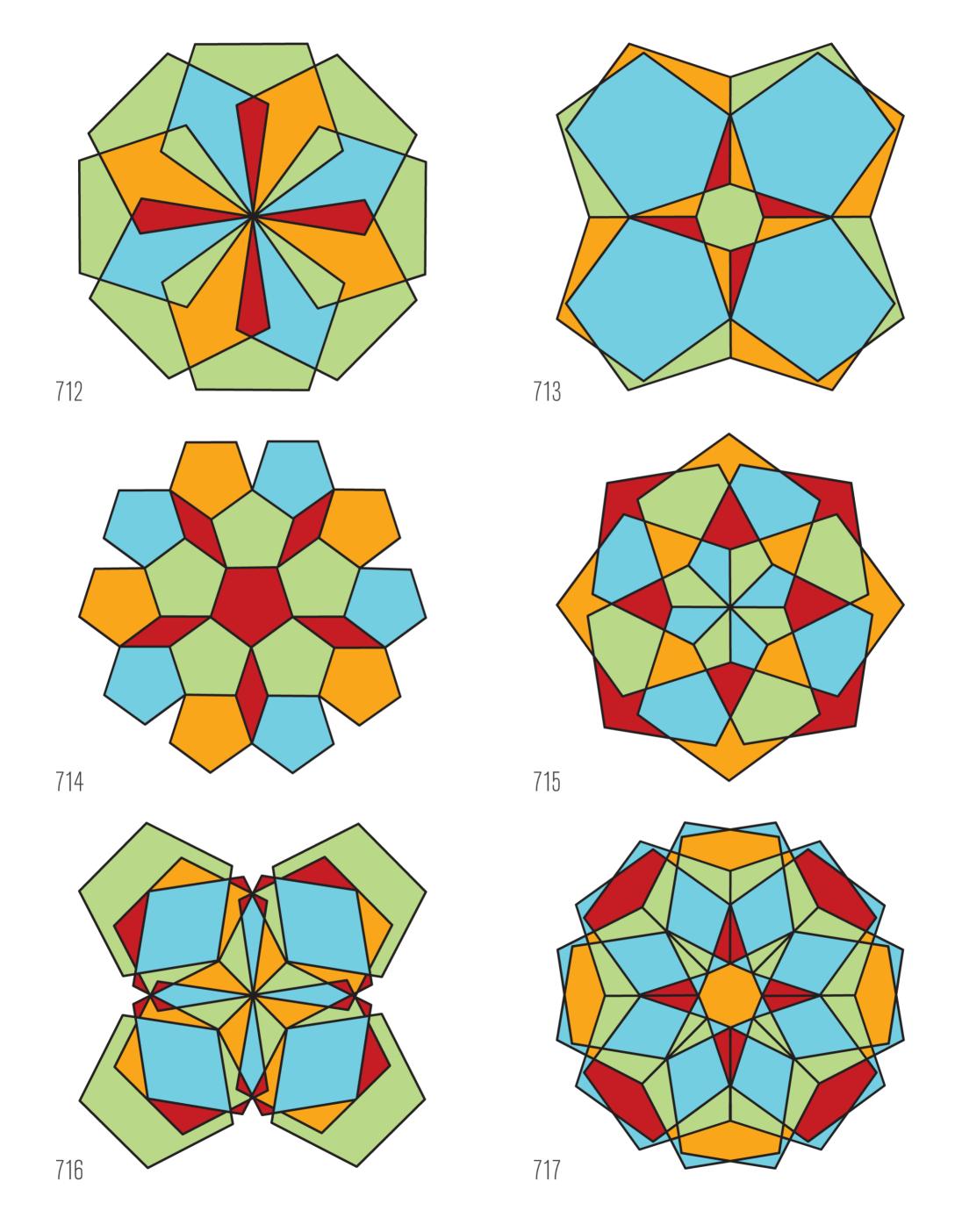
145

Parallelograms



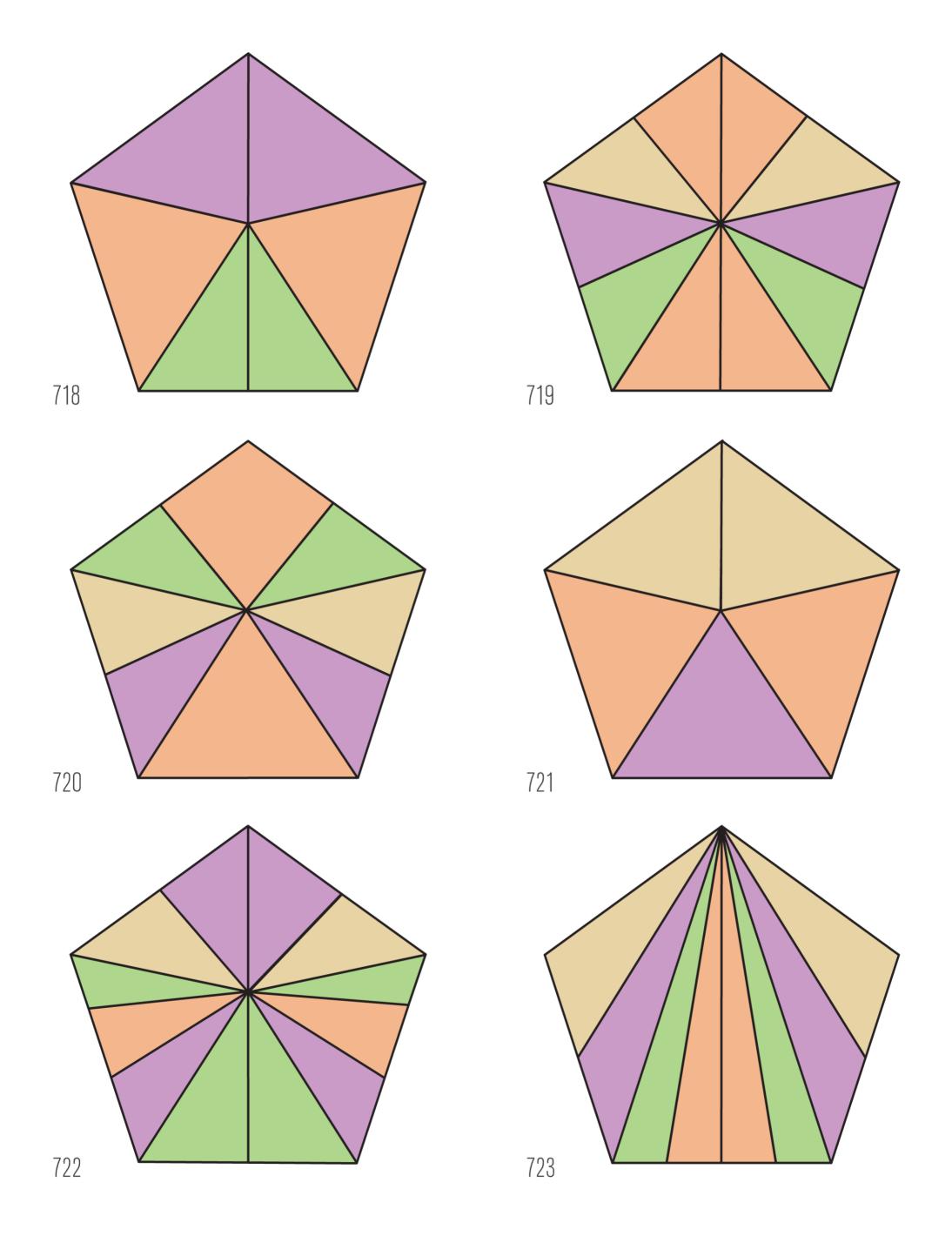


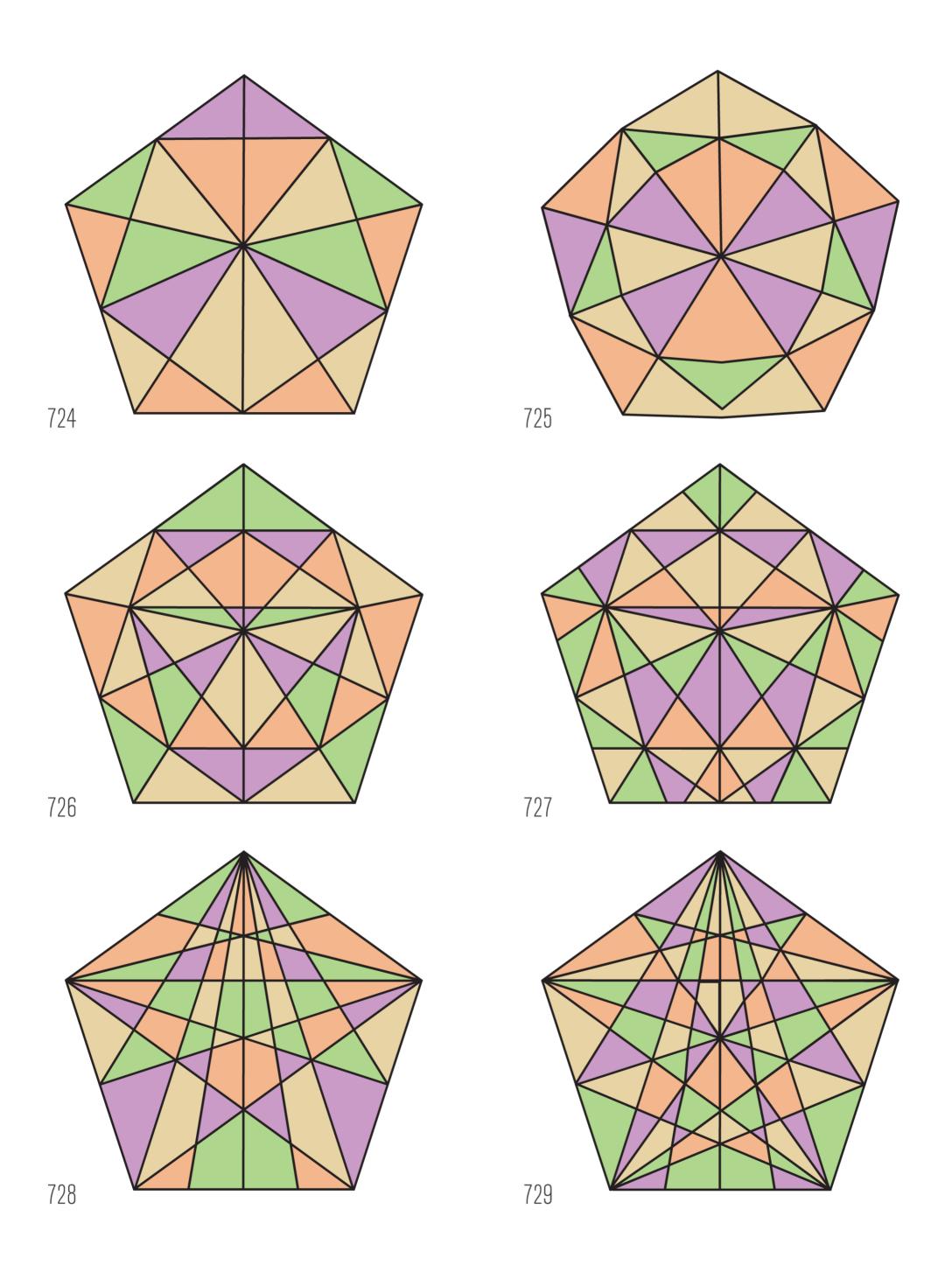
Pentagrams





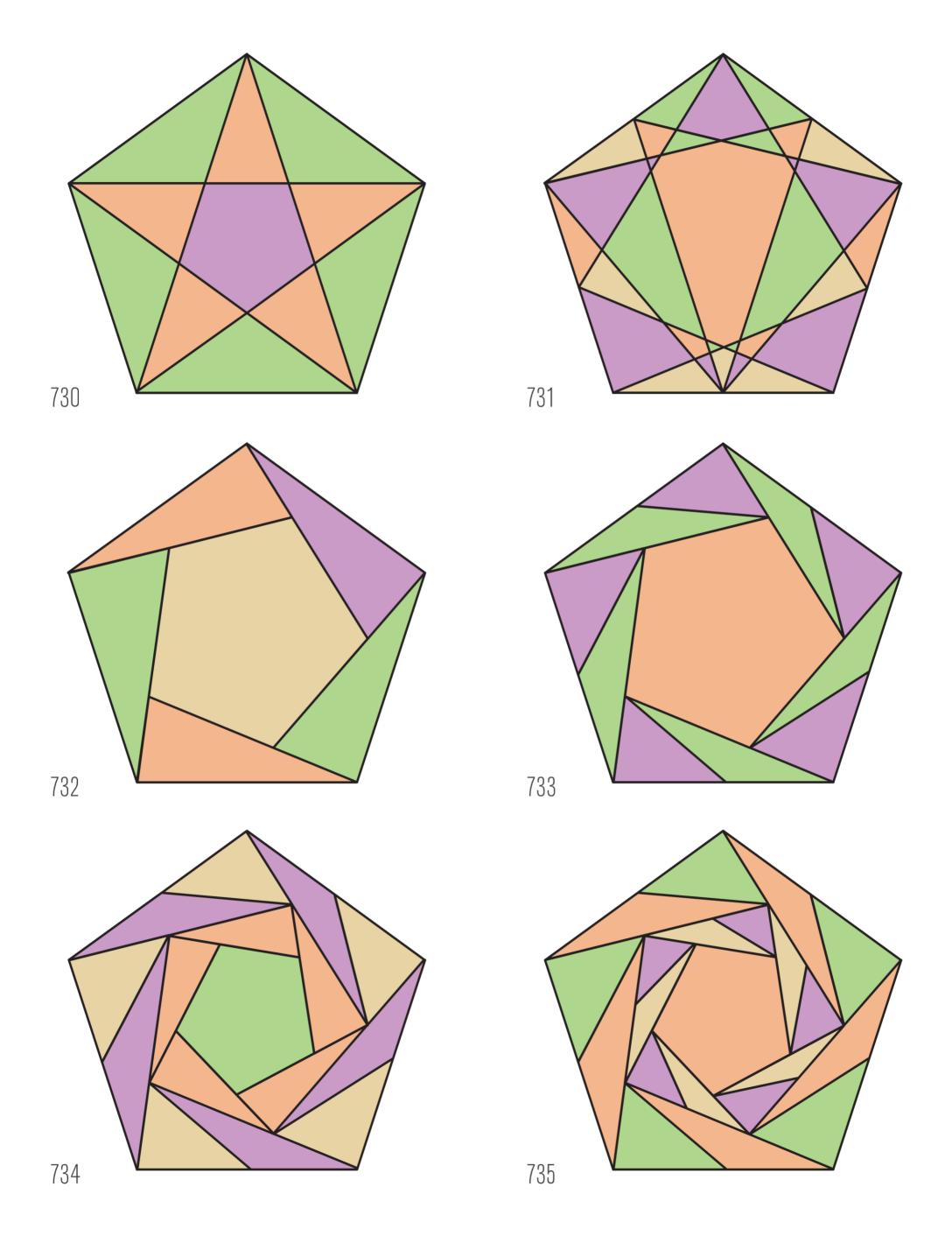
Pentagons Divided



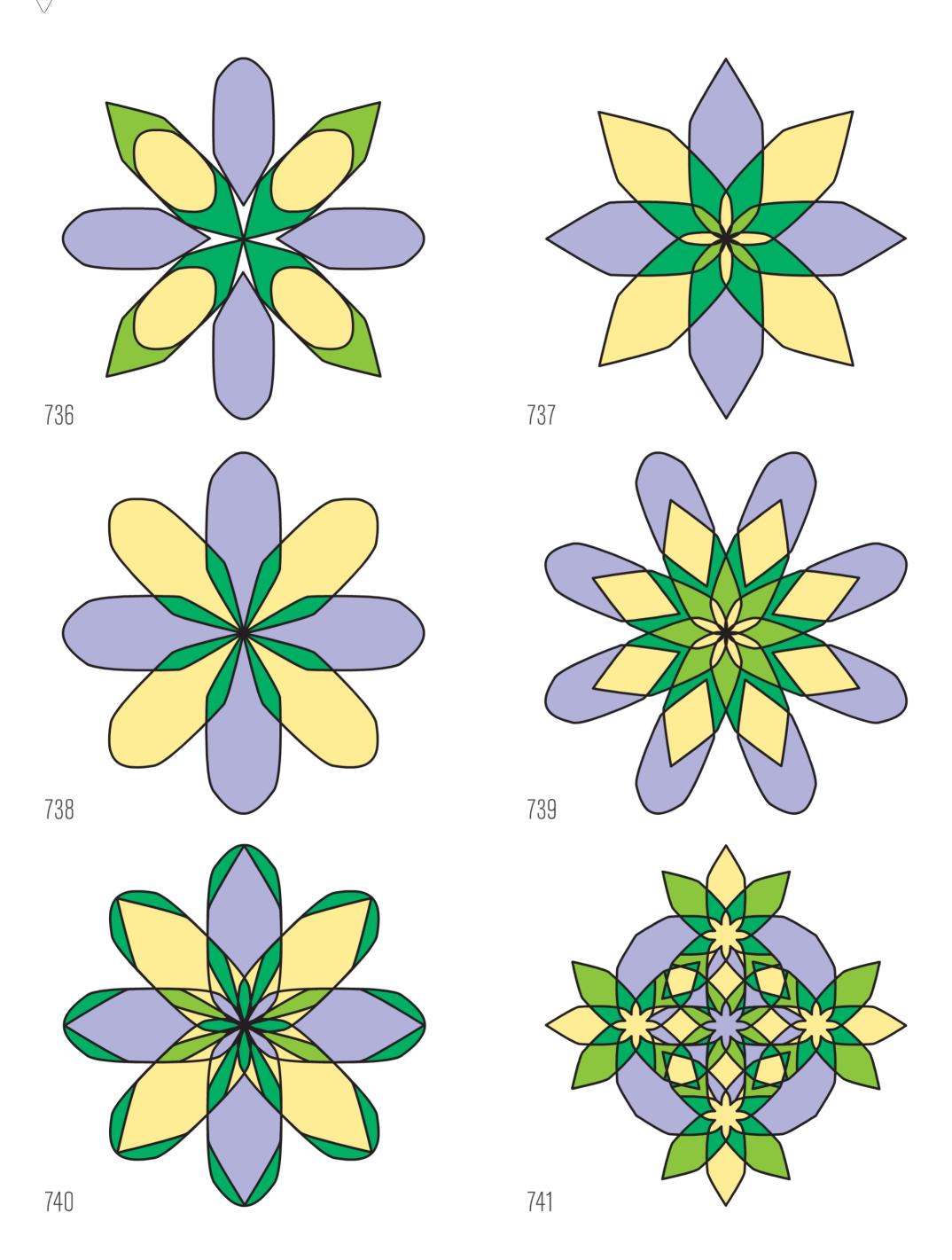




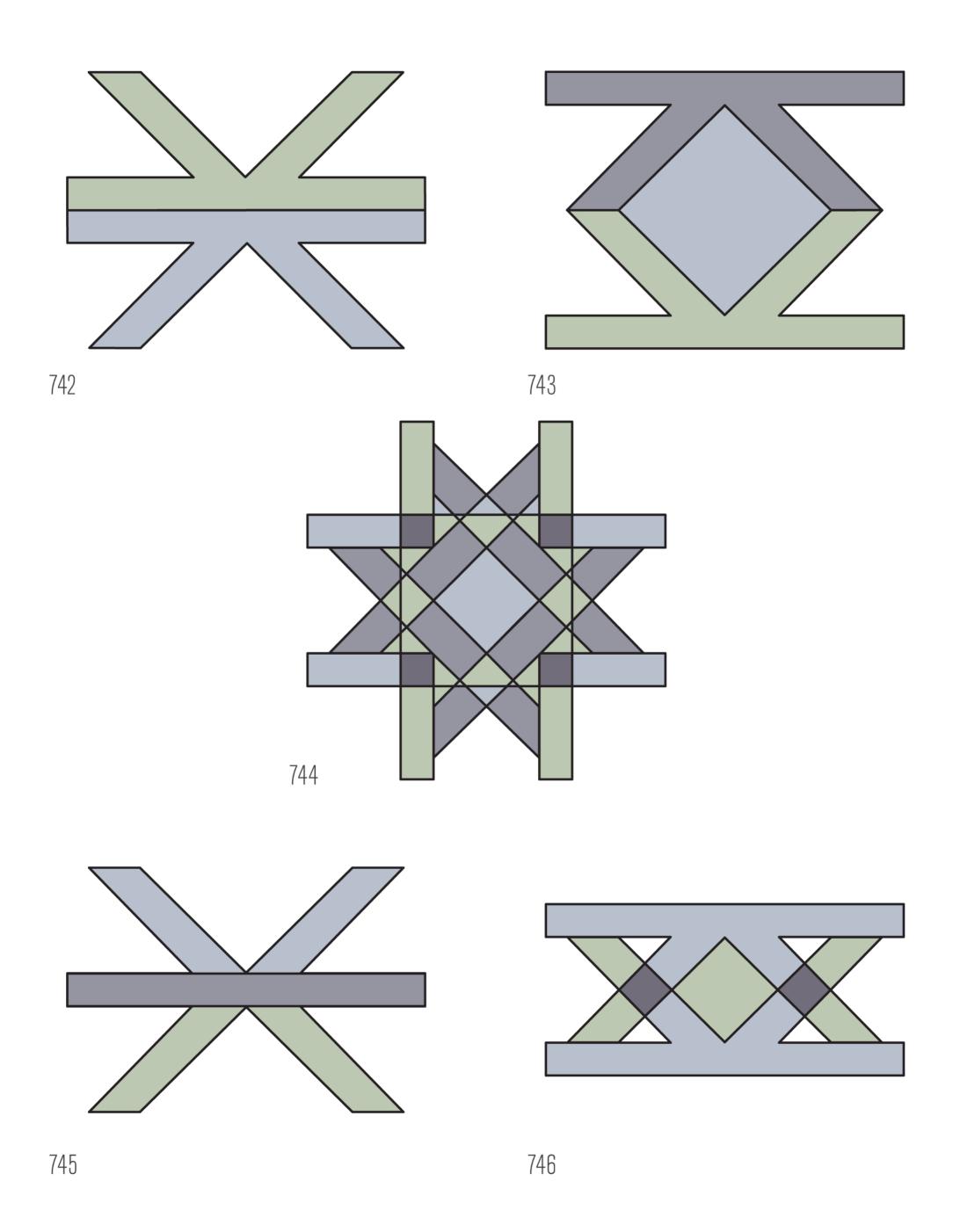
Pentagons Divided

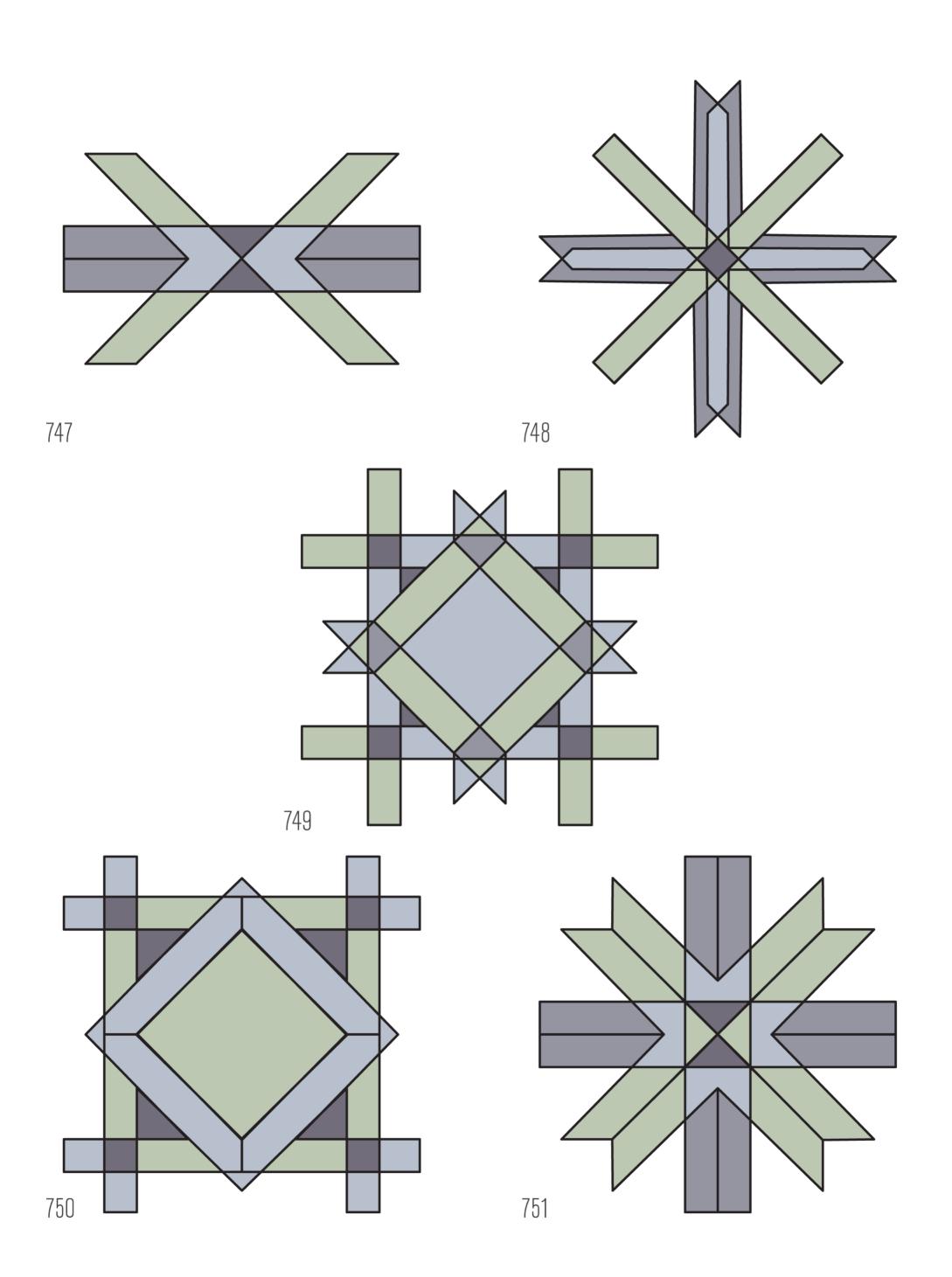


Petals

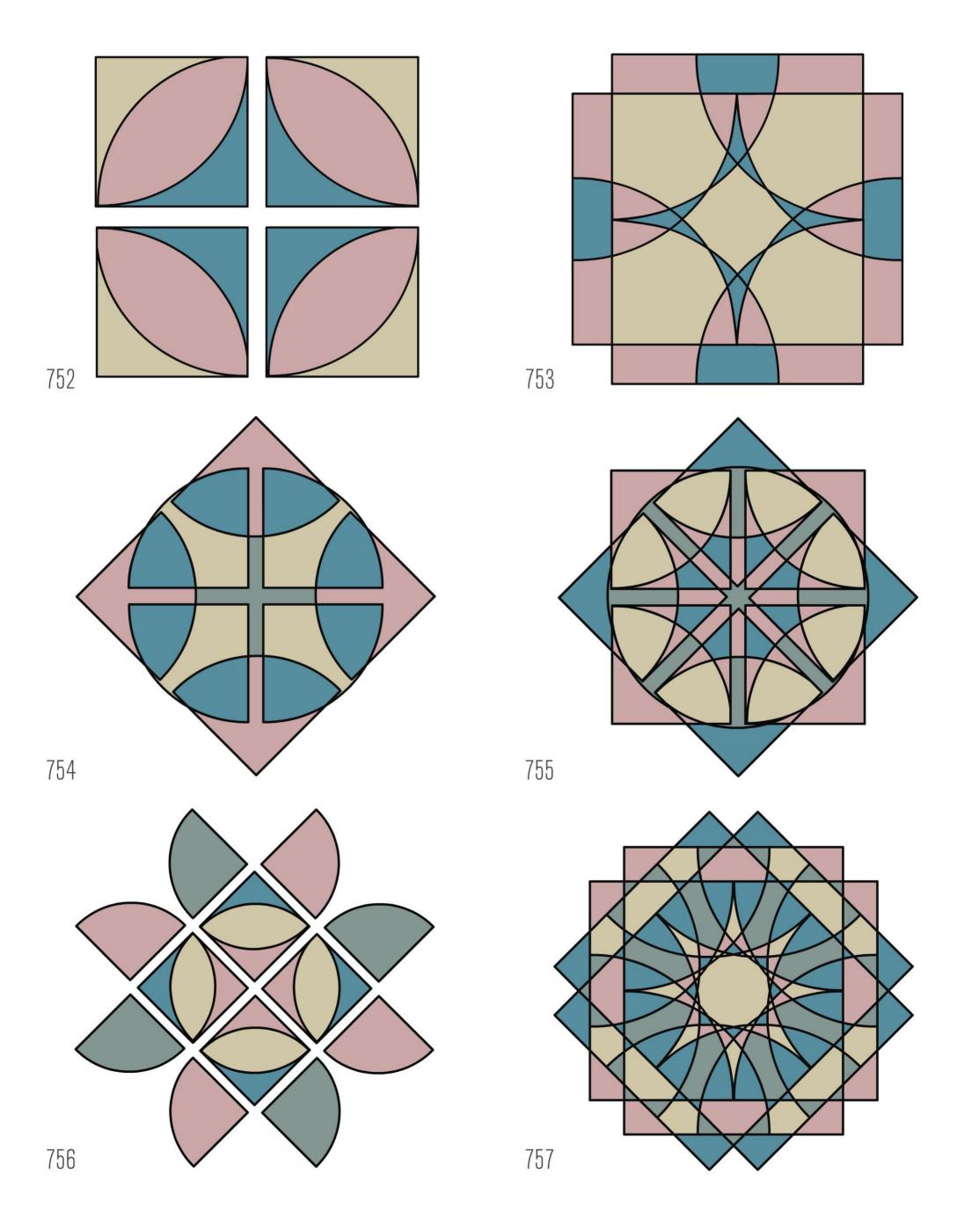


Picnic Tables



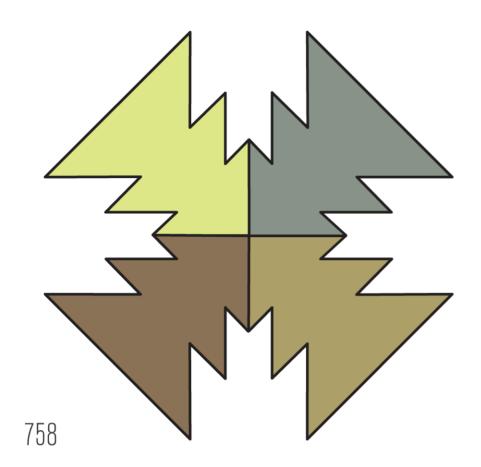


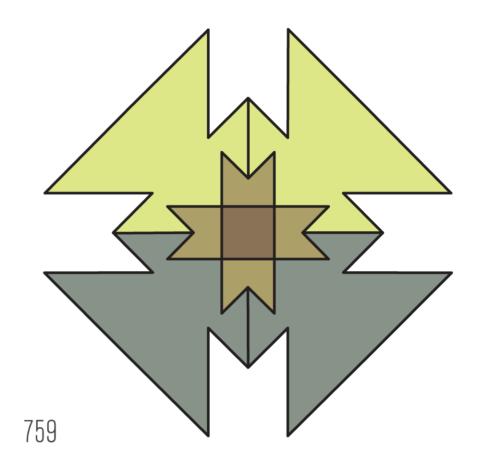
Pie Pieces

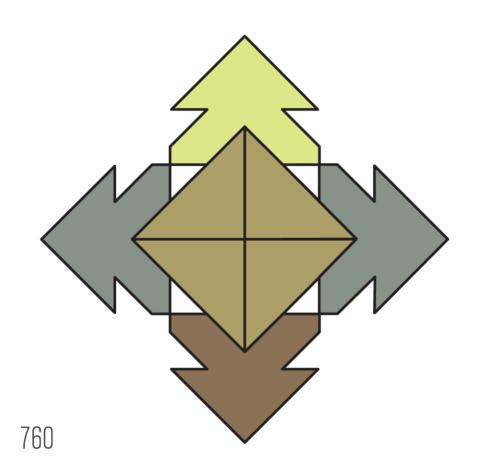


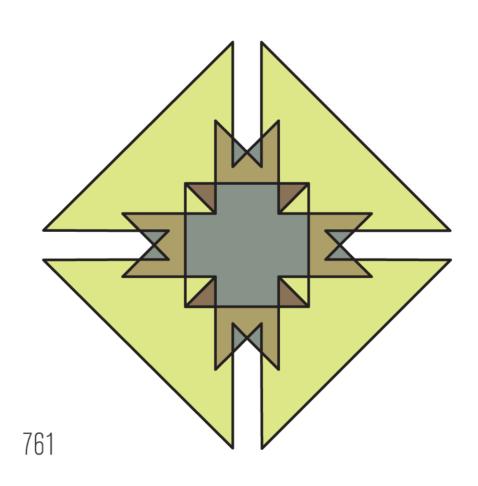


Pine Trees

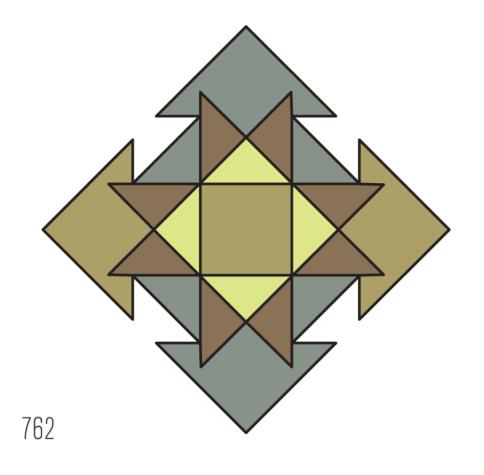


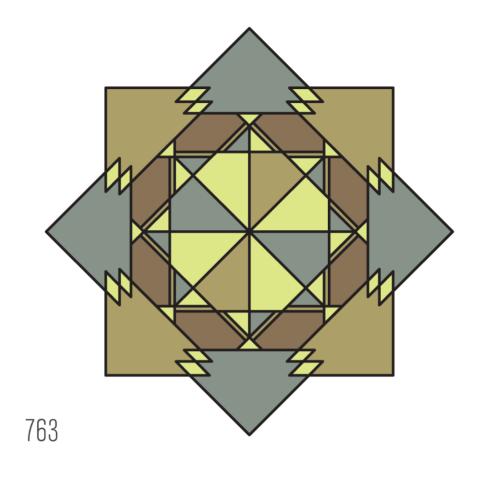


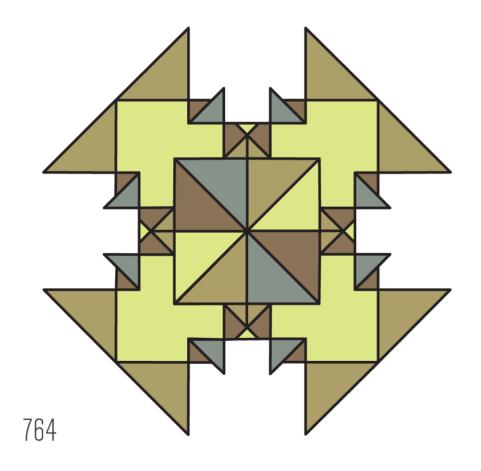


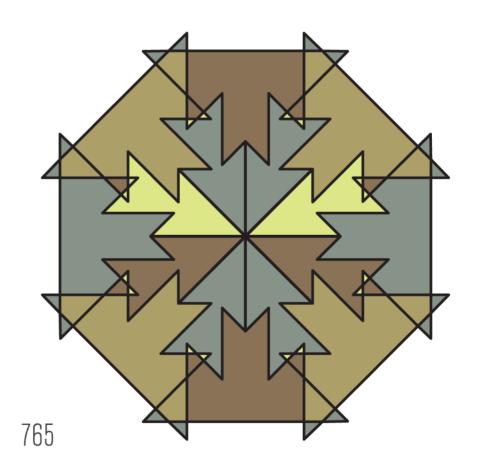




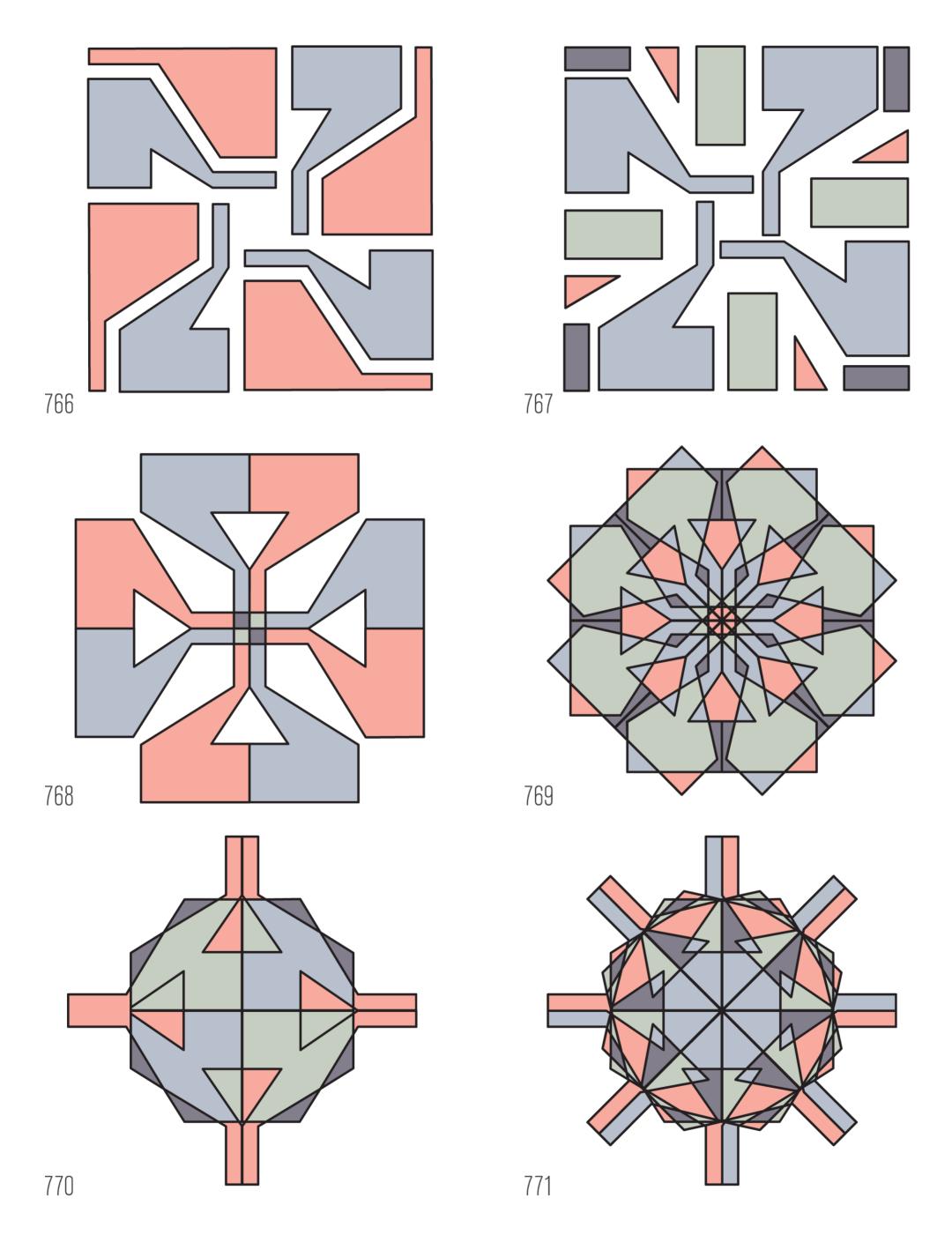


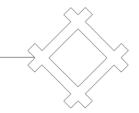




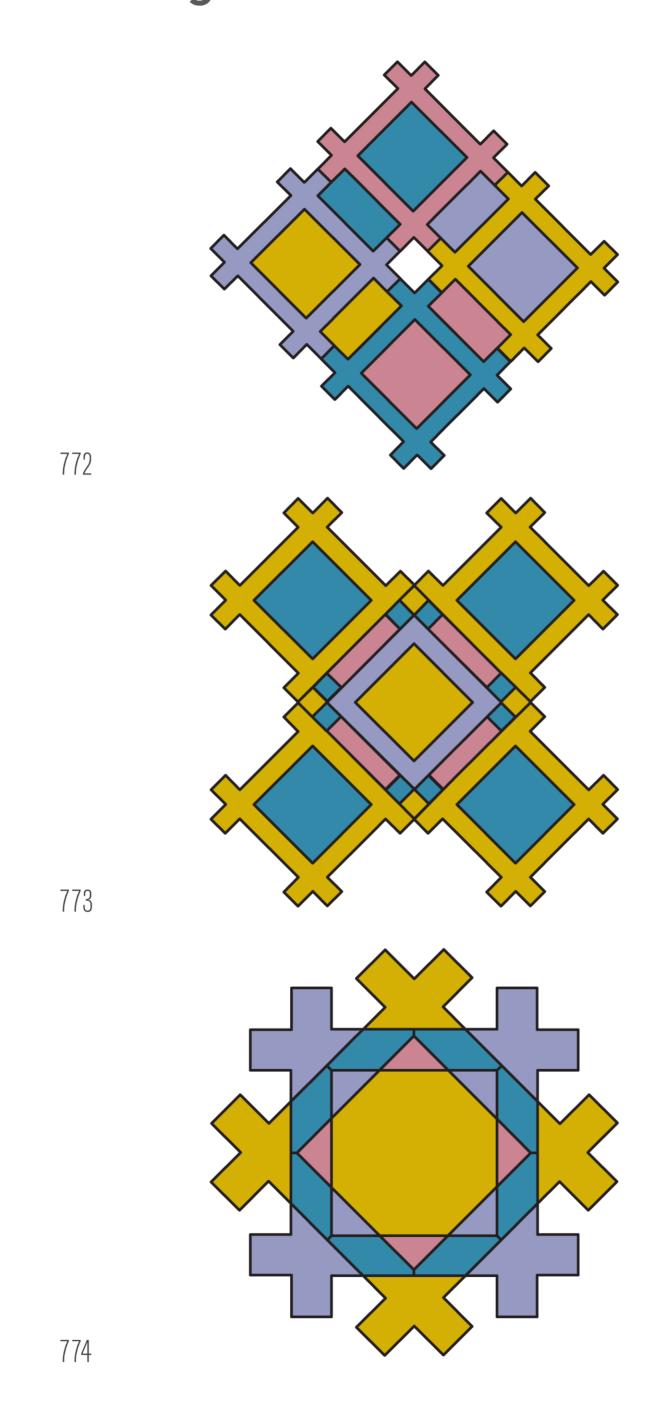


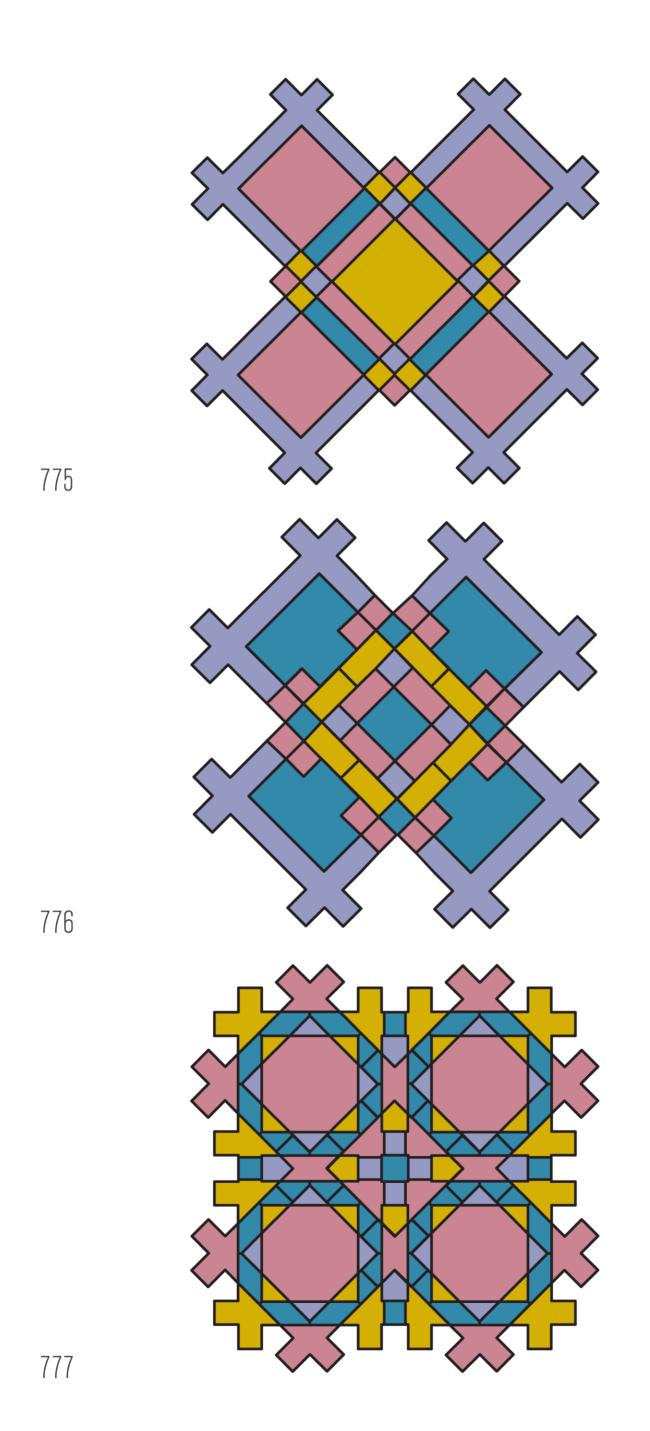




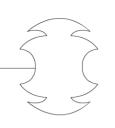


Pound Signs

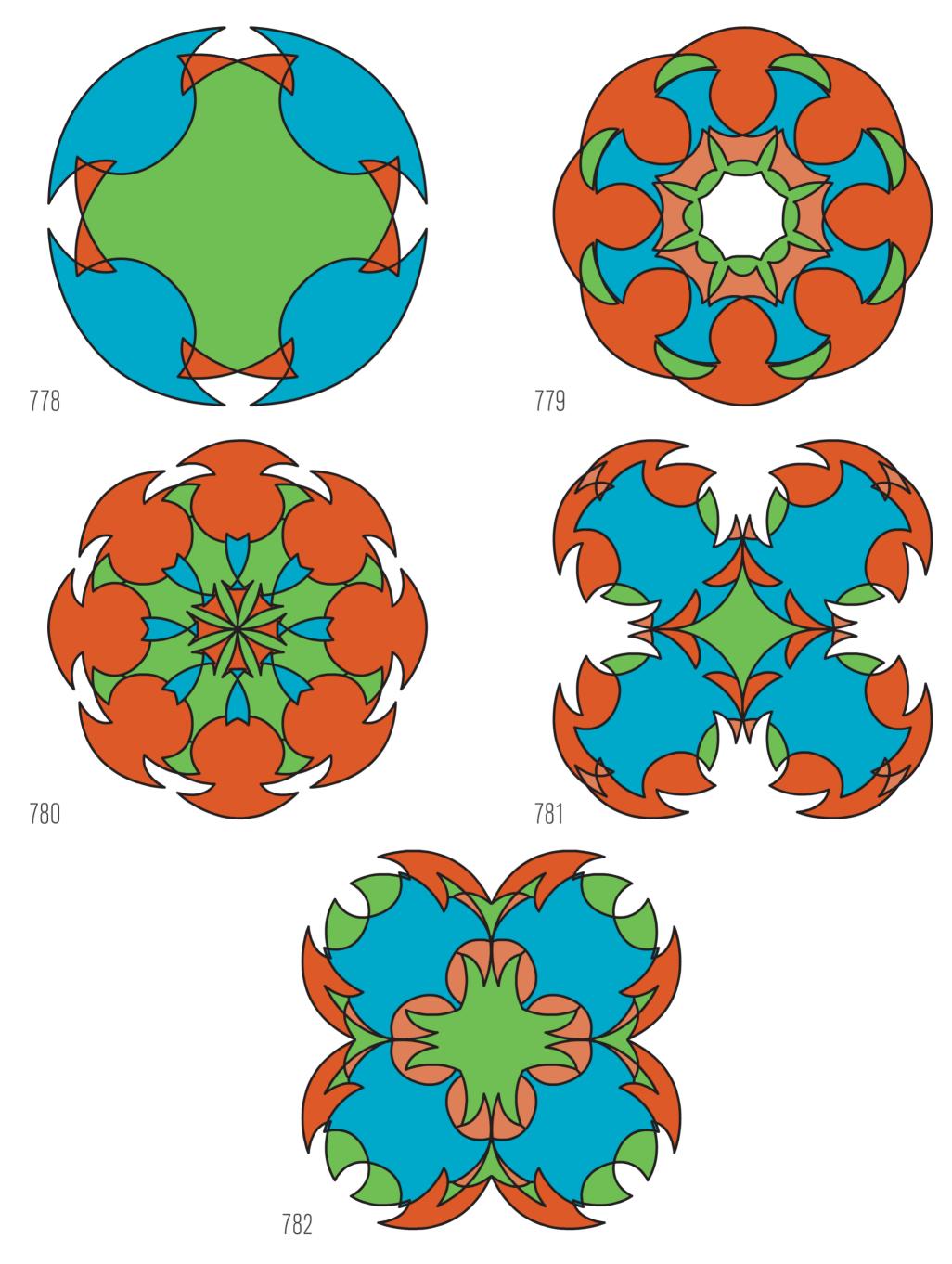


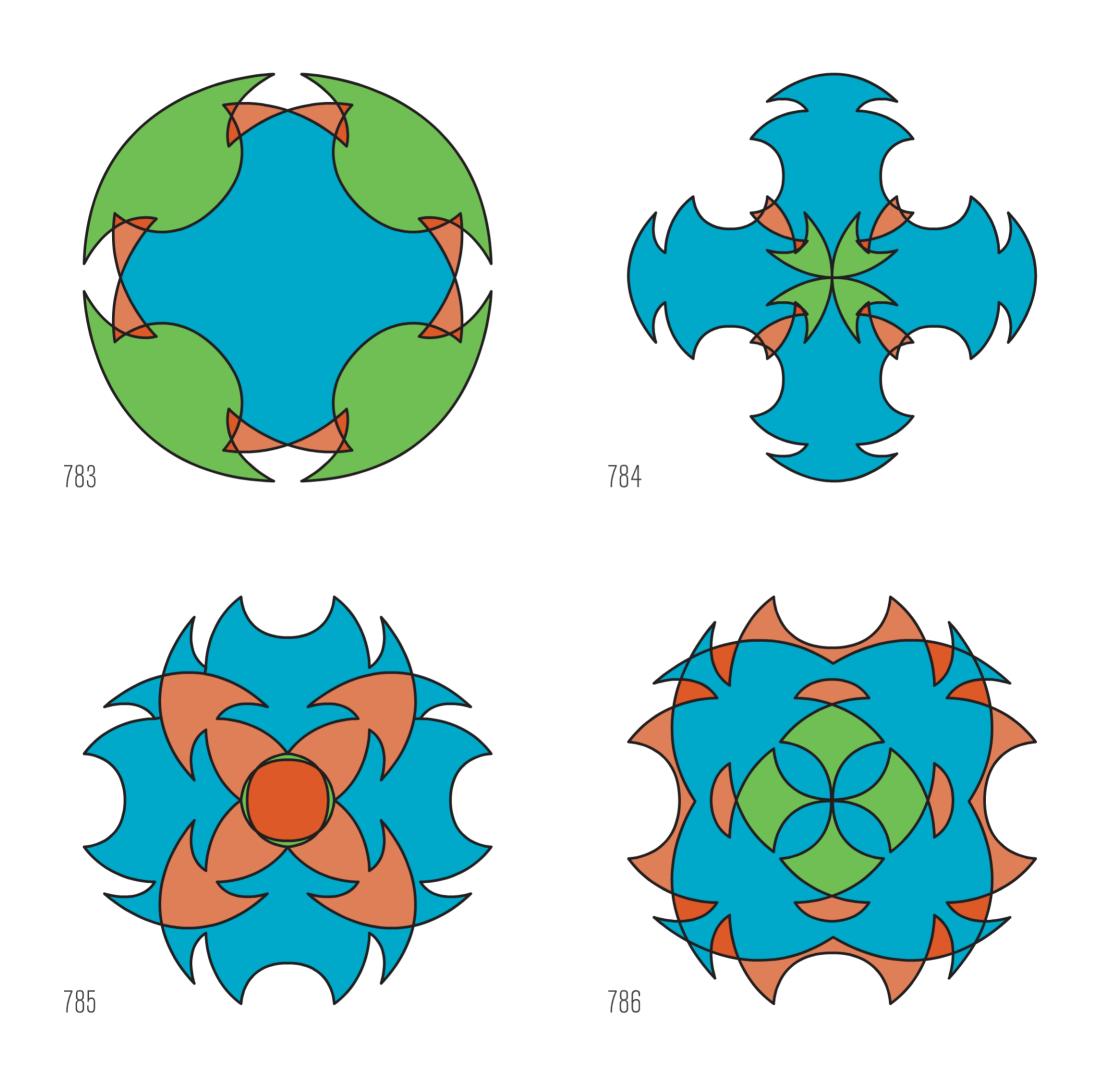


159

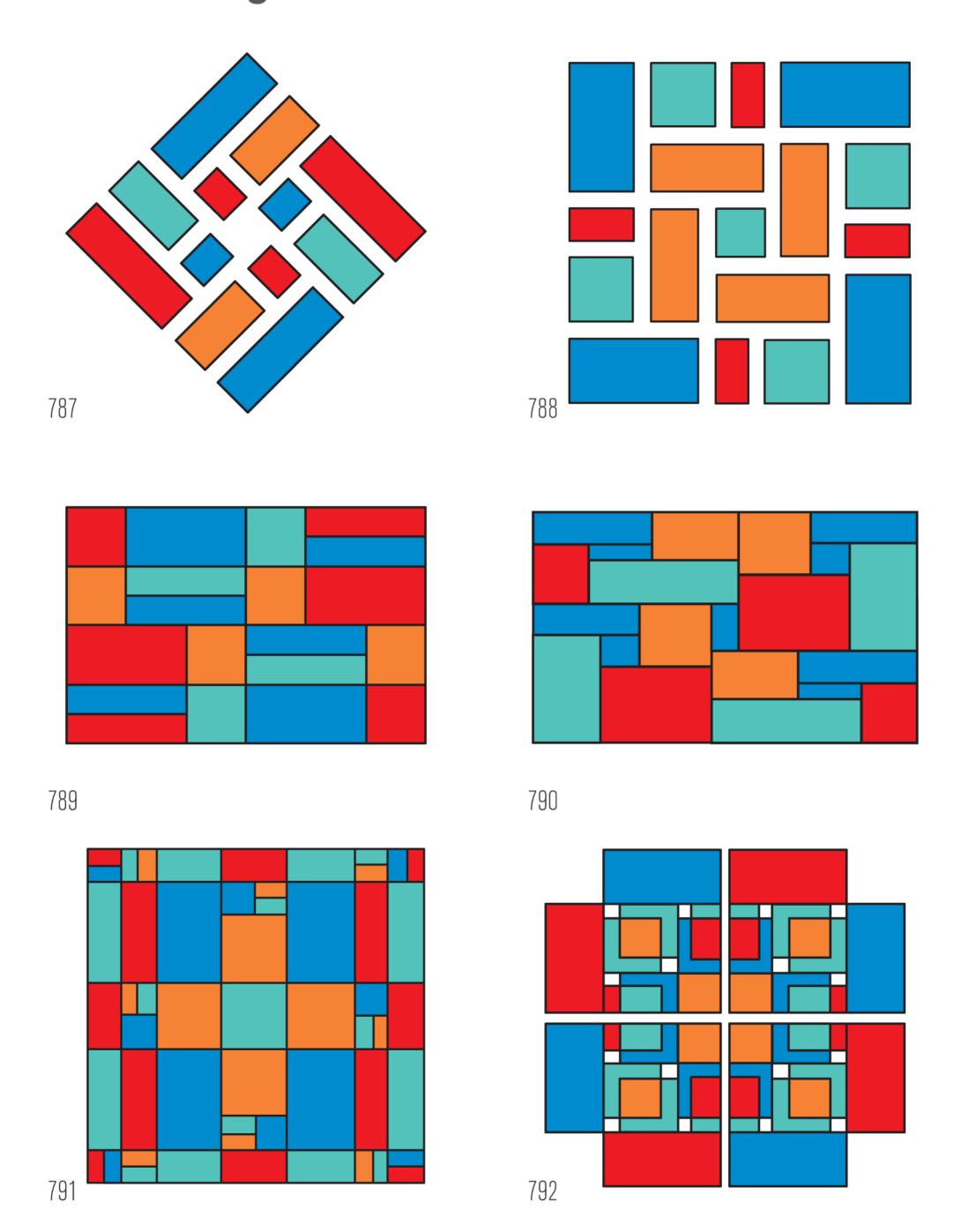


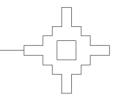
Question Shape



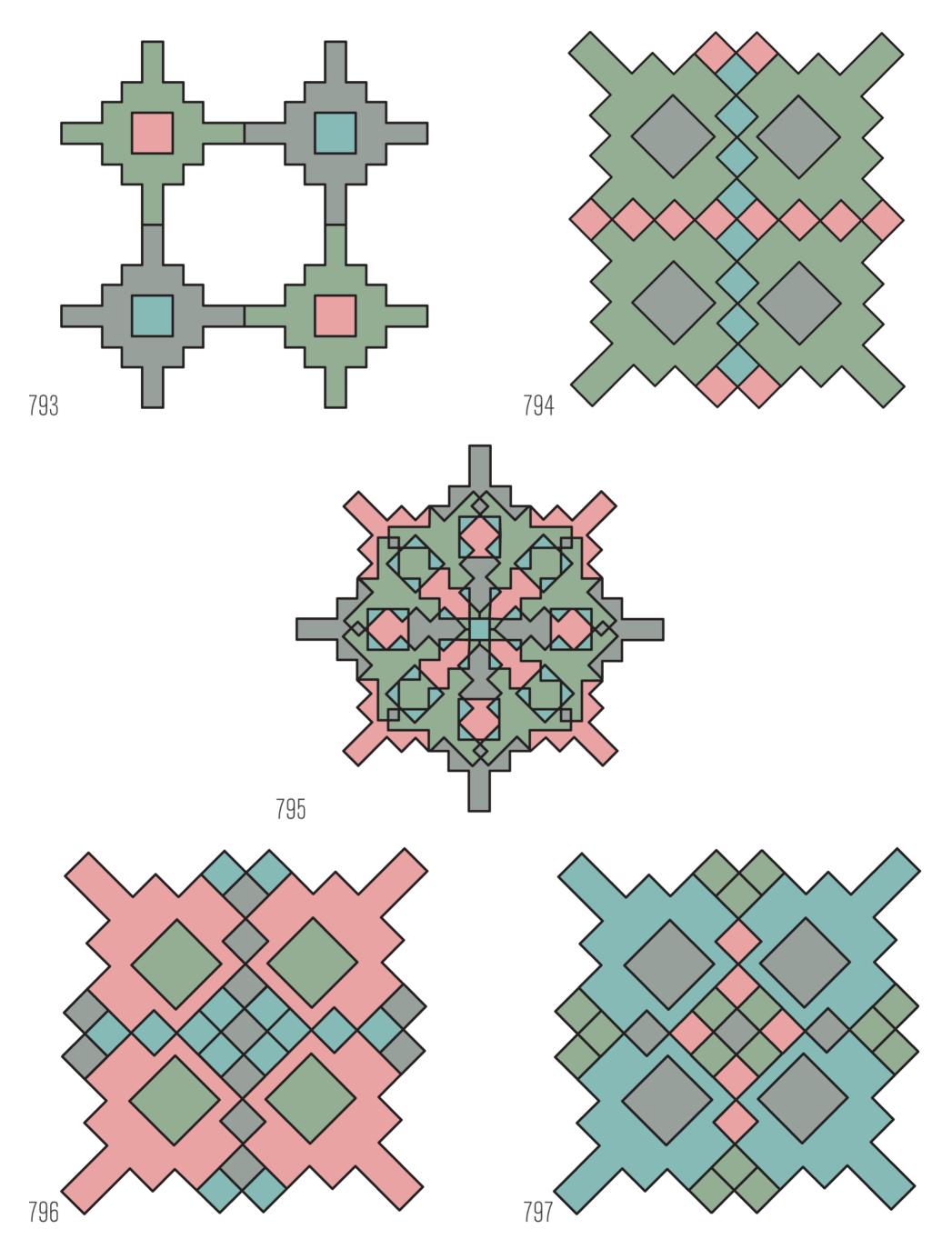


Rectangles

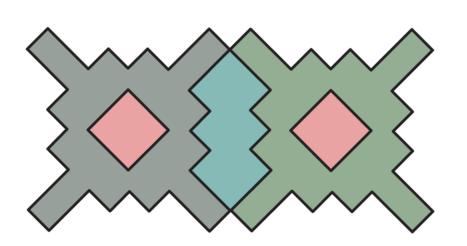


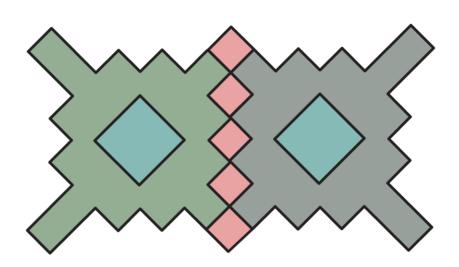


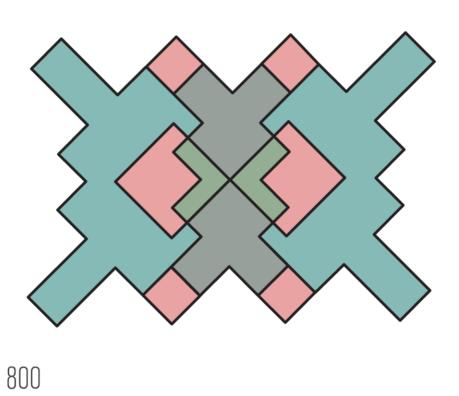
Reticules

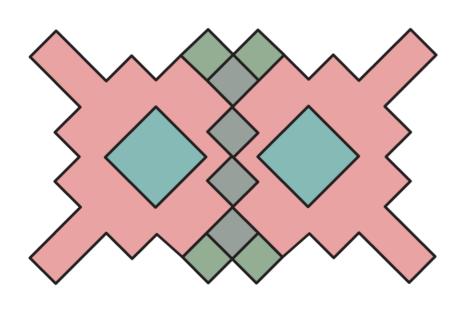


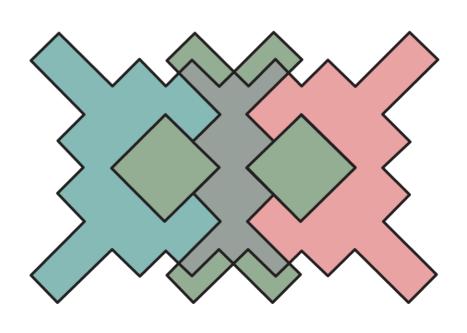
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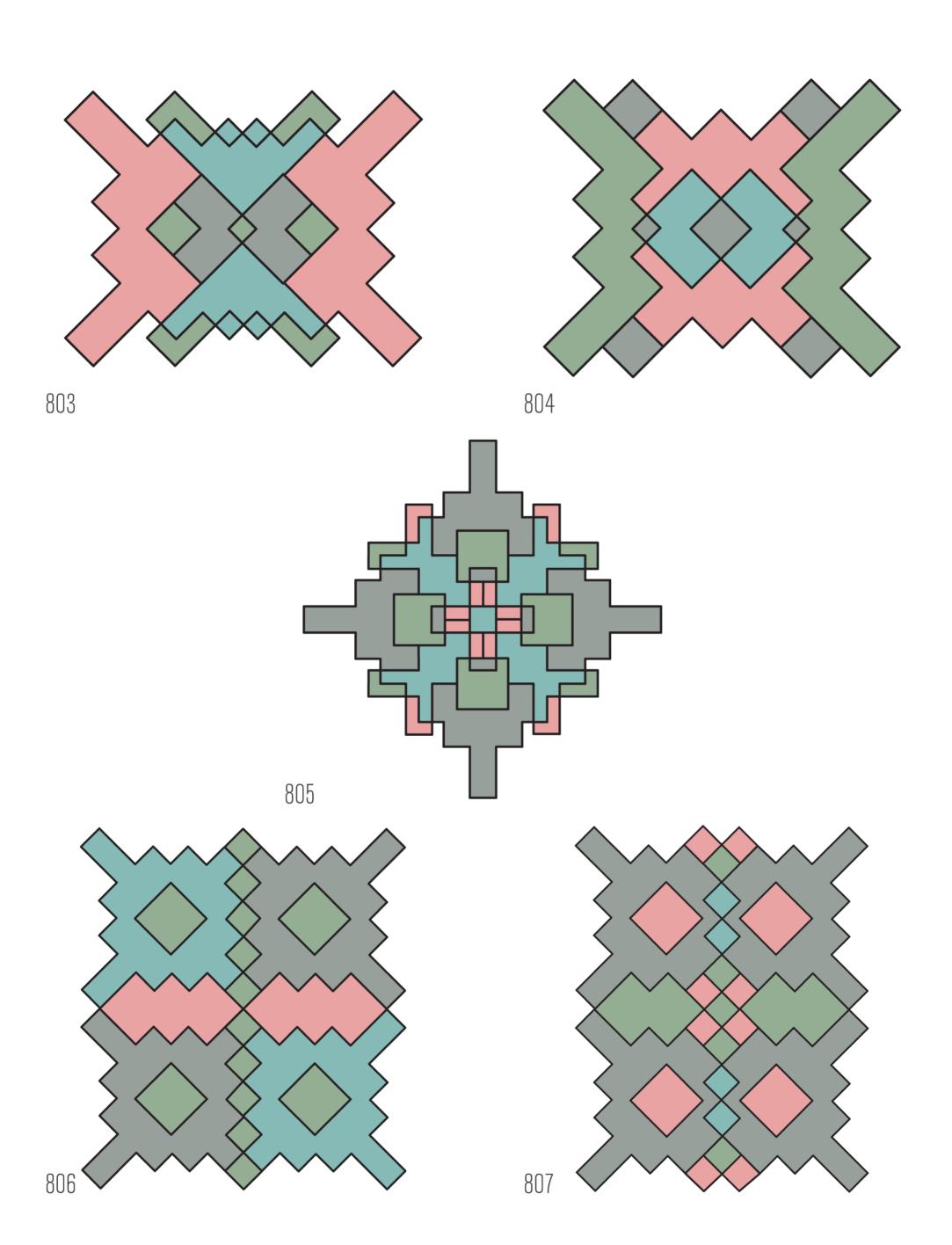




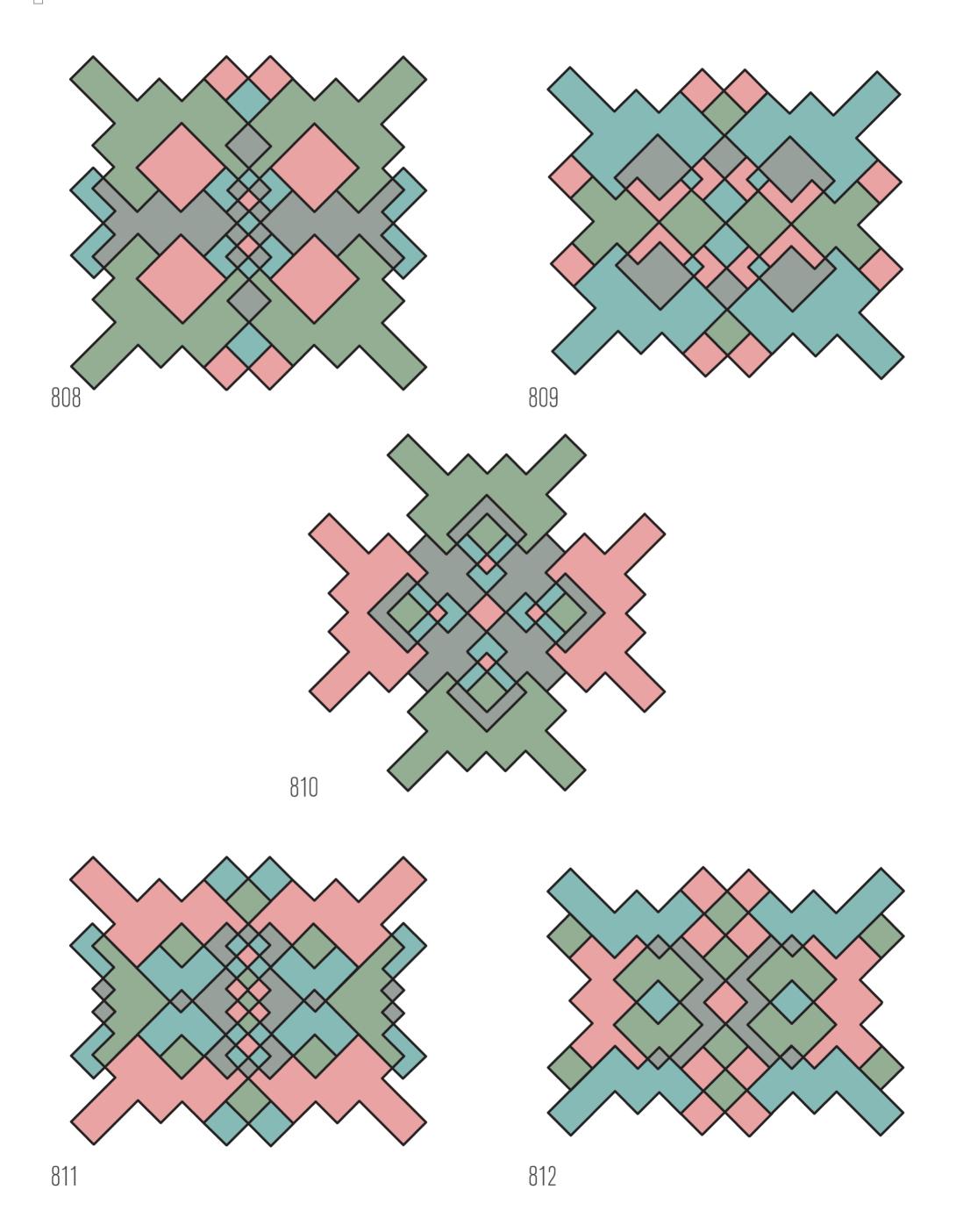


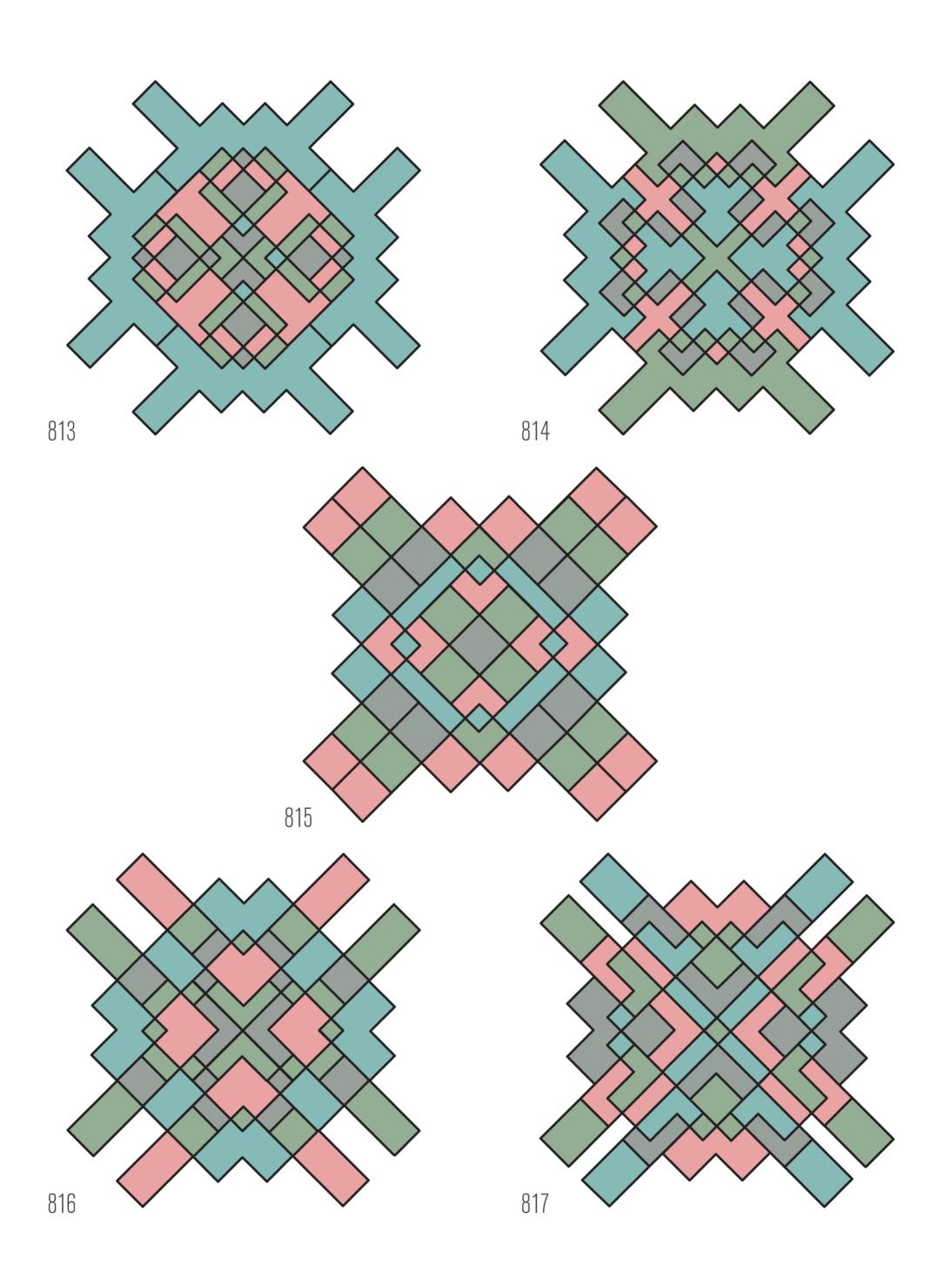


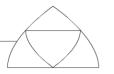




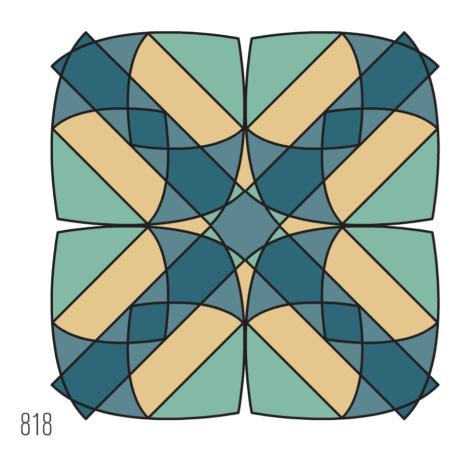
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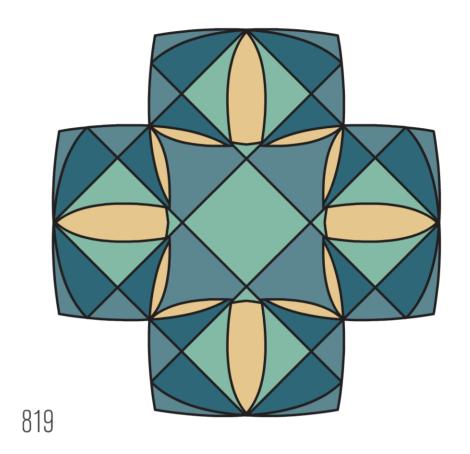


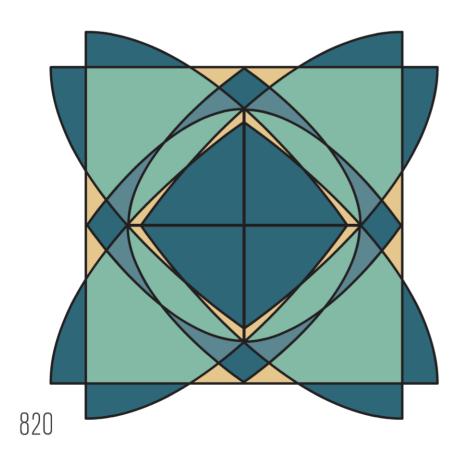


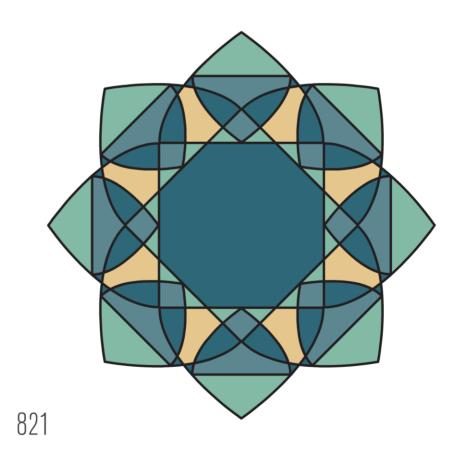


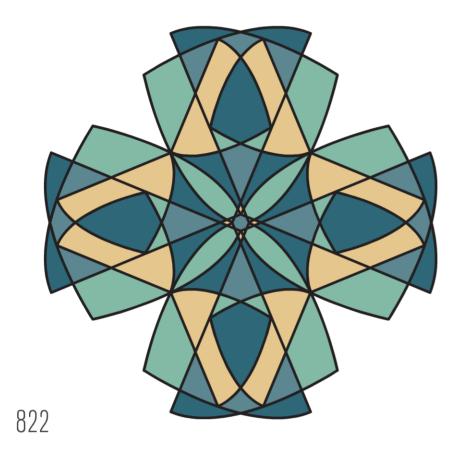
Rounded Triangles

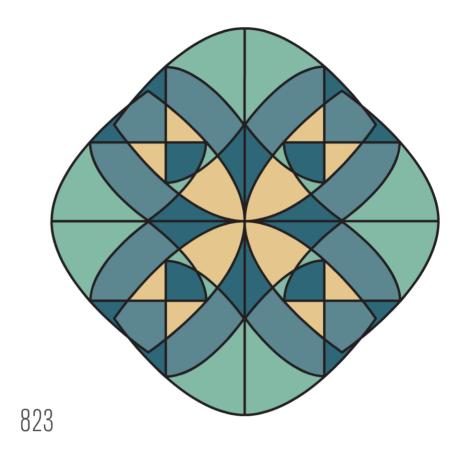


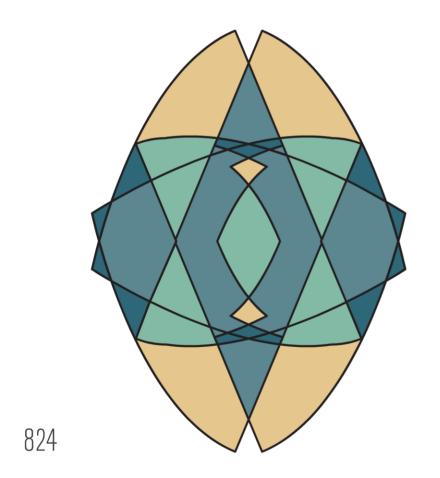


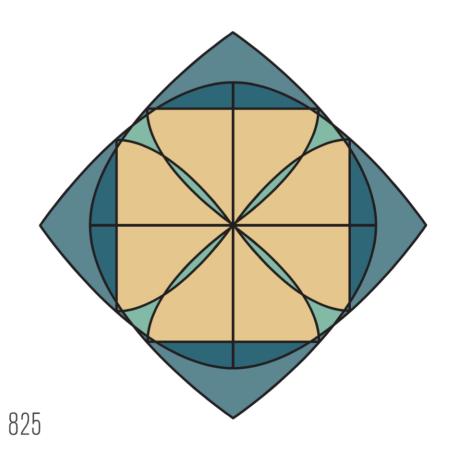




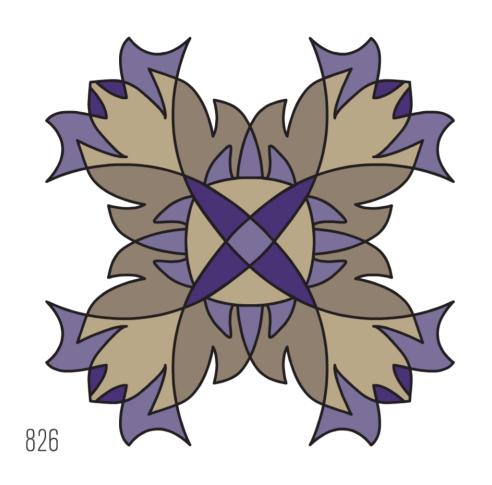


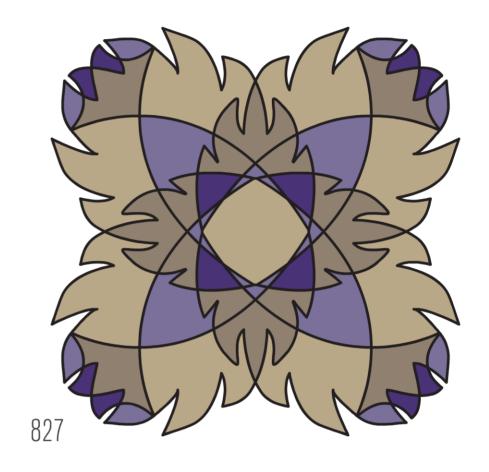


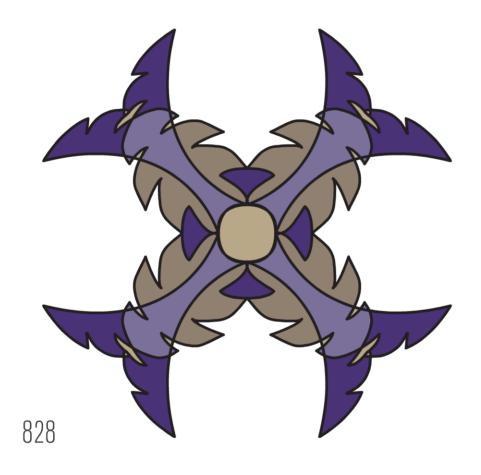


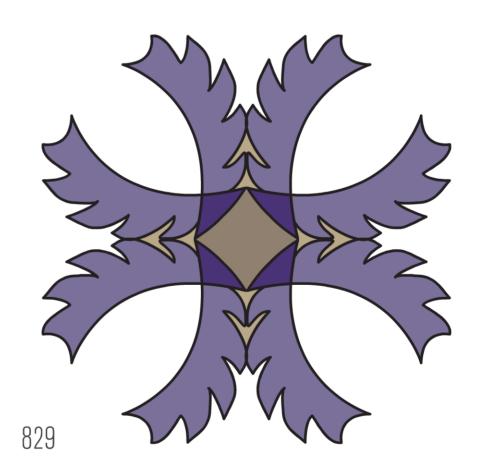


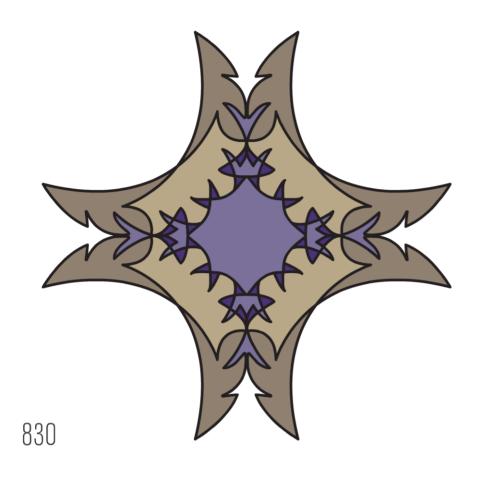
Saw Leaf

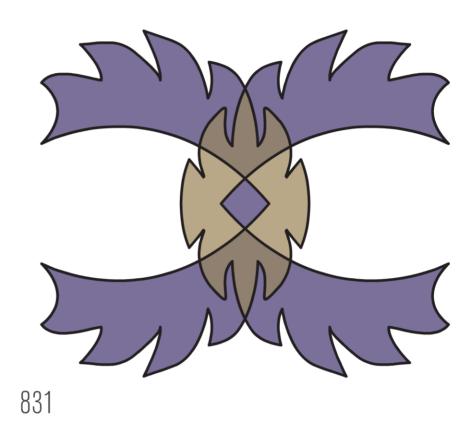


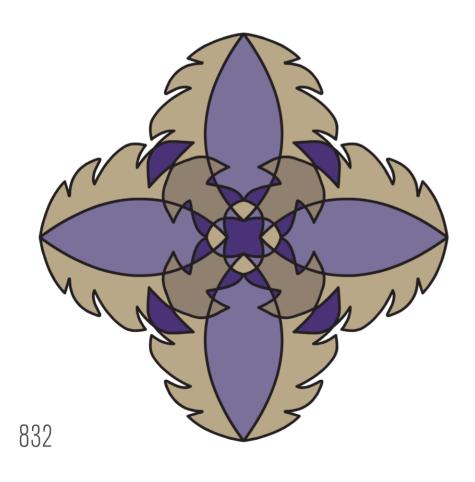


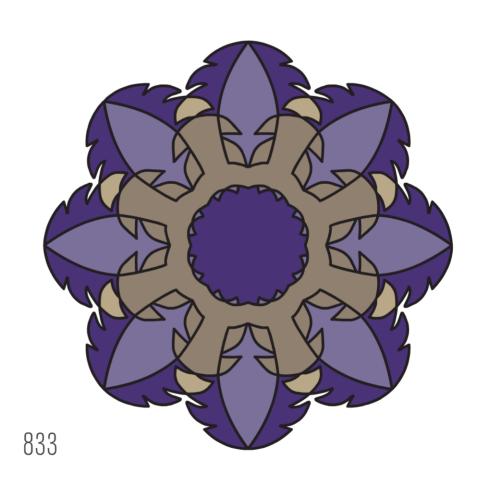




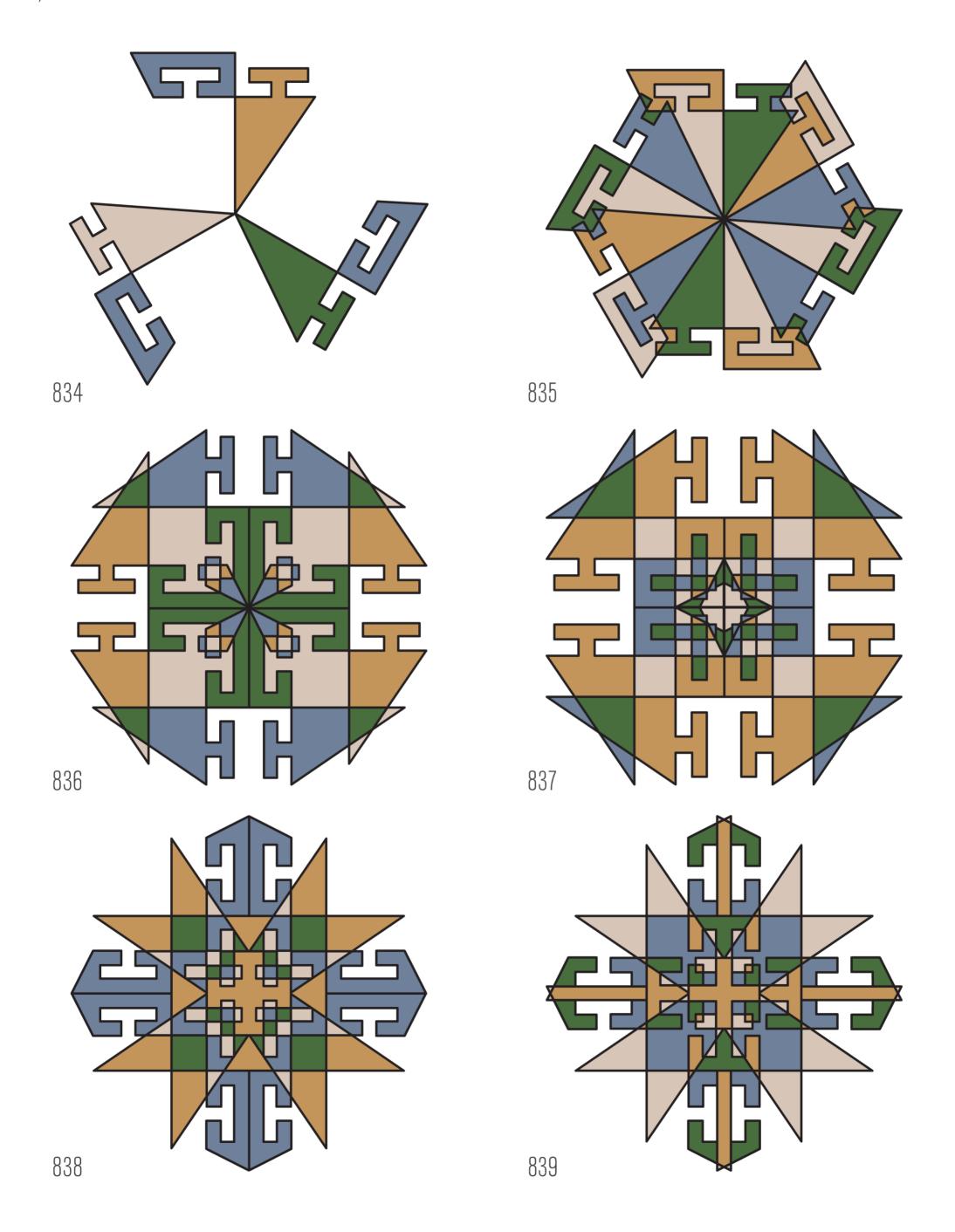






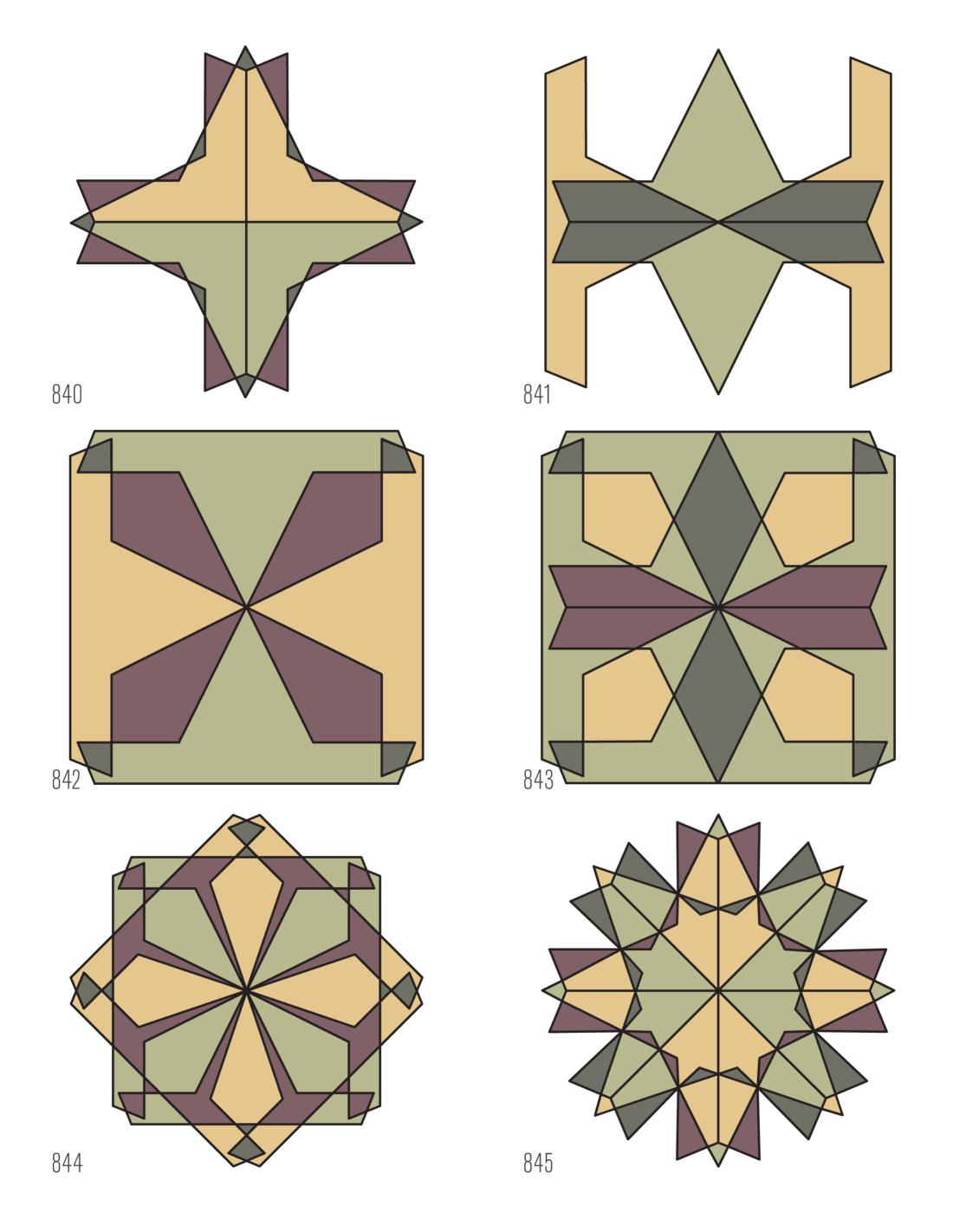


Shield Patterns



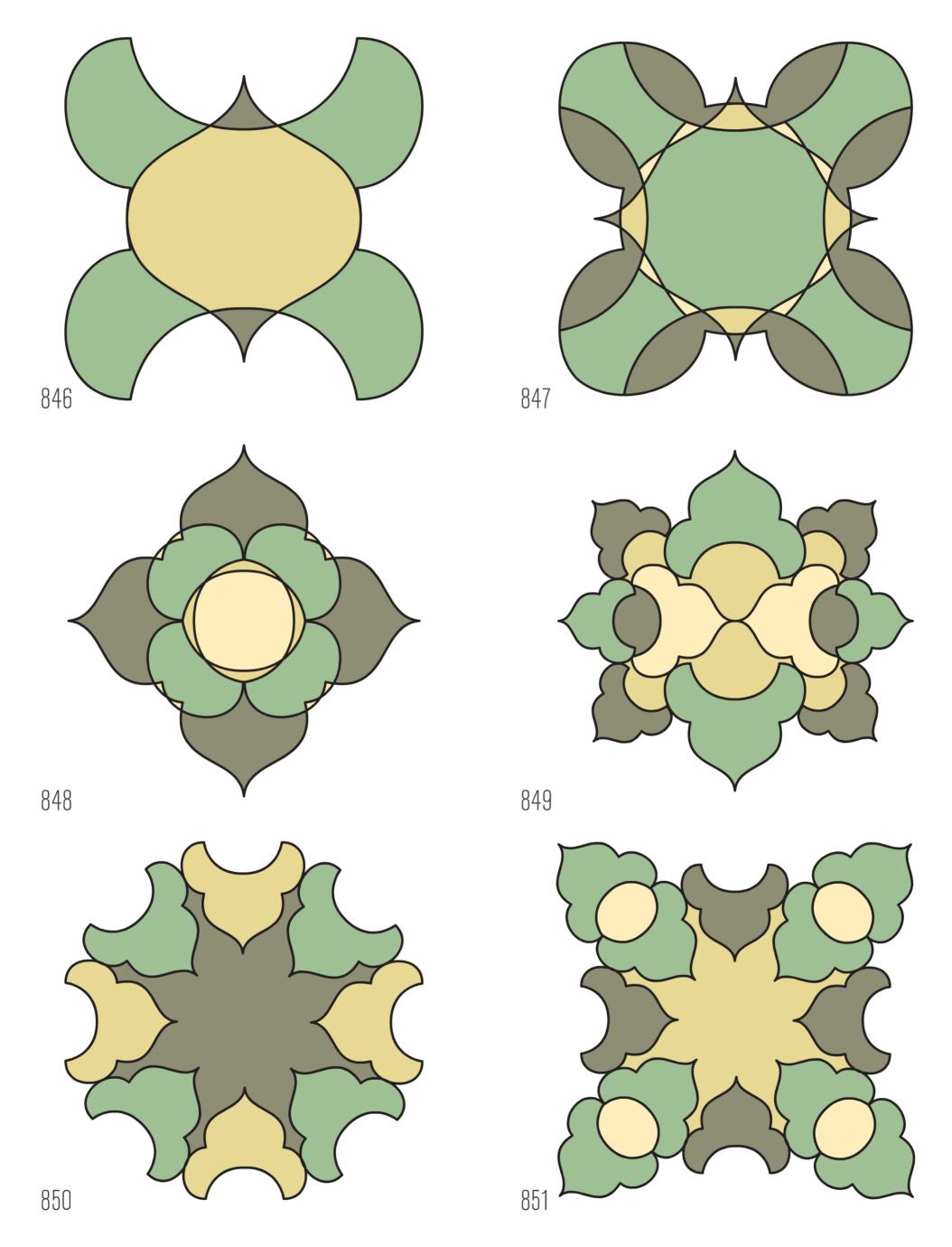


Sombrero



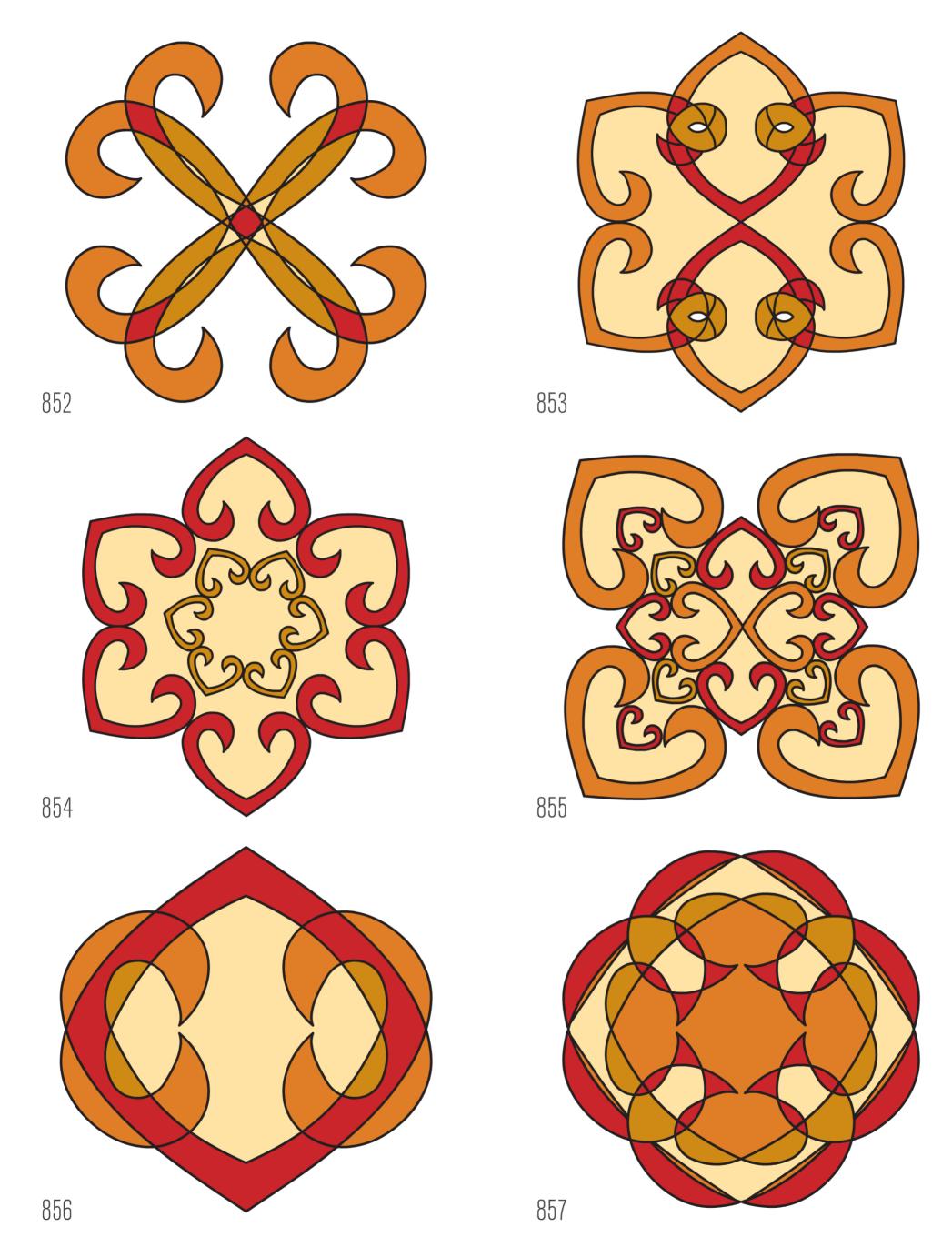


Spade

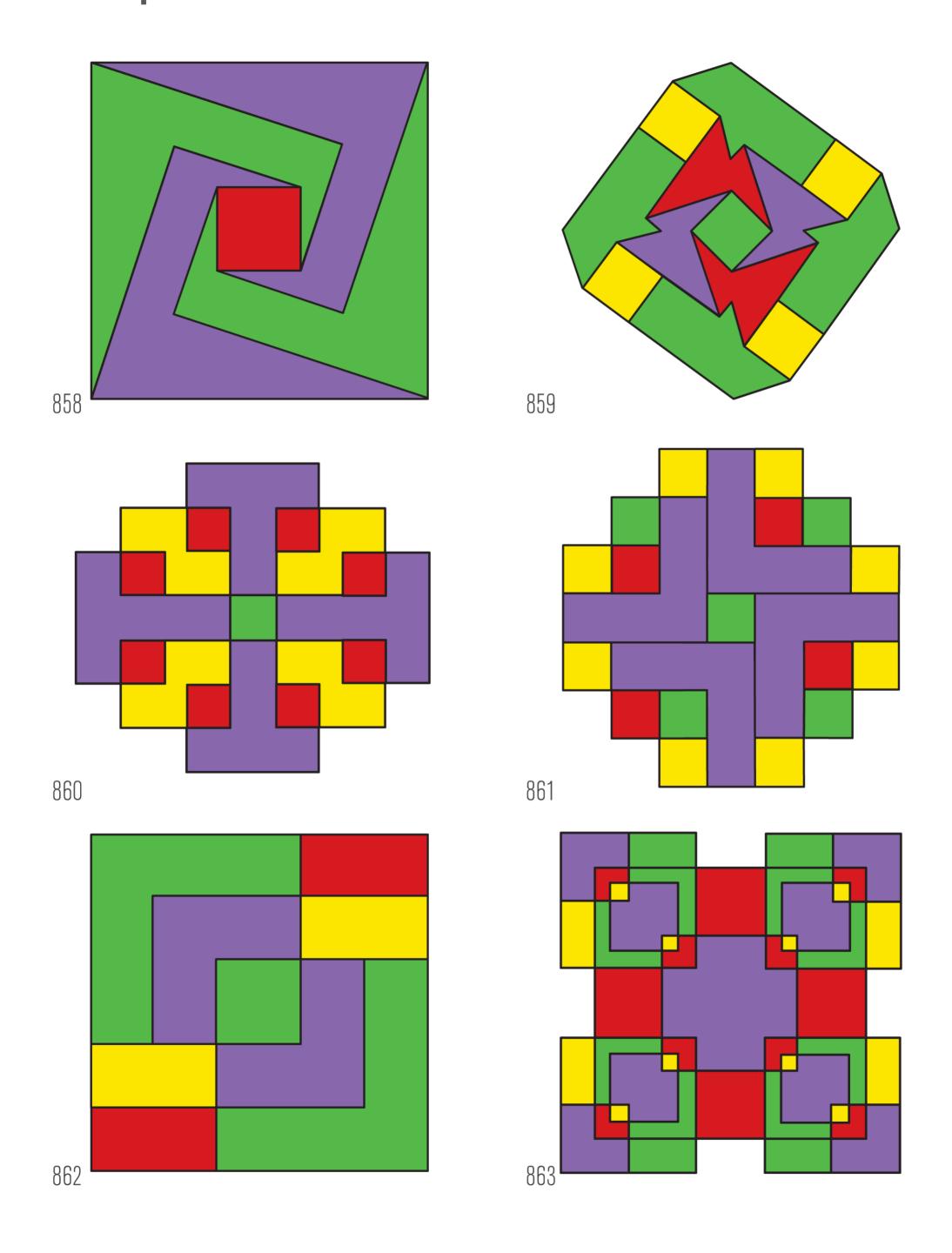




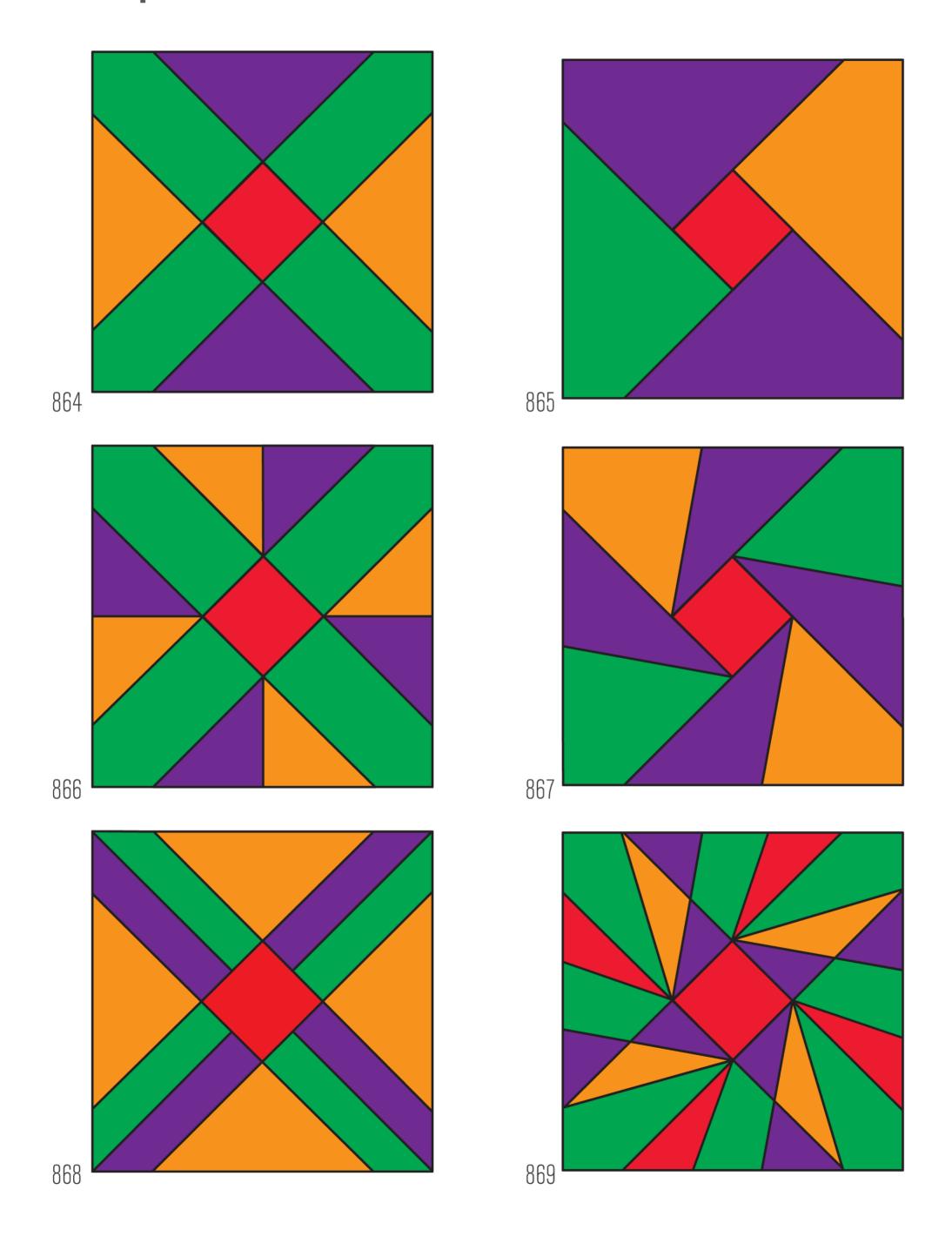
Spade 2



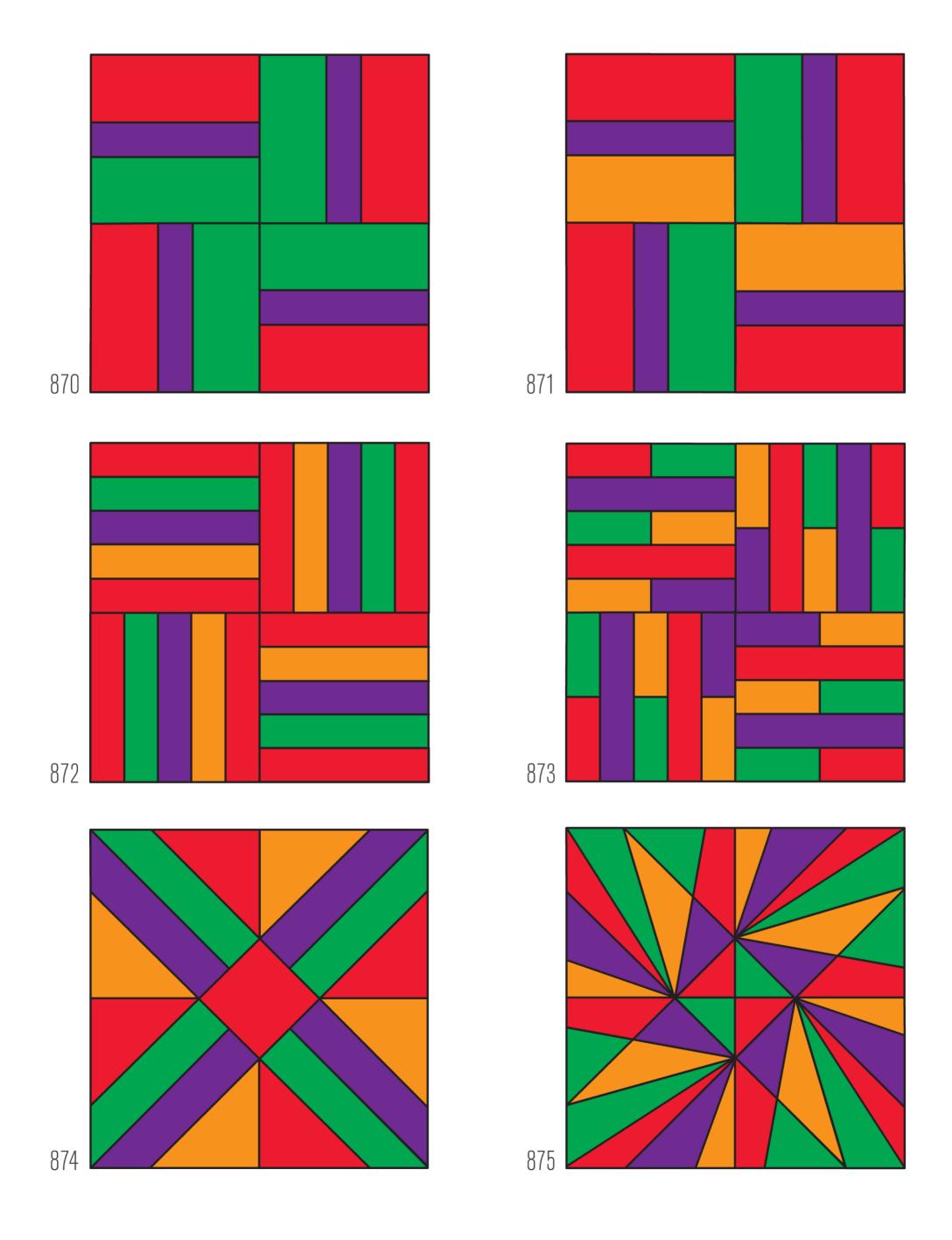
Squares



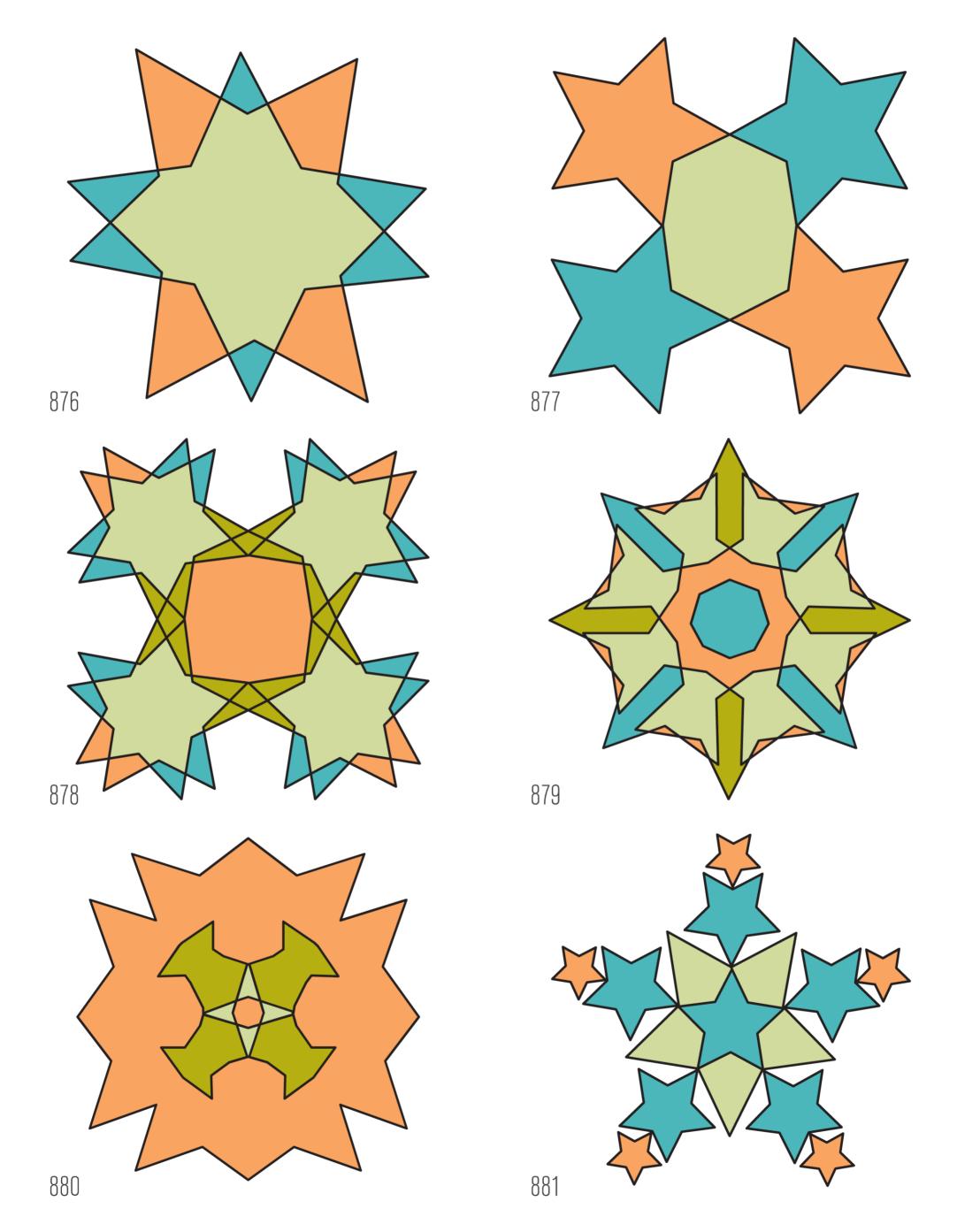
Squares Divided



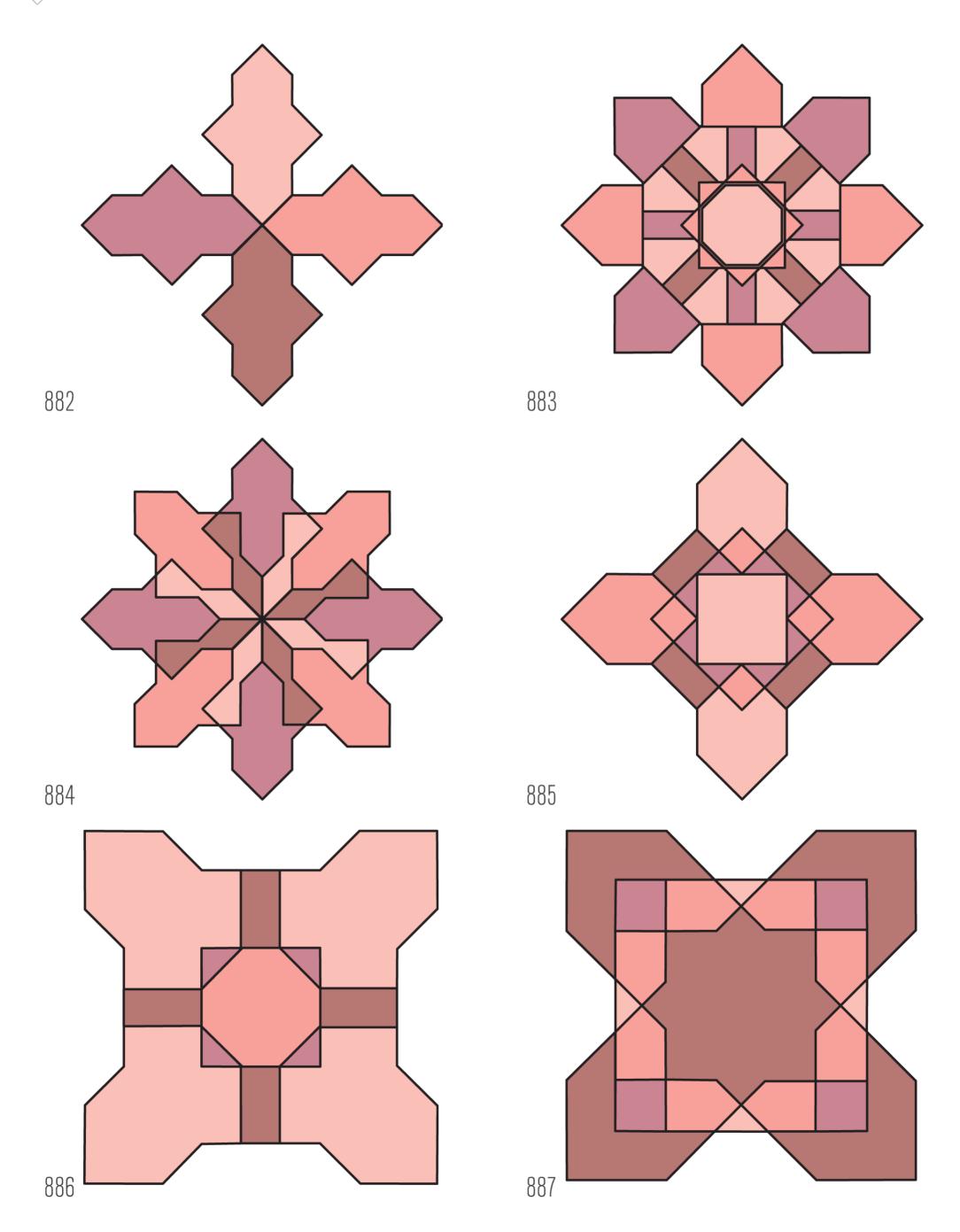
Squares Divided





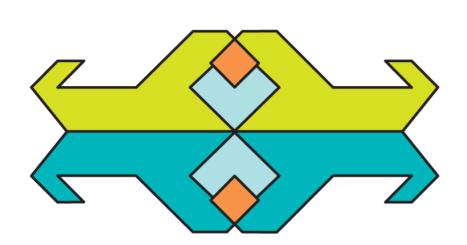


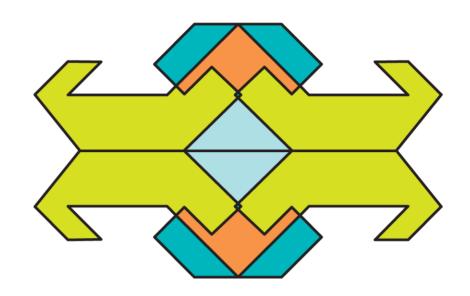
Thorns



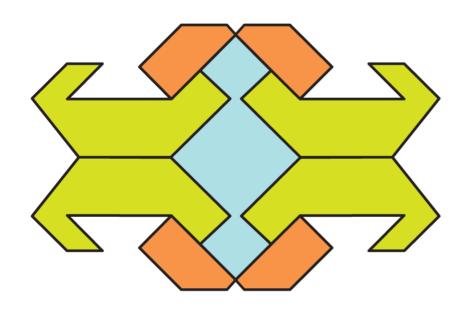


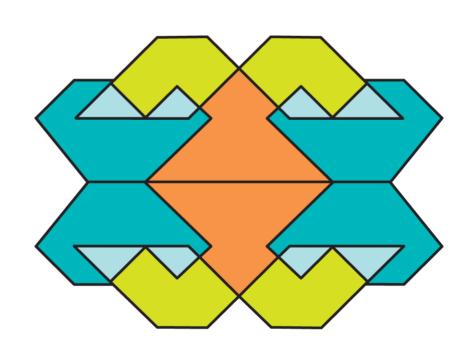
Top Dogs





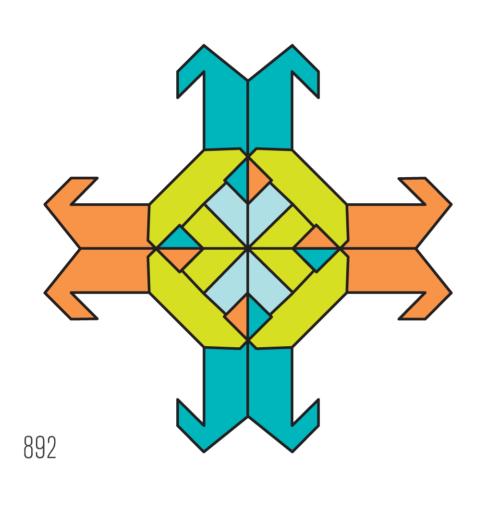
888

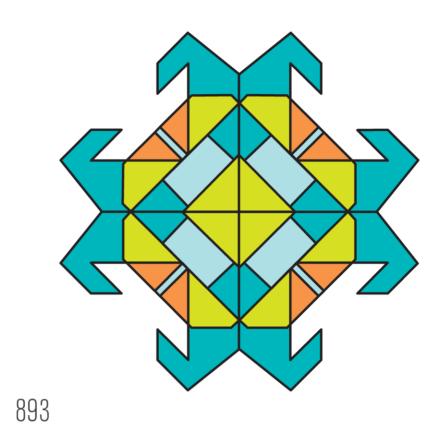


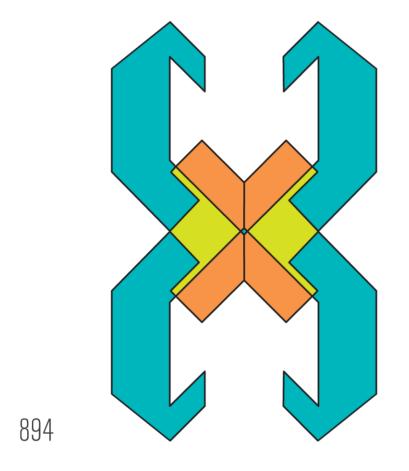


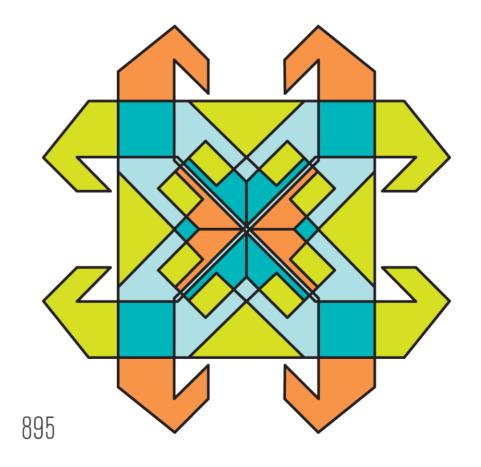
890 891

Top Dogs

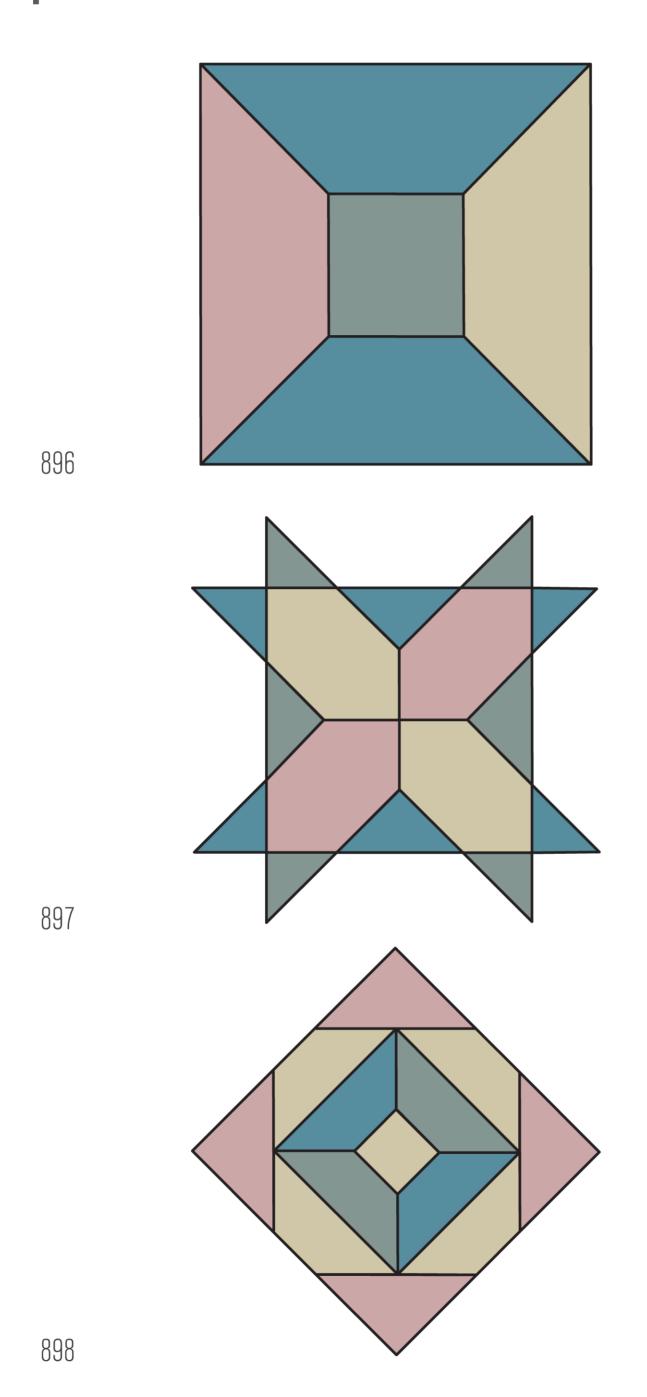




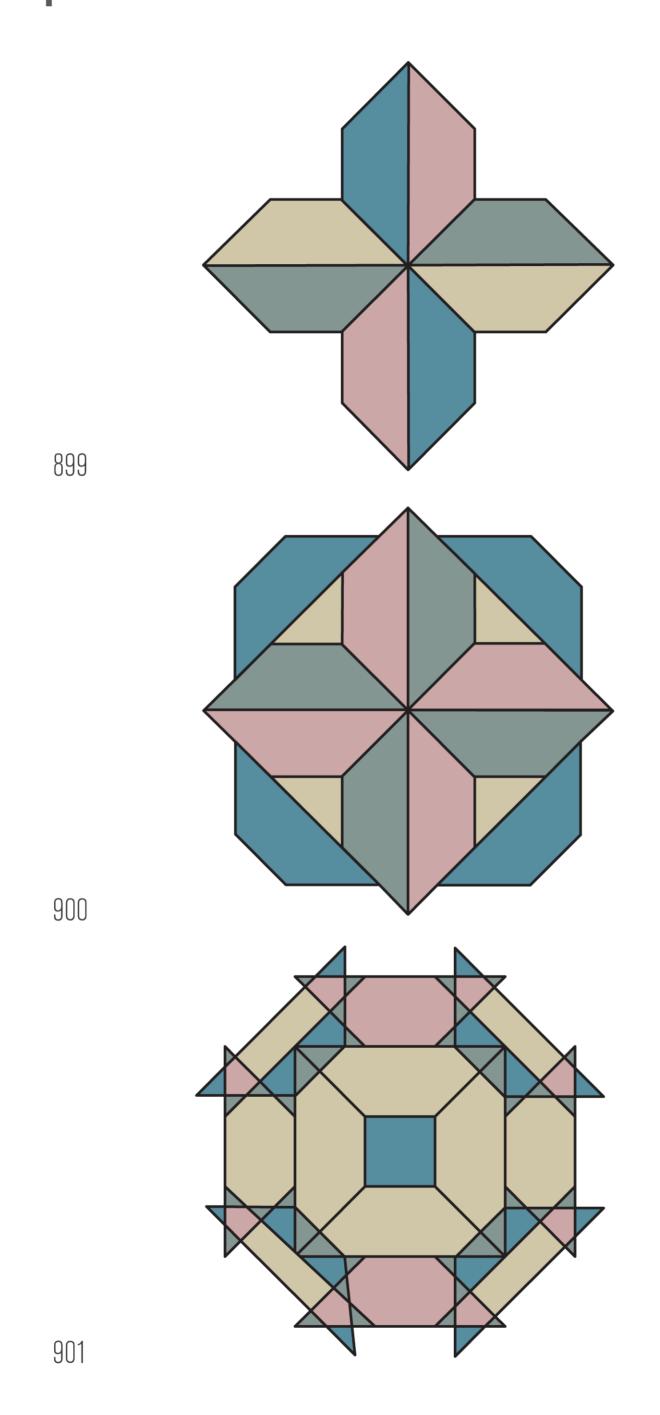




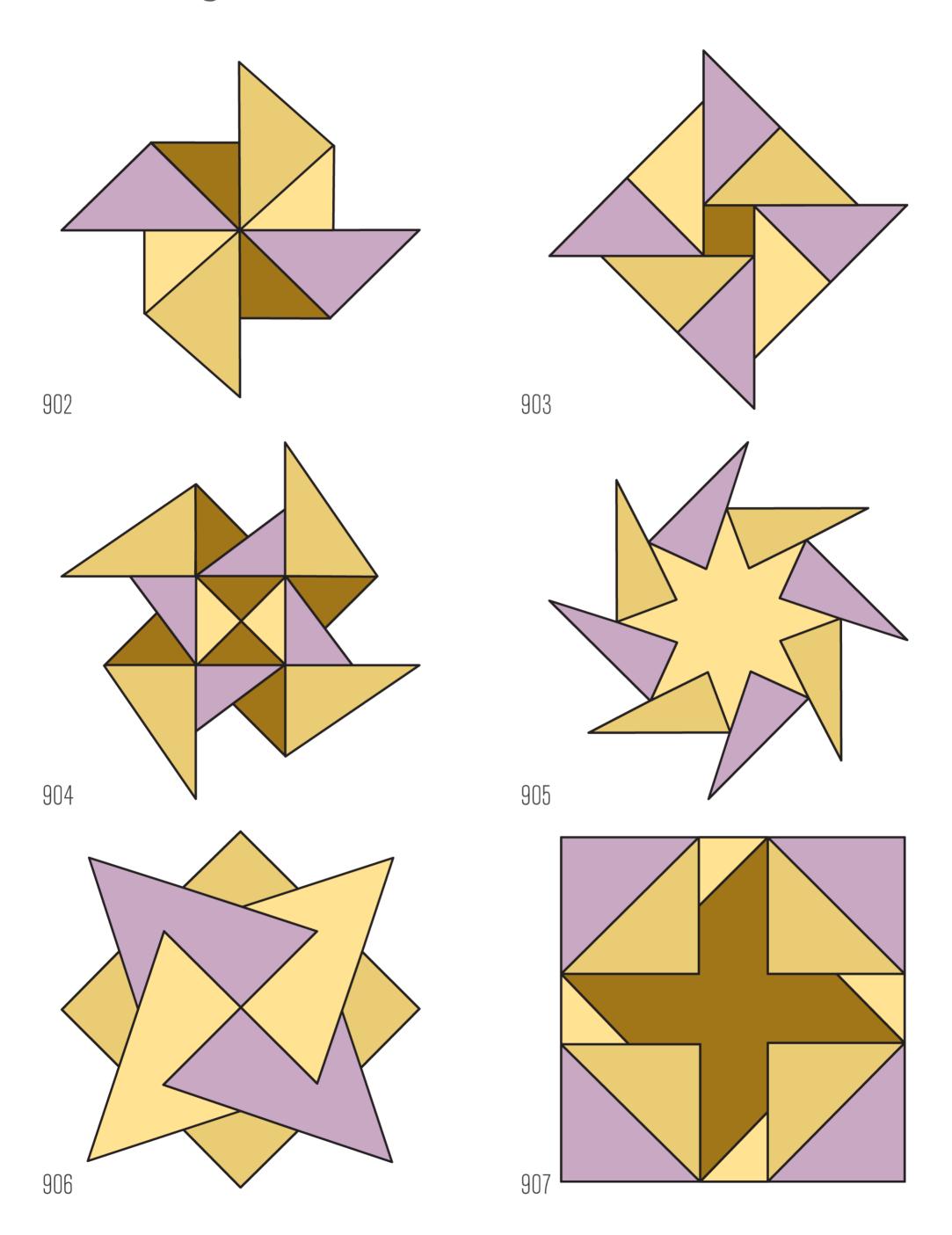
Trapezoids

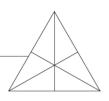


Trapezoids

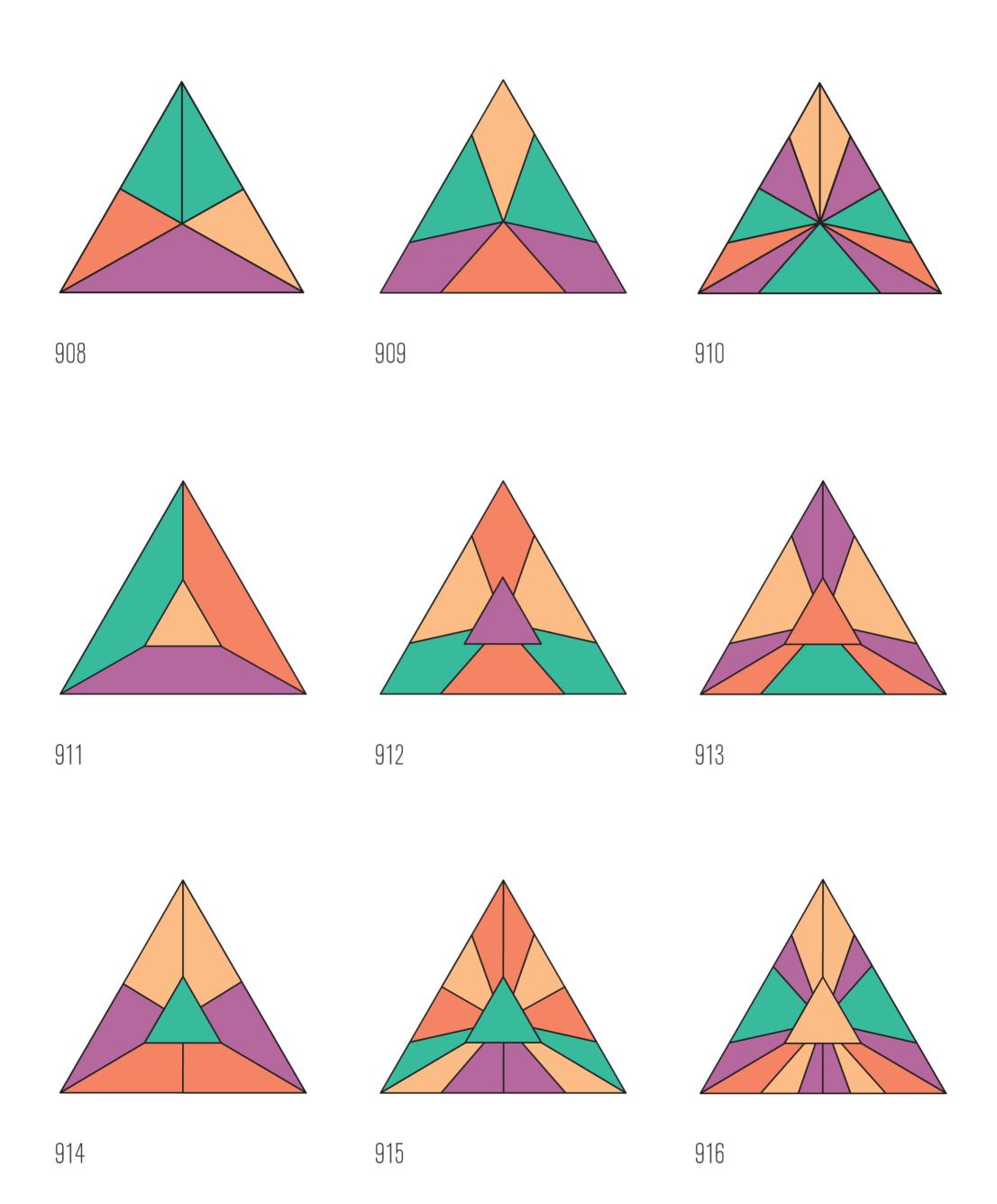


Triangles

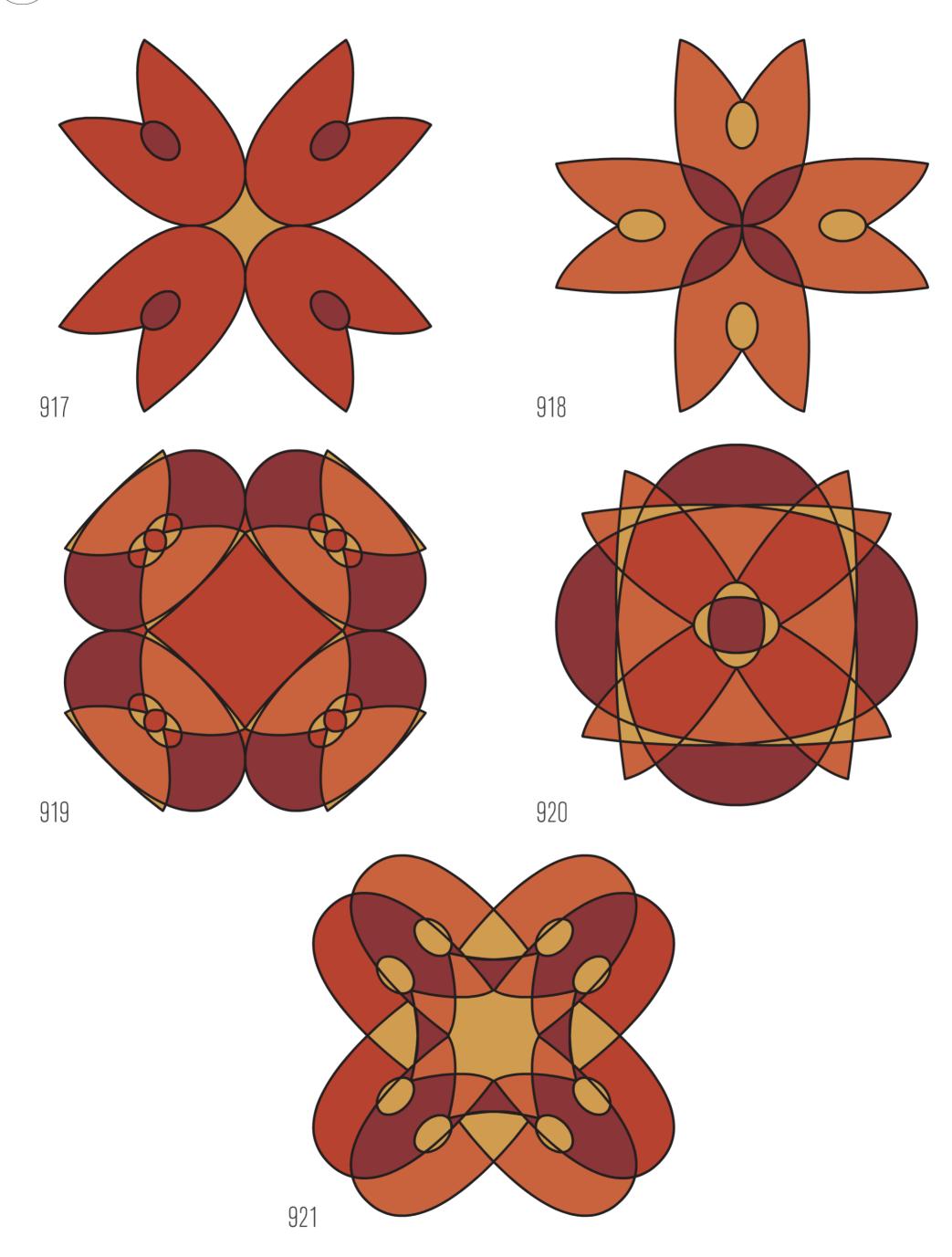




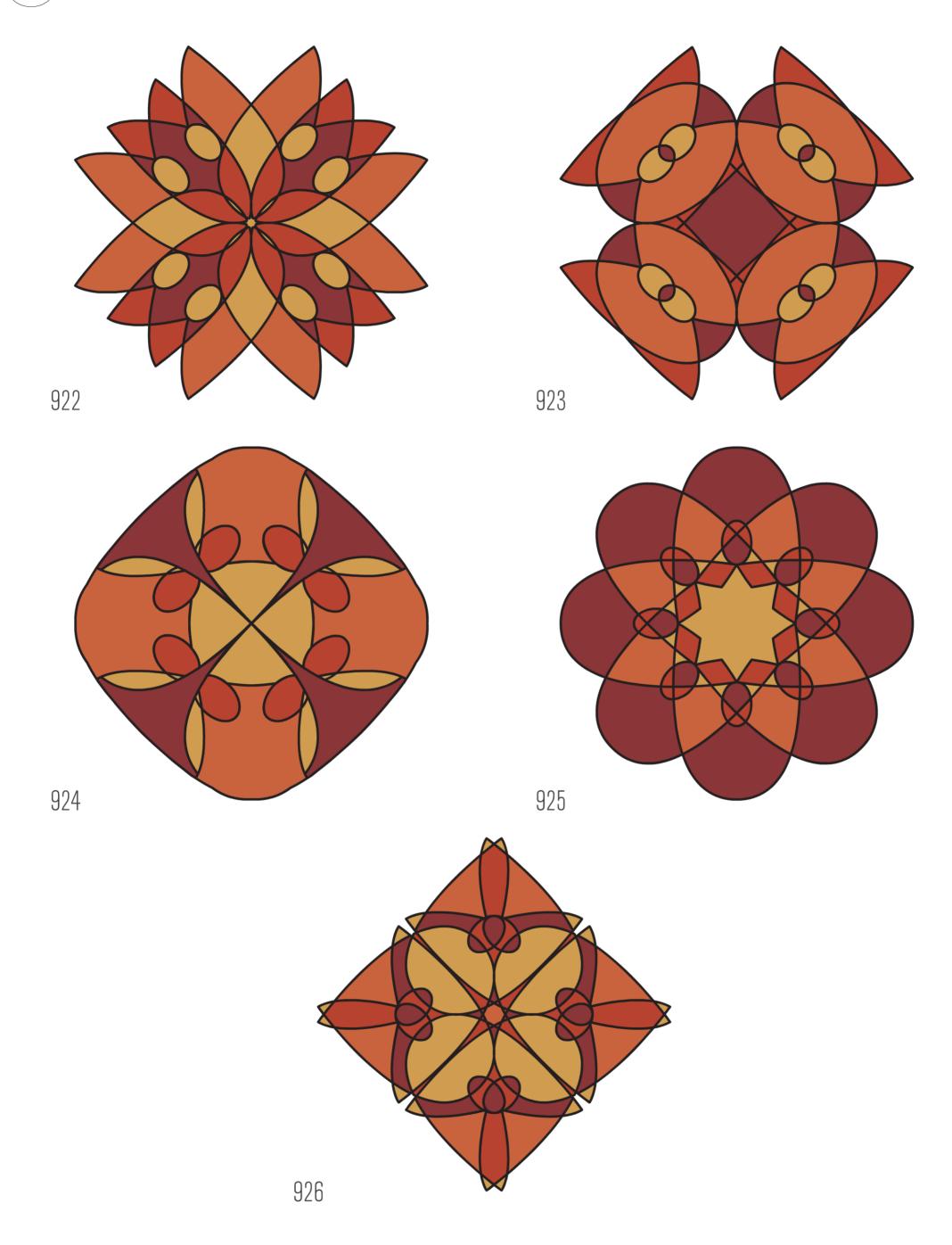
Triangles Divided



Tulip

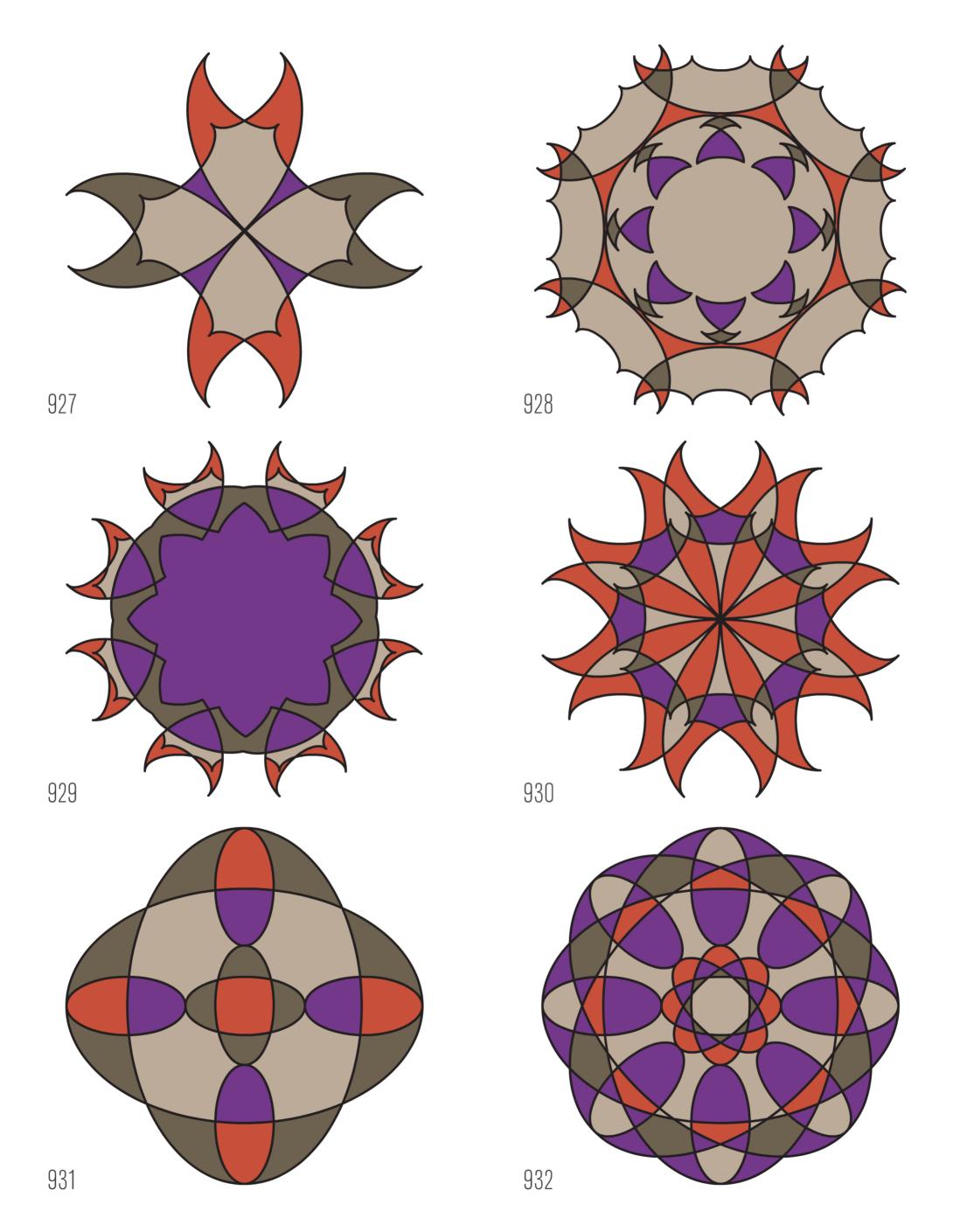


Tulip

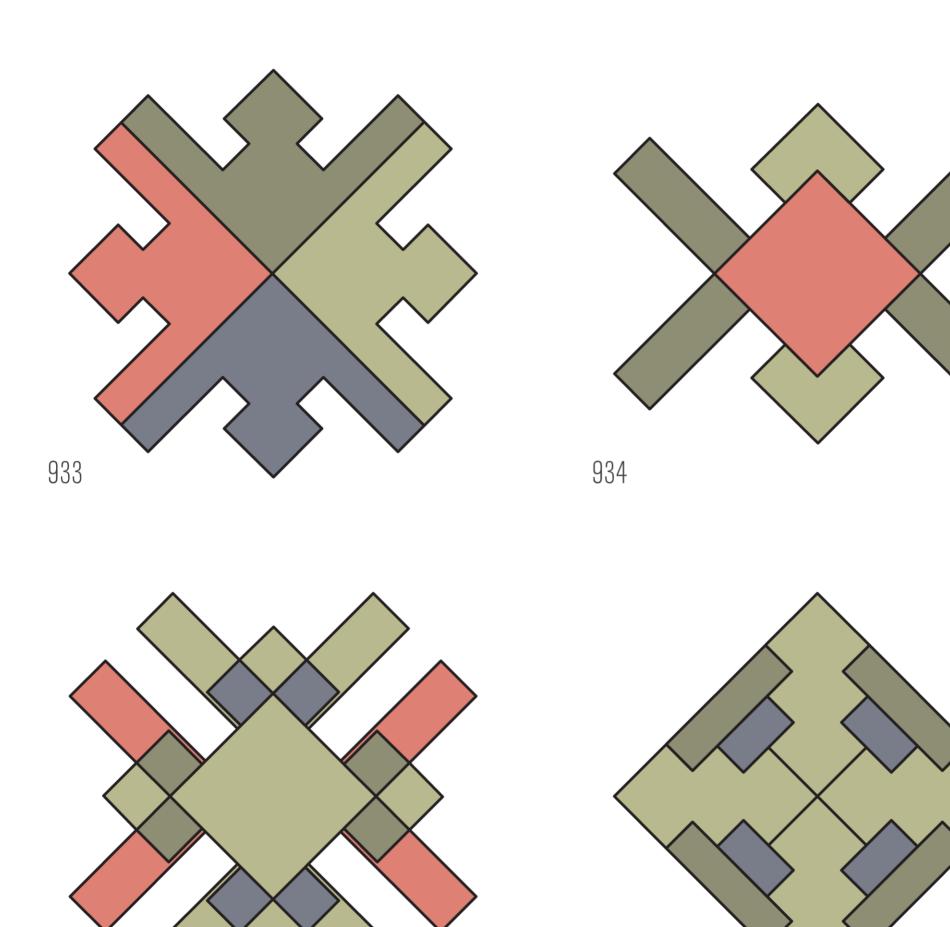




Umbrellas

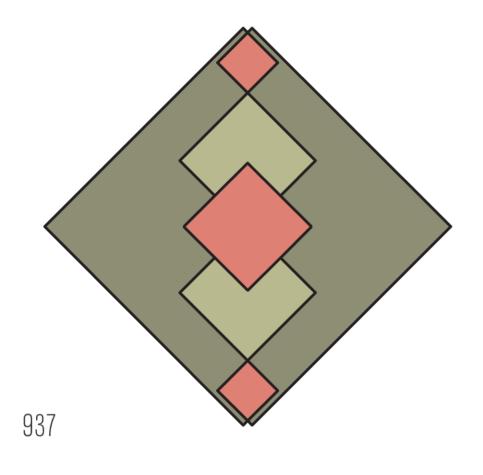


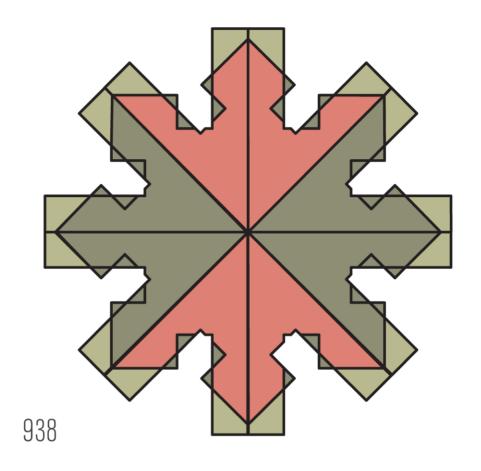
Up at Arms

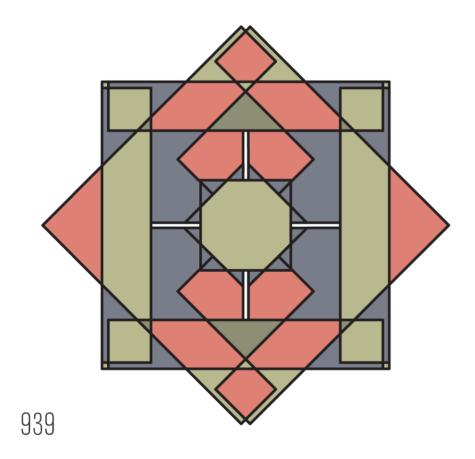


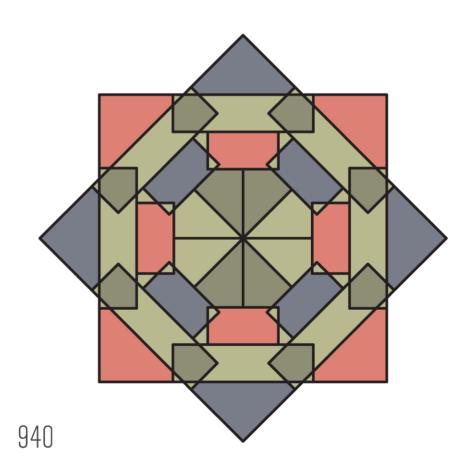
936

935

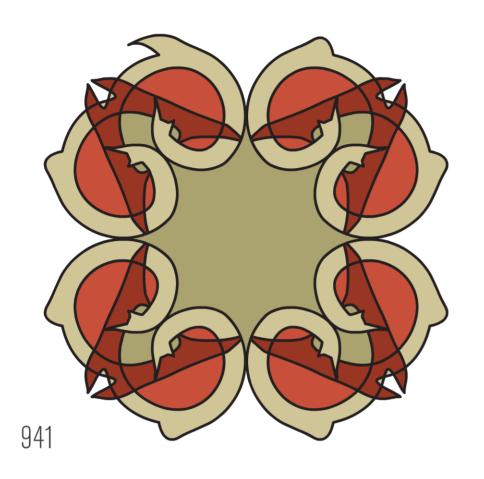


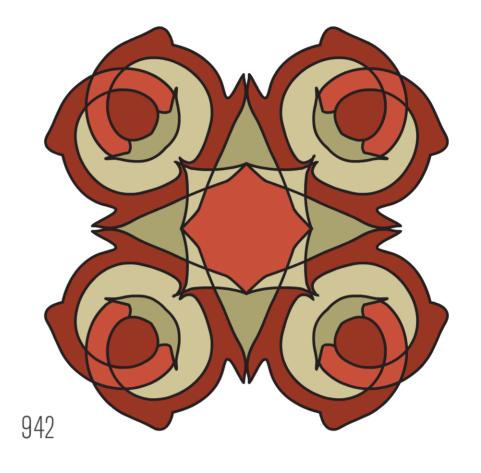


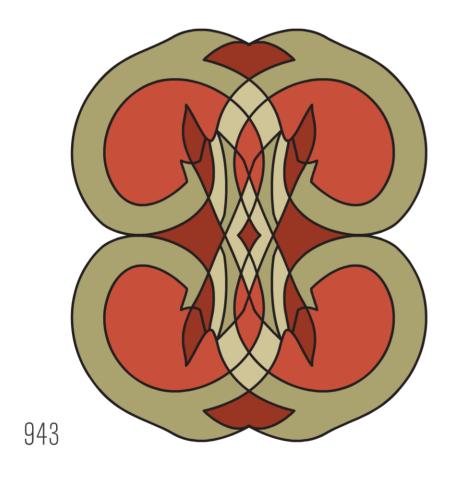


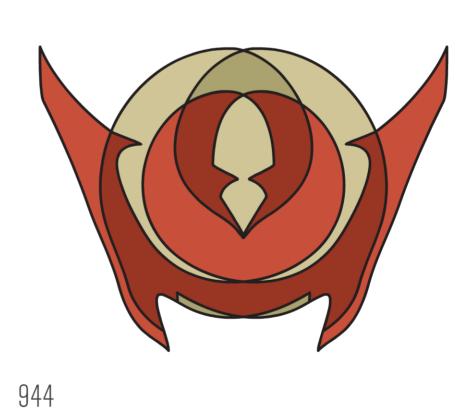


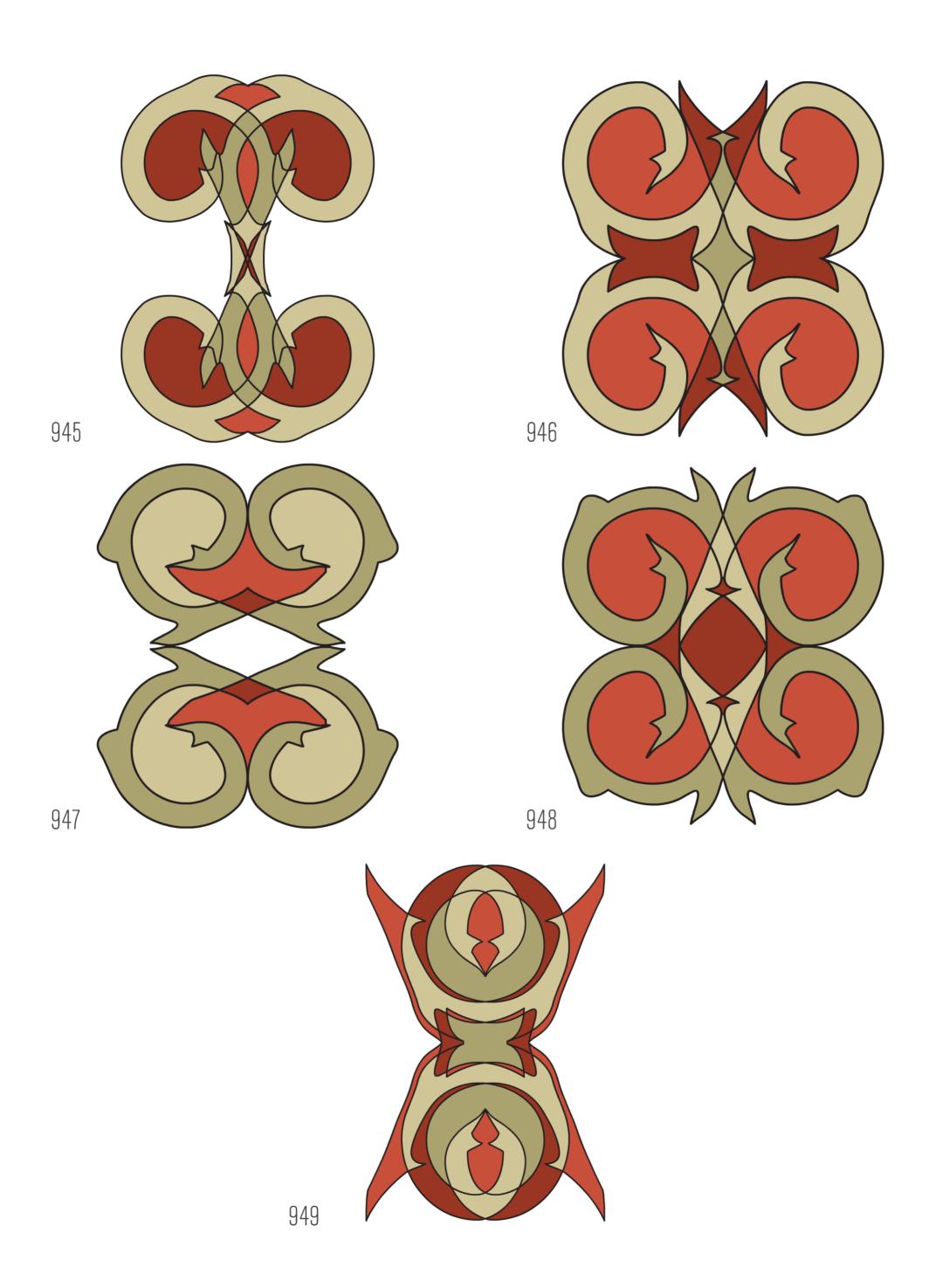
Vine Leaf



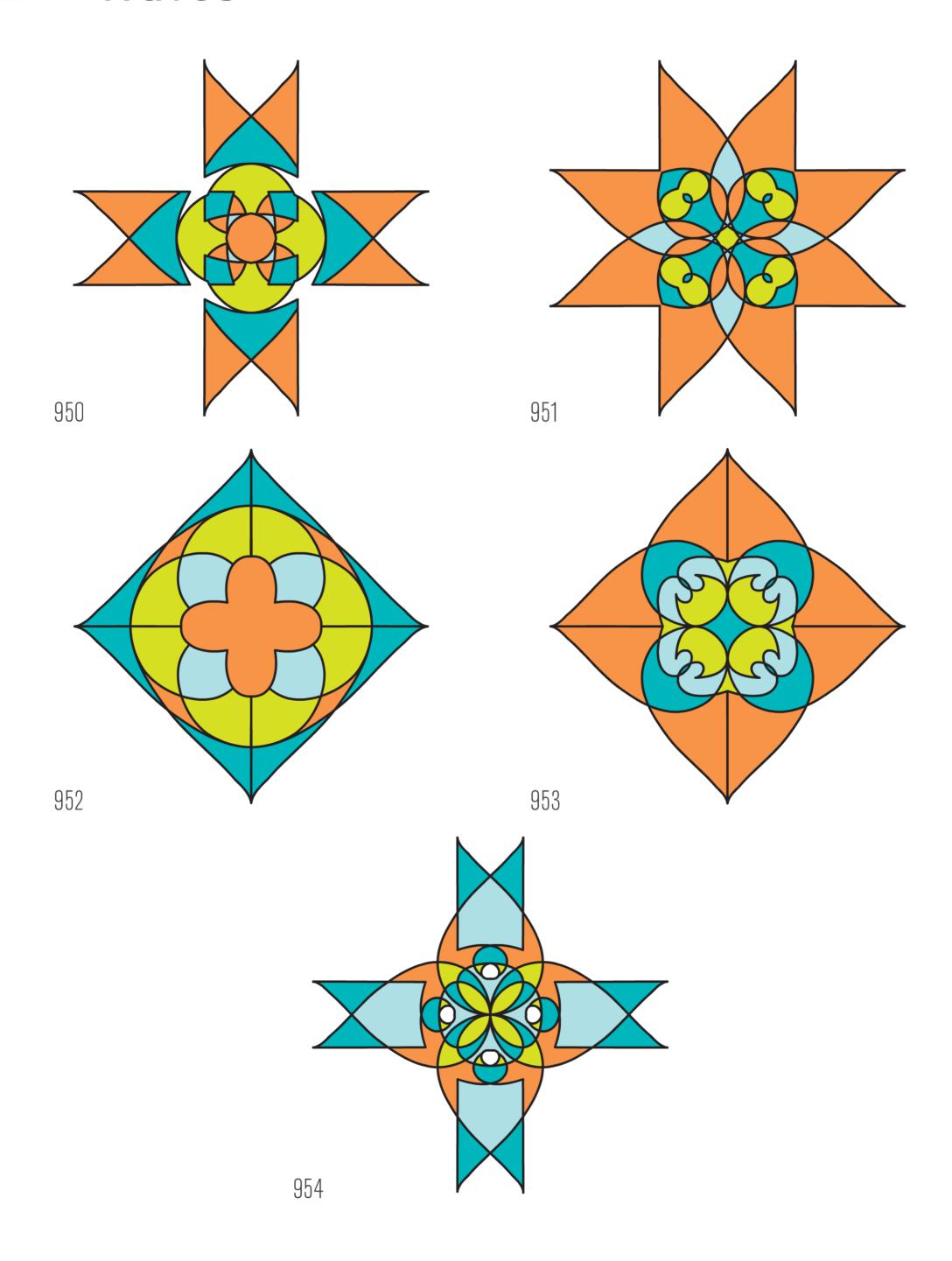


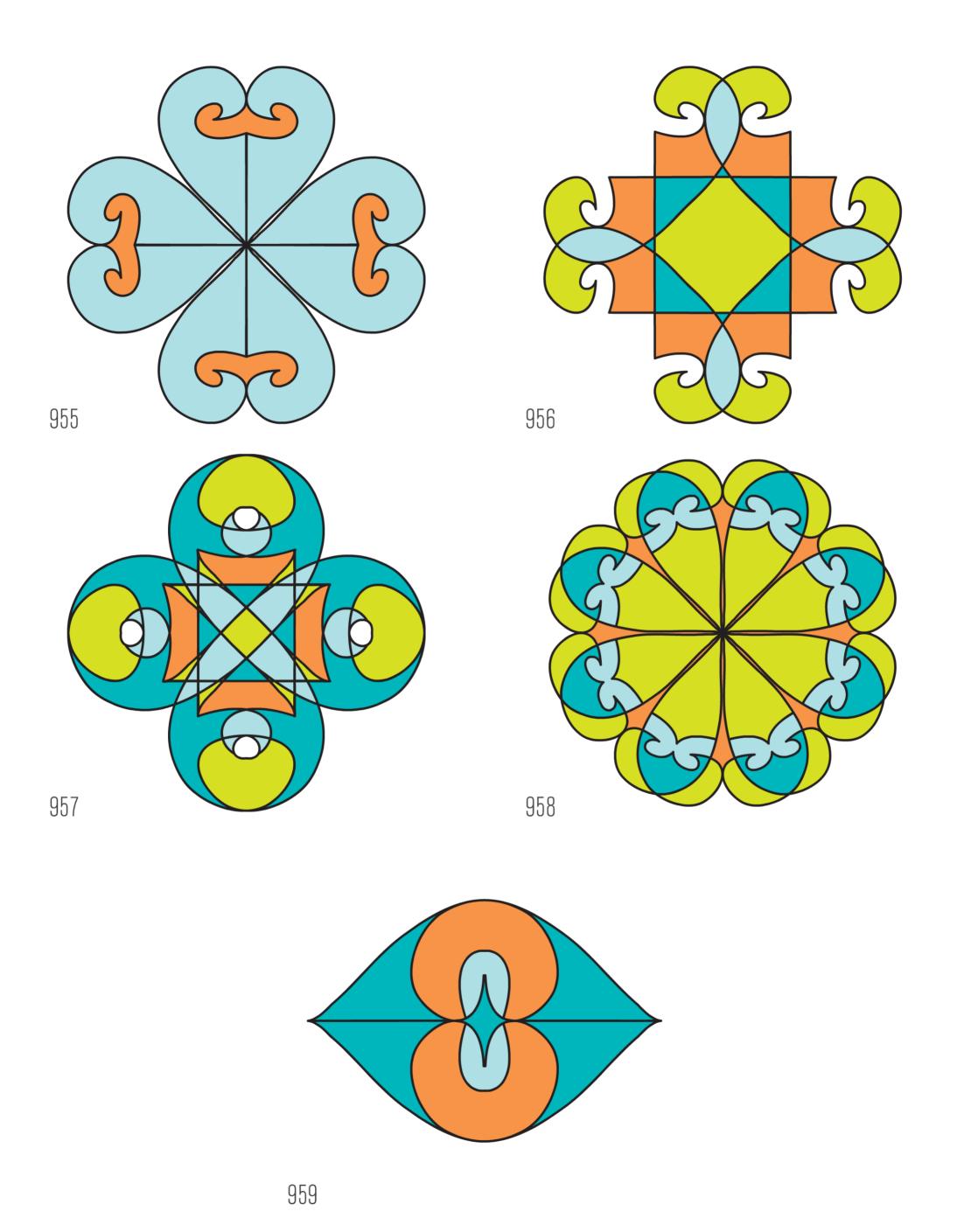


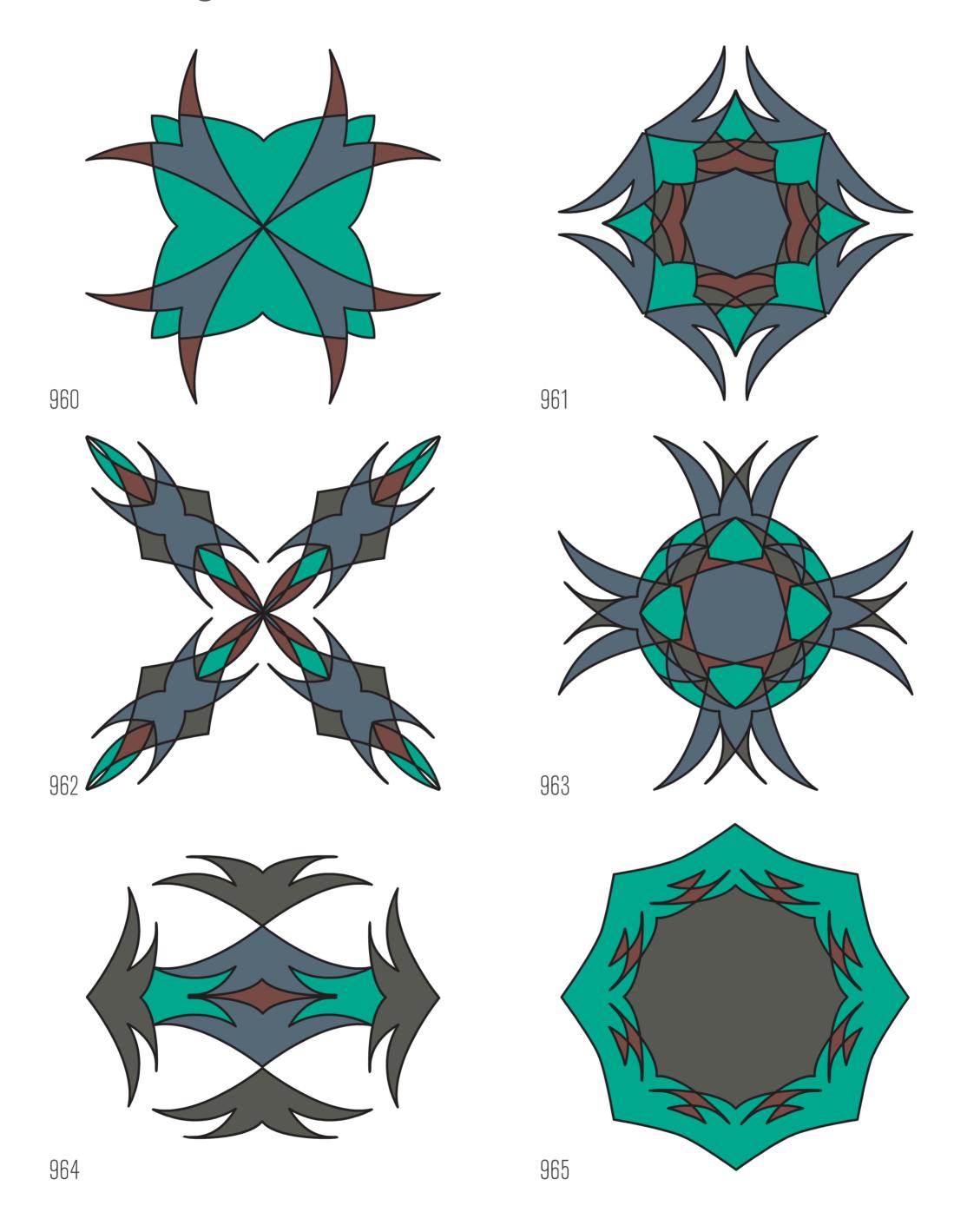


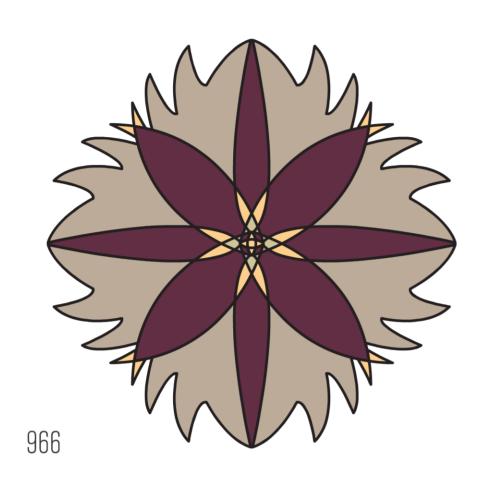


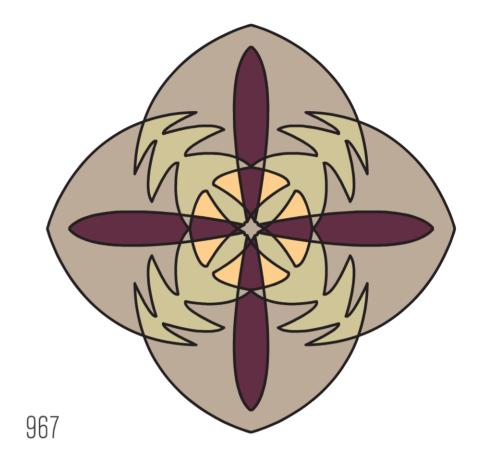
Waves

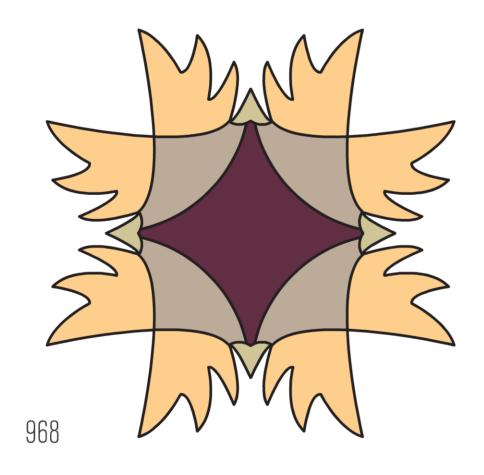


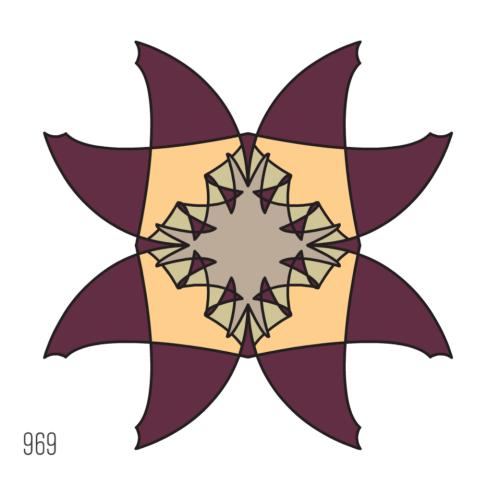


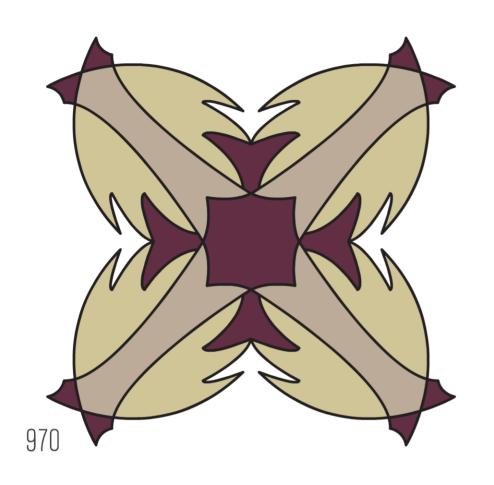


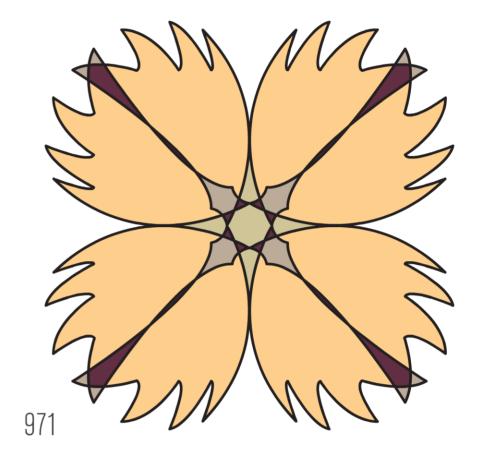


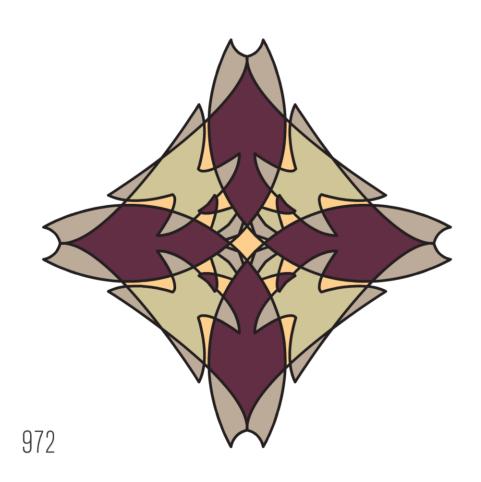


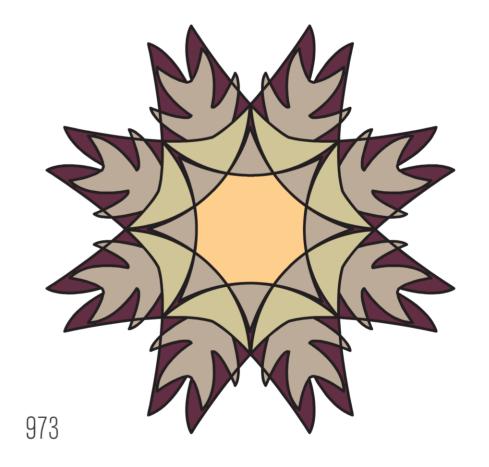


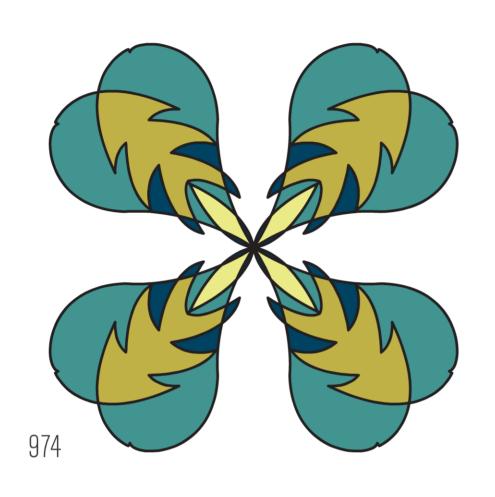




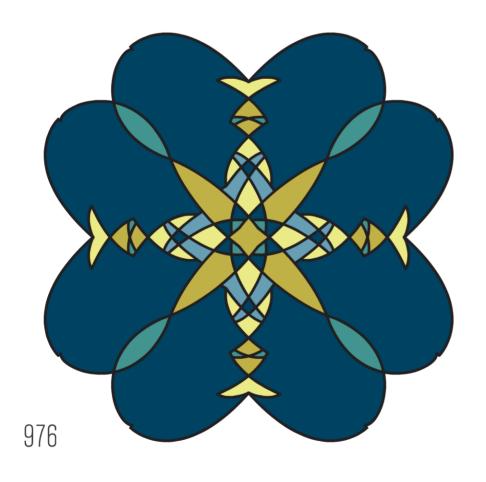


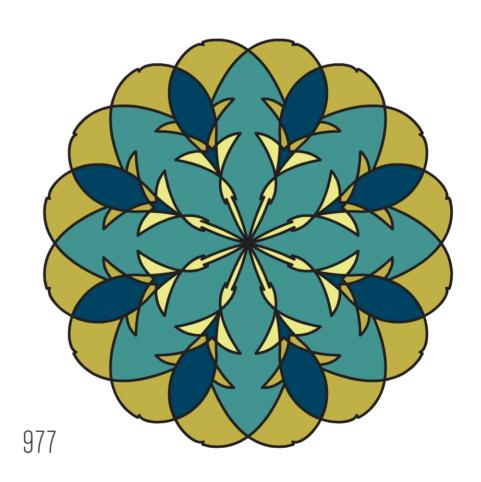




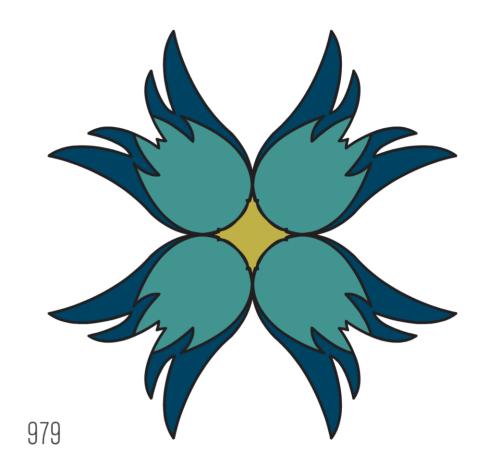


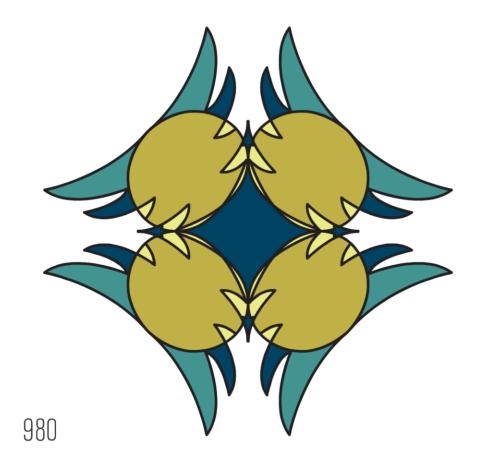


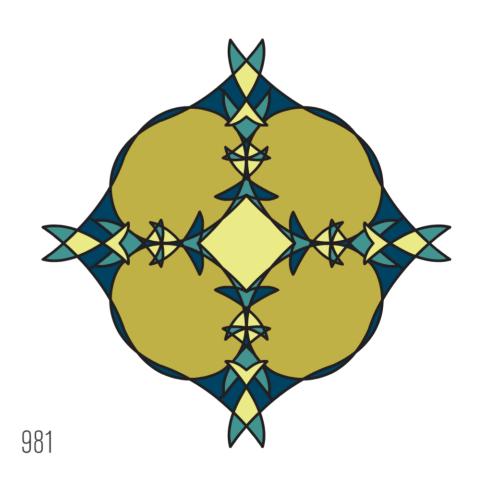




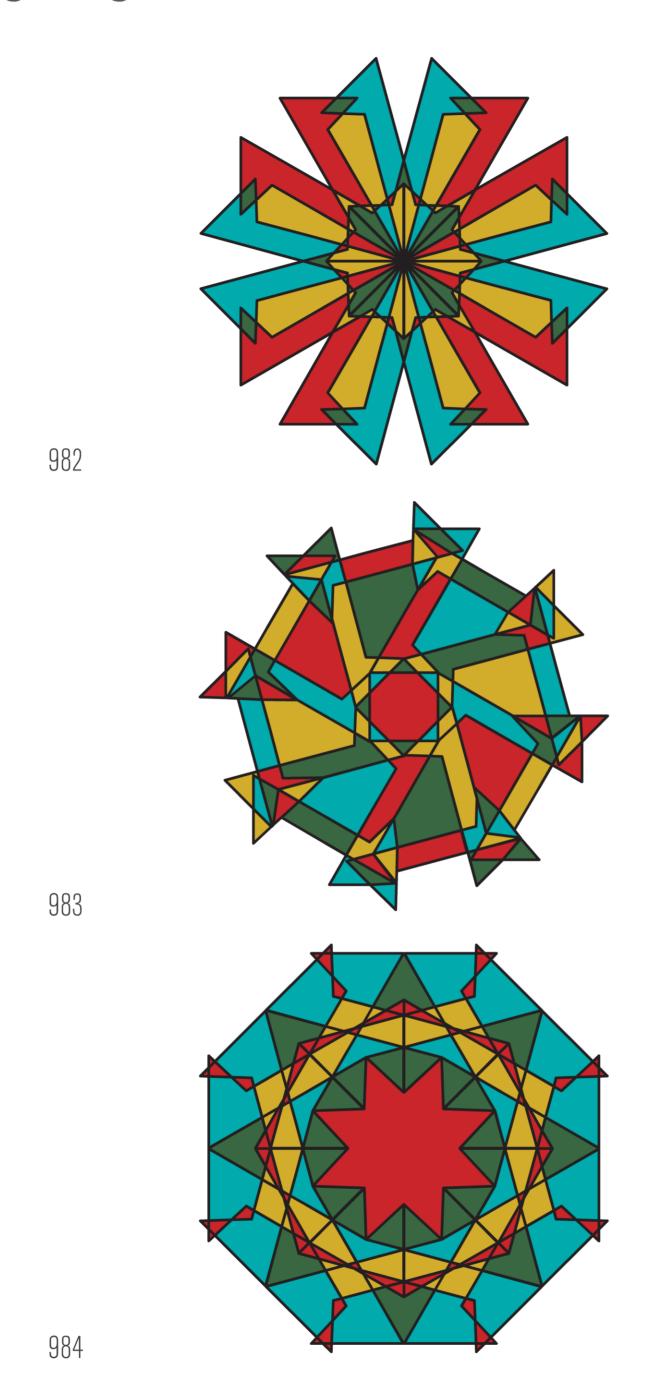






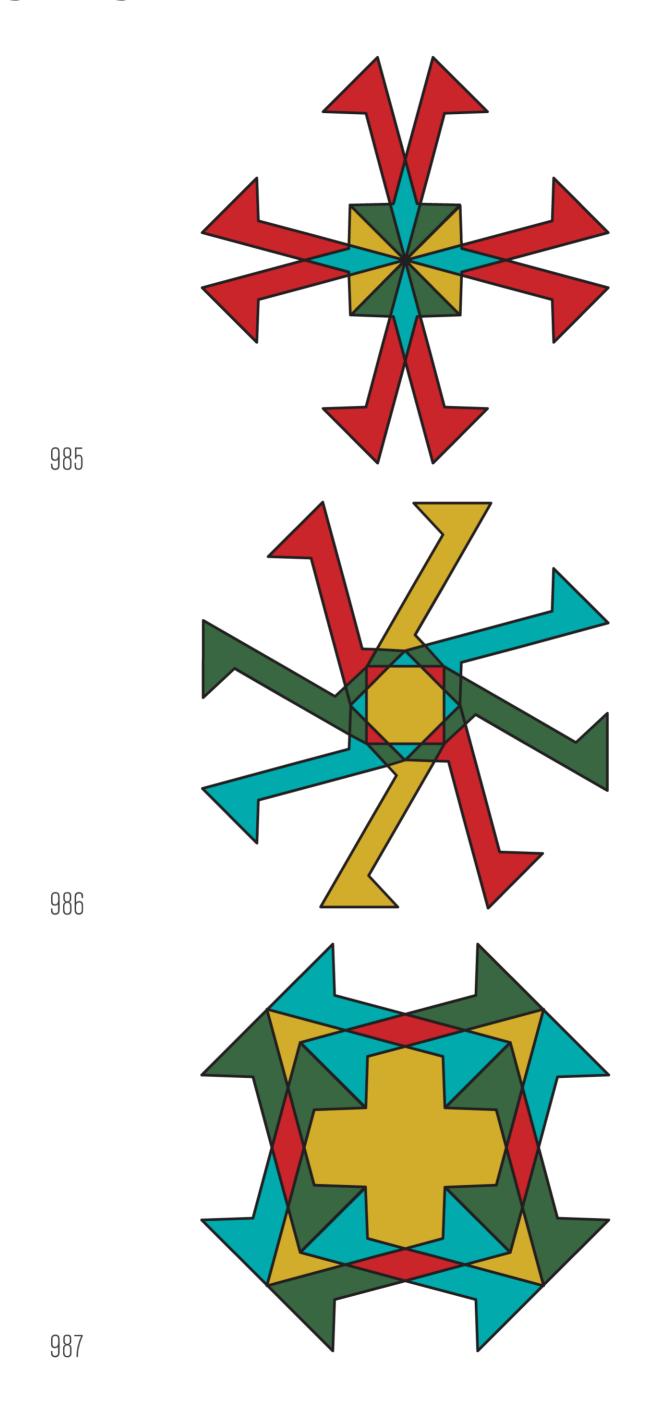


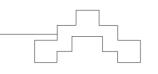
Zig Zags



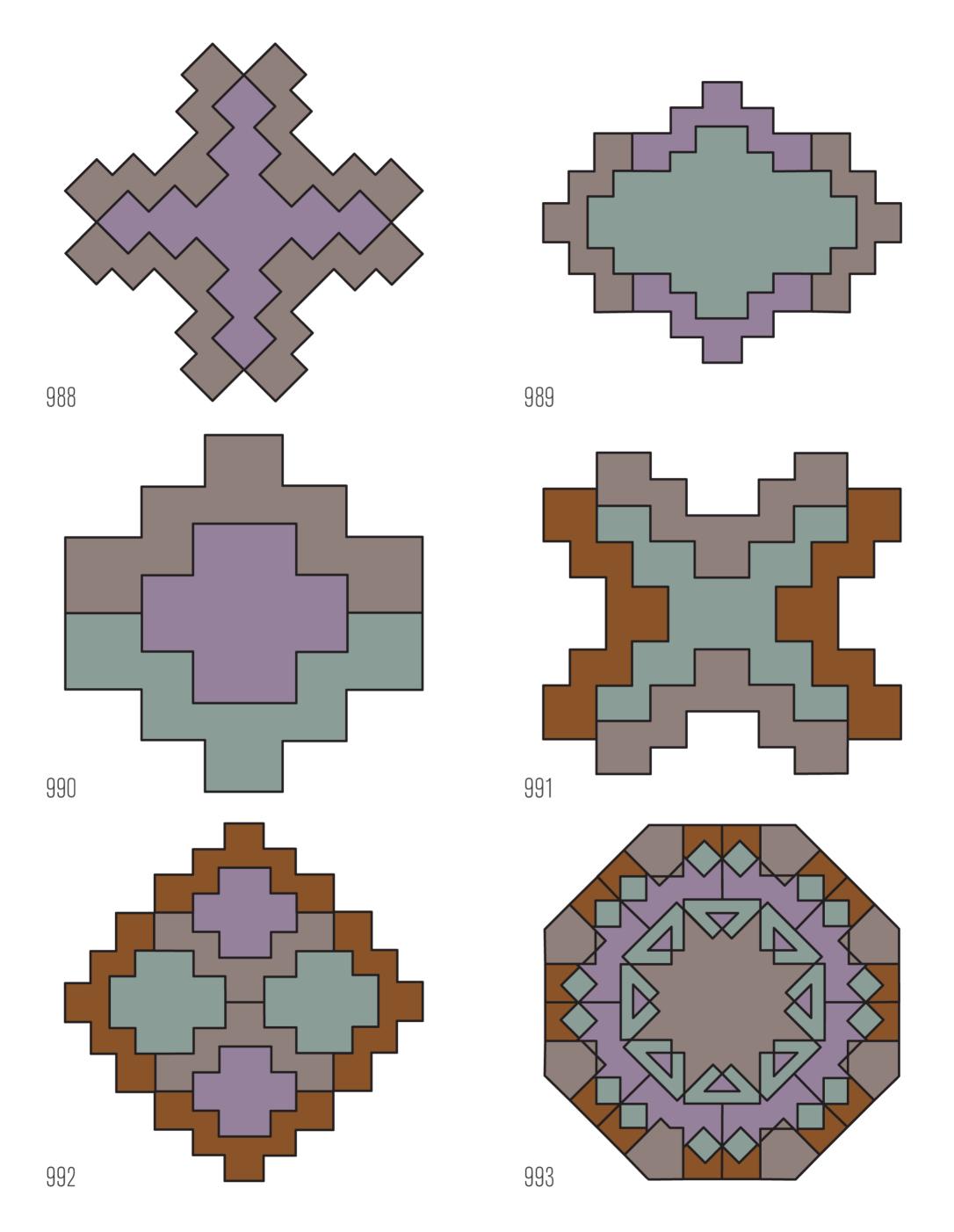
Zig Zags

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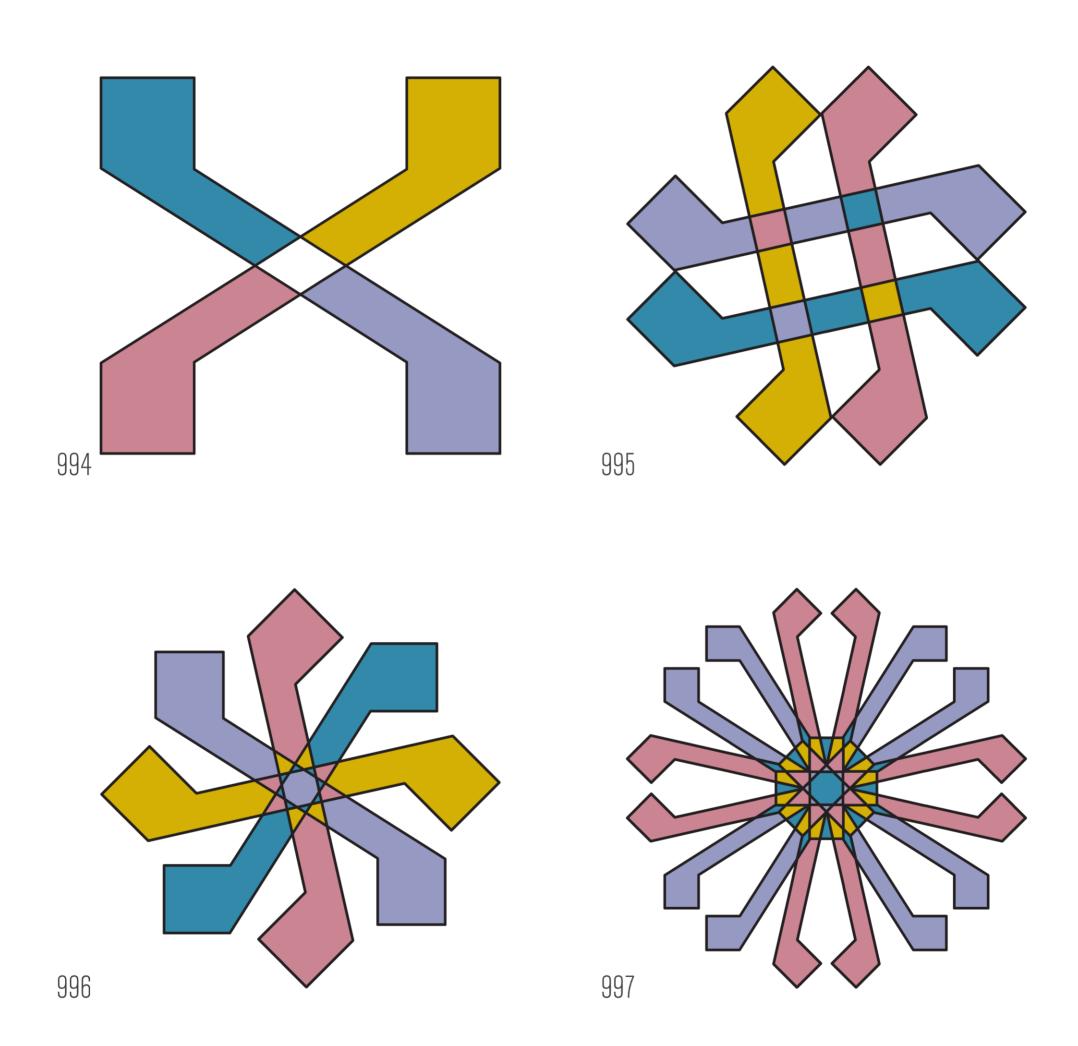


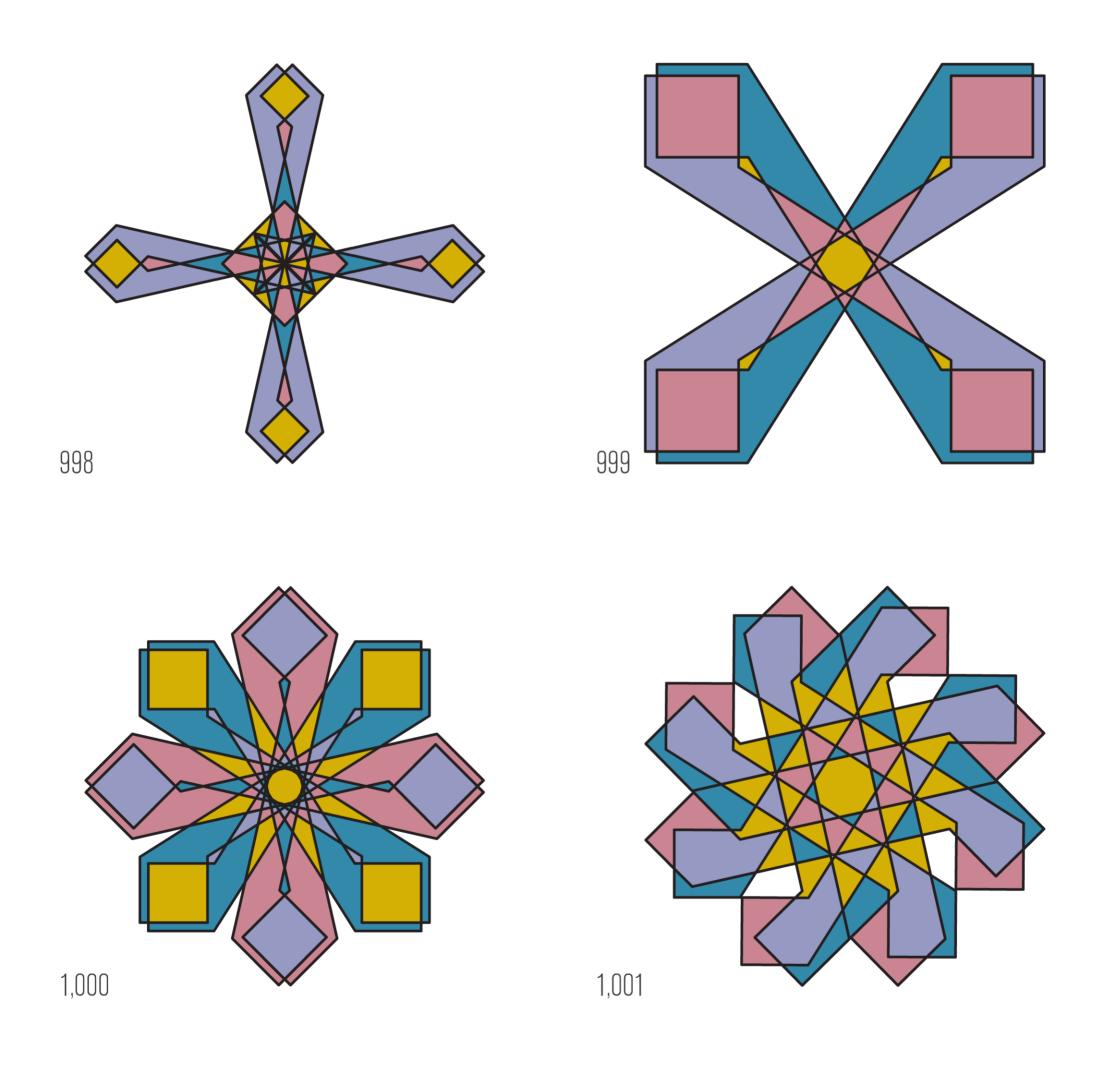


Zig Zags 2



Ziggurat





Footnotes

- 1. Conway, J. H., Burgiel, H., & Goodman-Strauss, C. (2008). *The Symmetries of Things.* Wellesley, MA: A. K. Peters.
- 2. Weyl, H. (1983). Symmetry. Princeton University Press.
- 3. Hargittai, I. & Hargittai, M. (1994). *Symmetry. A Unifying Concept.* Bolinas, CA: Shelter Publications Inc.
- 4. Washburn, D. K. & Crowe, D. W. (1991). Symmetries of Culture: Theory and Practice of Plane Pattern Analysis. Seattle, WA: University of Washington Press; (2004). Symmetry Comes of Age: The Role of Pattern in Culture. Seattle, WA: University of Washington Press.
- 5. Abas, S. J. & Salman, A. S. (1995). *Symmetries of Islamic Geometrical Patterns*. World Scientific.
- 6. Thornhill, R. & Gangestad, S. W. (1993). "Human Facial Beauty, Averageness, Symmetry, and Parasite Resistance." *Human Nature*, 4, 237–269.
- 7. Grammer, K. & Thornhill, R. (1993). "Human (homo sapiens) facial attractiveness and sexual selection: the role of symmetry and averageness." *Journal of Comparative Psychology*, 108, 233–242.
- 8. Jones, O. (2001). The Grammar of Ornament. Paris: L'Aventurine.

About the Authors

Jay Friedenberg is professor of psychology and chair of the psychology department at Manhattan College. He founded and directs the Cognitive Science Program at the college, whose mission is to educate undergraduates in and prepare them for graduate study in the cognitive sciences and allied fields. He also currently serves as department chairperson.

Friedenberg's research interests are in vision and he has published numerous articles on symmetry detection, center of mass estimation, and art perception. In addition to focused publications in the abovementioned areas, he has written a number of books on cross-disciplinary topics.

Jacob Roesch is an artist, designer, and educator whose work spans across many disciplines, from fine oil painting to children's book illustration. His work has appeared in numerous shows including *ORG:* Reaping the White Walls at the Macy Gallery, Ground Zero at the Detroit Museum of New Art, AGAST at the Gowanus Art Center, and Selected Works at the Carrie Haddad Gallery in Hudson, New York. Roesch currently teaches graphic design and digital drawing at Manhattan College and continues to hone his painting and design skills. He resides in Connecticut with wife, Diana, and his dog, Fergus.

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